Dear Editor/Typesetters,

This PDF document contains our point-by-point response to the two reviewers’ comments on our paper “Are seasonal calving dynamics forced by buttressing from ice mélange or undercutting by melting? Outcomes from Full Stokes simulations of Store Gletscher, West Greenland”.

We have also included a PDF of the latexdiff output, tracking changes between the initial and revised manuscript. Note that figures 6, 7 and 9 have been changed, as has the supplementary material, but latexdiff does not reflect this.

Yours sincerely,

Joe Todd and Poul Christoffersen
Response to Reviewer Comments on “Are seasonal calving dynamics forced by buttressing from ice mélange or undercutting by melting? Outcomes from Full Stokes simulations of Store Gletscher, West Greenland” by Anonymous Reviewer

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We are very grateful for the positive and constructive feedback from the reviewer. We address the reviewers points in turn below, with original comments in black and our responses in red.

I think that overall this is a fine paper, easy to follow, well written and clearly documented. It makes a significant contribution to the overall question of how ice melange and marine terminus undercutting by melting along the calving face exposed to the ocean influence calving rates and retreat or advance of Greenlandic outlet glaciers. I don’t think that the study settles any issues, but it still provides important knowledge and experience on the subjects. I also think that it may be that a false dichotomy is being implied without intending to be implied: is it really fair to say that ice melange back stress is more or less important than marine face undercutting? The two processes both have the potential to be important, and is it really fair to imply that they are in “competition”? As the paper clearly points out: the results hold for Store Glacier most precisely and may not apply to other situations. This might be pointed out more emphatically in the abstract (if it is not).

This is a fair point; while it was not our intention to imply that the processes of mélange buttressing and submarine melting are in direct competition, the choice of wording in the abstract may imply this. We have modified the abstract (p.3526,l.7-8) to read “On the other hand, the effect of submarine melting on the calving rate of Store Glacier appears to be limited.” as opposed to “secondary role” which may imply competition between the two processes.

- page 3529, line 23 - “annual formation and collapse” of melange. What is specifically meant by formation and collapse? e.g., does collapse mean “dispersal” or does it mean something else, and does formation mean that a previously empty fjord is then filled with icebergs?

We are principally interested in the presence of rigid mélange. We have modified the text (p.3529,l.23-25) to clarify this:

“The glacier is buttressed by a rigid proglacial mélange, which is typically present from late January or early February to the end of May (Howat et al., 2010). When
present, this rigid ice mélange has been shown to exert a significant backstress on the calving terminus of Store (Walter et al., 2012).”

– page 3535 line 25 - why is it necessary to apply a scaling factor? How would results change if no scaling were done?

We discuss the need for this scaling factor in Section 3.4, p.3535,l.13-24. Without the application of the scaling factor, the terminus continues to advance indefinitely into the fjord. We would emphasise, however, that the scaling factor used here is small compared to previous studies using crevasse-depth based calving models (Nick et al., 2010; Vieli and Nick, 2011), as discussed on p.3535,l28-p.3536,l2.

– Just a strange comment: The Norse were in Greenland before the Inuit. The Inuit apparently replaced the Dorset people who the Norse found in Greenland when they arrived before the Inuit. (At least, this is what I have heard or read.) So, is it really fair to use an Inuit word for ice melange rather than an Indo-European word? In fact, if there were to be appropriate attribution to the original native languages of Greenland, would an Icelandic term (representing a close approximation to Norse of Greenland) be better than both ice melange and sissusak? Is there a Dorset word for the same type of ice? Anyway, something that occurred to me now and then. . .

Interesting comment! A brief search didn’t reveal much info about what the Dorset people might call it. Previous studies have opted for either “ice mélange” (Amundson et al., 2010; Walter et al., 2012) or occasionally “sikussak” (Dowdeswell et al., 2000; Ryan et al., 2014). Here, we opt for the former which, being French, presumably falls under the broad heading of ’Indo-European’.

– Out of curiosity: Is it possible that bending moment at the ice front (due to sea water pressure alone) could cause the calving face to become non-vertical? If so, how does the rate of rotation of the vertical face due to bending moment of sea water compare to the effective rotation rate caused by a typical ice-front melting profile?
The stress situation at the calving terminus of Store Gletscher is quite complex. There is the persistent outward and downward bending moment, typical of calving glaciers, which results from the imbalance between the ice cliff and sea water pressure at the face itself. Counteracting this, there is an upward bending moment acting on the base of the floating section of the terminus; this is due to the glacier flowing downhill into the sea, below the level of neutral buoyancy, faster than ice creep allows it to adjust upwards. As such, the overall bending moment is difficult to ascertain, making the question difficult to answer. One might expect, however, that in the general case, this forward bending moment most likely results in the toppling of the subaerial seracs, followed by submarine calving events, before a significant slope in the calving front could form.

This wasn’t clear to me at about page 3541: Does the model predict “ice melange formation”? or is the presence or absence of ice melange as a boundary condition on the ice front independent of what calving is actually happening at the ice front in the model?

Our model focuses solely on the flow dynamics and response of the glacier itself. As mentioned on page 3538:11-7 we use the observations of Howat et al. (2010) to prescribe the presence or absence of ice mélange through the year, and those of Walter et al. (2012) to constrain the magnitude of the buttressing force.

page 3542: in the discussion, is it fair to say that submarine (presumably on the vertical or nearly vertical ice front) is “less important” in all cases of all possible glaciers? . . . or is this a result that could be more or less specific to the regime of the Store glacier? Is it possible to evaluate how representative the results of the present study are in determining a generality about the relative importance of the ice melange vs the submarine melting? I see that this is somewhat answered on the next page. . .

We don’t claim that submarine melting is less important than mélange for all possible glaciers. On the contrary, we interpret our results from Store as a reason this glacier has remained stable while others have retreated, and on page 3543 line 12 we state that this feature is most likely “specific to Store” in order to avoid implying that our results necessarily extend to other glaciers.
As to broader applicability of our results, Store Gletscher is characterised by its fast-flow and strong topographic control. We might expect Store’s characteristic “melt insensitivity” to be shared by other glaciers with similar topographic control. Although many glaciers have retreated, there is a growing body of evidence for contrasting behaviour of neighbouring glaciers (e.g. Moon et al., 2012). However, given that we presently only investigate Store itself, we feel that to make any more general claims in the paper would be overreaching.

References


Response to Reviewer Comments on “Are seasonal calving dynamics forced by buttressing from ice mélange or undercutting by melting? Outcomes from Full Stokes simulations of Store Gletscher, West Greenland” by Chris Borstad

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We are very grateful to Dr Borstad for his thorough, technical and insightful review of our paper. We address the points in turn below, with original comments in black and our responses in red.

1 General Comments

This paper outlines a model study of the terminus position and stability of Store Gletscher in West Greenland. A model is applied that solves the full-Stokes momentum equations along a central flowline of the glacier, with a basal friction field determined from inverse methods. The glacier is considered isothermal, and the geometry of the glacier is constrained using remote sensing data. The grounding line and the ice front position are allowed to freely migrate, and the model is capable of representing the development of a floating ice tongue. A novel flux convergence term is added to the incompressibility equation to account for lateral convergence or divergence in the flow. The stress field computed in the model is used to calculate the theoretical depth to which surface and basal crevasses would propagate, and calving is assumed to occur whenever surface and basal crevasses meet. Perturbation experiments are run with different combinations of undercutting by melting and buttressing by mélange to explore the calving dynamics of the glacier and its response to possible future climatic changes. The results indicate that the geometry of Store is principally responsible for its observed interannual stability, but that buttressing by mélange (which suppresses calving) is likely responsible for the seasonal advance of the glacier.

The perturbation experiments are well constructed, and a reasonable range of variability in mélange strength and duration and submarine melt strength and duration are explored. I think it would have been revealing to explore what conditions would be necessary to get Store to retreat into the overdeepening behind the basal pinning point and the constriction in fjord width. Even if you had to use unrealistic values of submarine melting or negative SMB or get rid of mélange altogether, it could be instructive to see what it would take to destabilize the glacier. This might also prove illustrative of the fidelity of the model setup. I find the discussion of the perturbation experiments a bit hard to follow in places (it’s hard to keep track of all the different numbers...
and ratios of years being used), and some of the figures could be improved for legibility (e.g. coloring and scaling). Otherwise I think this is a novel contribution that will be well received by the glaciological community. Most of my comments are minor and can likely be addressed relatively easily.

2 Specific comments

1. Were there any indications prior to your modeling work that the topography of Store was the principal reason for its interannual stability? If the fjord bottleneck and basal pinning point were known, then it’s probably not surprising to find that geometry is the most important factor. This makes me wonder why Store was chosen, as there are surely other glaciers for which mélange and undercutting by melting might be much more important for determining glacier stability and terminus position. I do agree that it is a valuable result to demonstrate that glacier geometry is more important in this case, but you might give a bit more motivation for why Store was chosen (even if it is just for the availability of data to constrain the model). The sophistication of the model setup might also be used to find (or construct synthetically) a glacier for which it can be demonstrated that mélange or melt undercutting (or some combination of the two) are the dominant influences on tidewater glacier behaviour.

Store Gletscher is the target of an extensive, ongoing field investigation by our department, in collaboration with Aberystwyth University. This field campaign aims to answer questions both about the calving dynamics and the basal conditions of Store. The availability of this data is one of the main reasons for choosing this glacier.

Additionally, we feel that if we seek to use new models to understand and reproduce long-term changes in the dynamics of calving glaciers, we should first attempt to investigate the seasonal changes onto which these longer term trends are imposed. Store Gletscher is ideal from this perspective, as it displays a large seasonal range in dynamics while maintaining long term stability. As such, we are able to focus on investigating the “normal”
behaviour of a fast-flowing outlet glacier, before attempting to investigate how long term change throws these systems into disequilibrium. We have added a brief statement about the suitability of Store (p.3528,l.27).

We agree that an investigation into various synthetic geometries would be interesting and we would consider this for future work, but we believe it to be outside the scope of this investigation.

Related to this comment, and to the general comments above, we experimented with unphysically large values for melt rate in order to force retreat into the trough. We found that melt rates larger than velocity were required to force this retreat. We chose not to include these results as they are not representative of a real climate scenario. Furthermore, following the commencement of rapid retreat through the trough, we found that the model breaks down after ~25km of retreat, before reaching a stable pinning point. This is because the model currently doesn’t include the ability to fully remesh the glacier geometry; rather, we manipulate the location of the nodes following a calving event. This works well for all but the most extreme changes in geometry. This is something we hope to improve upon by undertaking full remeshing in future work.

We have updated the text at p.3544,l.1-3 to mention this result: “We found that, by forcing the model with unphysically large values for submarine melt rate (not shown), we were able to force the terminus back off its pinning point, which led to rapid retreat through this trough.”

2. How much of the seasonal signal in ice front position is due to the imposed seasonal signal in basal friction? You might have attempted to partition the influence of this seasonality in basal friction by running some simulations with some kind of constant, annual-average friction at each point. The no-mélange results in Figure 6b seem to show evidence of this annual periodicity, which looks to be small here. However, the removal of mélange and the seasonal reduction in basal friction are likely (I’m guessing) to occur around the same time, and their combined influences may not necessarily be linear combinations of two separate effects.
Seasonal changes in basal friction have an effect on velocity at the terminus, but appear to have a negligible effect on terminus position. The blue lines in Fig. 5a,b show terminus position and velocity, respectively, for model simulations where changing basal friction is the only imposed perturbation (Also shown in Fig. 6). While the effect on velocity is clearly discernible, front position remains constant throughout the year. As such, we maintain that changing basal friction has no effect on calving front position in our model.

3. The theory behind the crevasse depth models contains the assumption that crevasses are closely spaced, which will lead to stress shielding and reduce the high stress concentration that would otherwise surround an isolated crack tip. Since you are applying these calculations everywhere in the glacier domain, you are implicitly assuming that crevasses are closely spaced everywhere. You might comment on how reasonable this is. It may not be too bad for surface crevasse fields, but what about basal crevasses? What would the implications be for basal crevasse penetration (and thus calving size/frequency) if basal crevasses form less frequently and are actually isolated rather than closely-spaced fractures?

This is a good point. For surface crevasses on Store Gletscher, we are confident that this is a good assumption; aerial photography over the terminus of Store presented by Ryan et al. (2014) show that surface crevasses are indeed closely spaced. If basal crevasses were found to be more sparse, the stress concentration effect would be larger, and so these crevasses would penetrate further upwards into the glacier. However, there is no data available as to the spacing of the basal crevasses, and so we choose to include them within the same theoretical framework for simplicity.

4. You mention (p. 3541) that in some cases the terminus position during the melt season is actually more advanced. You don’t mention how often this is the case, but you seem to brush off this result, suggesting that the calving dynamics appear unaffected by increasing melt magnitude. I think this point deserve more attention, however, as it seems like it could be important. Under what conditions do you see a terminus advance during the melt season? Does this depend on melt season length? What explains this behaviour?
The graph in Fig. 9 shows the location of the surface of the terminus, as opposed to the depth-averaged front position, or the location of the terminus ‘toe’. We chose to present the data in this manner to maintain consistency with observational records of front position. The variability of the front position between different melt perturbation experiments is of the order of 200m. Somewhat counter-intuitively, these ~200m advances occur as a result of progressive undercutting. Calving appears to more strongly dictate the location of the ‘toe’ than the surface, and so, as progressive undercutting occurs, the toe remains in the same position, and the surface advances. A higher melt-rate is more rapidly able to undercut the terminus, and so the surface is able to advance further away from the toe before calving occurs. We have added the following to the text to better explain this (p.3541,l:23-27):

The response of the modelled terminus to increasing melt magnitude appears somewhat stochastic. It should be noted, however, that the positions shown in Figures 5, 6 and 9 represent the terminus at the surface, which is able to advance into the fjord when undercutting takes place, due to the fact that the glacier’s topography exerts a control on the position of the grounding line.

3 Line-by-line Comments

- p. 3526, line 18: remove comma after factors Done, thanks
- p. 3527, line 5: “this process” is a bit vague here, perhaps be a little more specific Agreed, changed.
- p. 3528, lines 8–10: are you sure this is conclusive, i.e. is there still any debate about this in the literature? I still hear people question whether the advance and retreat of some tidewater glaciers coincident with the appearance and breakup of mélange, respectively, is simply coincidence. Could we be missing anything else physical here? This is more of a minor discussion point, but it might be worth adding a bit of nuance
since this is introductory material that frames your work (which of course addresses this very issue, but not until the results are presented...).
This is a good point, and is a good justification for why a modelling study is needed! We have updated the text to reflect this. (p.3528,l.7,l.15)

– p. 3528, line 29: what about the last two decades? Your reference here from 1995 doesn’t address what has happened since then, which is quite a long time... True, we have added a reference to (Howat et al., 2010), which demonstrates stability over the past decade.

– p. 3530, line 3: when I think of a “range,” I think of two numbers that define some kind of upper and lower bounds. Do you mean $6600 \pm 700$ m a-1 here? This is indeed how you use the term “range” in a couple lines, but then you go on to talk about a range of 500 m for ice front position. Maybe a term like “variability” or something like that would be more appropriate in a few places?
Yes true. Changed where appropriate

– p. 3532, lines 5–8: Do you mean that for every date of the year, you take the average of the RACMO SMB for that date in every year from 1985 to 2008?
No. Because we do not investigate the effect of seasonal variability in SMB on calving (assuming it to be negligible), we impose a constant annual SMB throughout the simulations. This average annual SMB was found by averaging the entire record from 1985 to 2008.

– p. 3534, line 4: this term is not really a creep closure term, but an overburden (or cryostatic) pressure term that leads to creep closure. True, changed

– p. 3534, lines 14–17: just because you interpolate something within your mesh does not make the results independent of the mesh, as the stress results themselves may have some mesh sensitivity (have you checked for this?). Furthermore, the interpolation depends on your choice of basis functions (linear, quadratic, etc.).
You are right that the results are not independent of mesh resolution. We have changed “independent of the model’s mesh resolution” to “reasonably insensitive to the
model’s mesh resolution” on p.3534,l.16-17. The reason for saying this was that, prior to implementing the interpolation, calving wouldn’t occur until an individual node experienced both surface and basal crevassing. This setup meant that the occurrence of calving was totally dependent on the distribution of nodes in the mesh.

When experimenting with model setup, we tried different mesh resolutions at the terminus, and chose a resolution which we were confident was sufficiently high to capture the near-terminus stress field and beyond which little was gained.

- p. 3534, line 19: the cryostatic pressure will be higher than other terms at the bed. There are no rate terms in Eq. 3. True, changed.

- p. 3534, line 25: I’m confused here. Negligible difference in pressure at a given depth? i.e. between the open water and within a basal crevasse near the ice front? Yes, or in other words, negligible difference in theoretical borehole water level at any point near the front. We have changed the text to clarify this, thanks.

- p. 3535, line 18: it seems like you could come up with some kind of geometric normalization of the sidewall friction near the terminus to account for the arcuate shape of the ice front. Or do you think your overestimation of friction in this zone is negligible?

  It is not completely clear to us what exactly the reviewer has in mind with regards to geometric normalization and have left the text unchanged.

- p. 3535, line 22: this is a bold statement, that a crevasse field “significantly” reduces bulk density. Of course the bulk density should be reduced, but it’s not clear why this is necessarily significant. I would think that would depend on the specific geometric setting.

  We agree that crevassing may not always lead to “significant” change in bulk density, so we have changed “significantly reduces” to “may significantly reduce” on p.3535,l.22.
– p. 3539, line 20: I’m not sure what you mean here by “super-buoyancy,” can you define this term? I think you describe what is going on here a little better in the caption of Figure 7.

We have updated the text to clarify. By “super-buoyancy” we meant that the ice is being forced below the flotation level, and is then progressively forced back up out of the water by buoyant forces acting on the base.

– p. 3540, lines 9–11: this is confusing here. Velocity at a location is faster than a date?

Changed, thanks.

– p. 3540, line 12: fix “with the a significant...”

Done, thanks.

– p. 3545, lines 12-13: the Krug reference was actually applied to Helheim glacier, not a synthetic glacier geometry. Yes, true, our mistake.

– p. 3545, line 25: the presence of water in crevasses is not necessary for seasonal dynamics at Store (my emphasis). Fair point, changed.

– Figure 6: this figure is difficult to read. The colors are difficult to discern. I’m not sure it’s necessary to show 5 years of results, as there isn’t a lot of interannual variability. It might be better to just show 1 or 2 years, and work with the color scheme to aid in interpretation.

In producing this figure, we were faced with the challenge of maintaining readability whilst also convincing the reader that our model is interannually stable. Taking your feedback into account, we’ve opted for 3 years, as 5 was probably unnecessary.

– Figure 9: perhaps clarify in the caption that the panel titles are in fractions of a year. It took me a while to figure this out. It might be worth labeling each sub-panel (a through f), as it took me a while to figure out what each panel meant and how the experiments varied left-to-right as well as top-to-bottom. There’s a lot of good information in this figure, it just took me a while to get it!

Thanks for the useful feedback on this figure. We agree it is quite complicated and could be clarified. We’ve labelled each sub-panel as you suggest and included explanatory titles above the fractions of a year.
Supplemental Equations S3 through S5: in S3 and S4 you use \( U_x \), but in S5 you use a lower case \( u_x \). Is there supposed to be a difference?

No, this was a mistake, thanks for pointing it out.

Supplemental: proponents of XFEM would take issue with your claim that FEM is “inherently incapable of dealing with fracture...” It is possible to account for fractures with the use of suitable enrichment functions in XFEM.

This is interesting, and wasn’t something we had come across before. When thinking about how to modify the text accordingly, it occurs to us that it’s not the inability to deal with fracture that’s the problem, it’s the instantaneous change in domain shape. The method outlined in this section would still be required even with a proper treatment of crack propagation. We have changed the text to reflect this and to avoid the claim that FEM can’t handle fracture.

Supplemental S6 and thereafter: I was confused by the use of \( H \) as a surface elevation variable. I kept thinking of thickness in my head. Wouldn’t it make more sense to use something like \( z_{\text{bed}} \) and \( z_{\text{surf}} \) in Eqs. S6 and S7 (and in the figure)? What you’re trying to show (in words, and correct me if I’m wrong) is that the height variable on the bed is equal to the surface elevation of the bed, and same for the surface. It’s kind of confusing the way you’ve written the equations.

Yes, we should have avoided capital \( H \), due to its typical use to define thickness. However, we want to highlight the distinction between the height variable and the \( z \) coordinate, so we opt to change to lowercase “\( h \)” rather than \( z_{\text{bed}} \) and \( z_{\text{surf}} \). This also emphasises the fact that “\( h \)” is the same variable through the domain, and we simply set its boundary conditions based on the \( z \)-coordinate of the surface and bed.
References


Are seasonal calving dynamics forced by buttressing from ice mélange or undercutting by melting? Outcomes from Full Stokes simulations of Store Gletscher, West Greenland

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Abstract

We use a full-stokes 2D model (Elmer/Ice) to investigate the flow and calving dynamics of Store Gletscher, a fast flowing outlet glacier in West Greenland. Based on a new, subgrid-scale implementation of the crevasse depth calving criterion, we perform two sets of simulations; one to identify the primary forcing mechanisms and another to constrain future stability. We find that the mixture of icebergs and sea-ice, known as ice mélange or sikussak, is principally responsible for the observed seasonal advance of the ice front, whereas submarine melting plays a secondary role. On the other hand, the effect of submarine melting on the calving rate of Store Gletscher appears to be limited. Sensitivity analysis demonstrates that the glacier’s calving dynamics are sensitive to seasonal perturbation, but are stable on interannual timescales due to the glacier’s topographic setting strong topographic control on the flow regime. Our results shed light on the dynamics of calving glaciers while explaining and may help explain why neighbouring glaciers do not necessarily respond synchronously to changes in atmospheric and oceanic forcing.

1 Introduction

Recent studies show accelerating net mass loss from the Greenland Ice Sheet (GrIS) (Khan et al., 2010; Rignot and Kanagaratnam, 2006; Howat et al., 2007), raising concerns about its future response to changing global climate and the impact this might have on global sea level. The two factors which govern this loss, are 1) an overall negative surface mass balance stemming from intensified surface melting in the ice sheet’s ablation zone (Hanna, 2005; van den Broeke et al., 2009; Enderlin et al., 2014), and 2) faster rates of ice discharge through calving glaciers which terminate in fjords (Luckman and Murray, 2005; Howat et al., 2005; Rignot and Kanagaratnam, 2006; Howat et al., 2007). The latter (dynamic) mechanism accounted for ~67% of the total net ice loss in 2005 (Rignot and Kanagaratnam, 2006), but less in recent years (Enderlin et al., 2014), highlighting the sensitivity of Greenland’s marine-terminating glaciers to the transient pulse of warm Atlantic water eircumnavi...
fjords over the last decade (Holland et al., 2008; Straneo et al., 2010; Christoffersen et al., 2011).

Owing to the advancement of surface mass balance models over the last two decades (Hanna, 2005; Box et al., 2006; van den Broeke et al., 2009; Enderlin et al., 2014), this process is well represented in global sea level predictions (Stocker, 2013) (IPCC, 2013). The rapid dynamics associated with sudden increases in the discharge of ice into fjords by marine-terminating glaciers are, on the other hand, complex and poorly understood, and their relationship with climate remains elusive and is so far unconstrained (Stocker, 2013) (IPCC, 2013). The main processes involved in rapid dynamics are fast glacier flow and calving, i.e. the mechanism whereby pieces of ice and bergs break off glaciers terminating in water. These processes are complex because they interact with and respond to atmospheric as well as oceanic forcing effects. As such, calving and its associated dynamics comprise one of the most significant uncertainties in predictions of future ice sheet mass balance and sea level change.

While atmospheric processes were previously thought to be the main driver of rapid ice sheet dynamics (Zwally et al., 2002), recent studies point to warm water in coastal currents as the main forcing of mass loss by discharge (Holland et al., 2008). The rapid acceleration of Jakobshavn Isbræ from ~4,000 m a\(^{-1}\) in 1995 to ~17,000 m a\(^{-1}\) in 2012, is clearly linked to the continuing retreat of the calving ice front over this period (Joughin et al., 2012, 2014), and it has been hypothesised that submarine melting plays a crucial role in driving this retreat (Holland et al., 2008; Motyka et al., 2010). Space-borne tracking of calving fronts also show that recent glacier retreat along the East Greenland coastline has been widespread and synchronous below 69\(^{\circ}\)N, but largely absent at higher latitudes, where coastal water is much colder (Seale et al., 2011). This suggests that these glaciers are retreating in response to changes in the ocean system. Warmer fjord water increases the rate of submarine melting of the calving terminus. This effect is further amplified by atmospheric processes; buoyant pro-glacial plumes, driven by the delivery of surface meltwater to the terminus by the subglacial hydrological system, are capable of significantly increasing melt rates (Jenkins, 2011). Undercutting of calving ice fronts by submarine melting should, in addition, amplify calving rate due to the stress response (O’Leary and Christoffersen, 2013).
The formation of ice mélange, a rigid mixture of bergs and bergy bits, held together by sea-ice, henceforth referred to simply as mélange, may also play an important role with regard to rapid ice sheet dynamics (Sohn et al., 1998; Joughin et al., 2008). Data from Jakobshavn Isbræ indicate a complete cessation of calving when the glacier is buttressed by mélange, a response that explains why the glacier advances by up to 5 km in winter (Amundson et al., 2008) and why the glacier retreats suddenly when the mélange disintegrates (Joughin et al., 2008). A similar correspondence between mélange clearing date and increasing calving rate has been found for a number of glaciers, including those near Uummannaq in West Greenland (Howat et al., 2010). Walter et al. (2012) used changes in velocity observations and a force balance technique to infer a buttressing stress of 30-60 kPa exerted by mélange onto the terminus of Store Gletscher. This buttressing effect, and the effect of submarine melting (Xu et al., 2013), appear to be crucial for the calving dynamics of this glacier. However, temporal correlation is insufficient evidence to confidently attribute seasonal calving retreat to either the collapse of ice mélange or submarine melting. This highlights the need for numerical modelling to attempt to partition these effects.

In this paper we present results from a numerical model developed using the open-source finite element (FEM) modelling package, Elmer/Ice, with newly implemented calving dynamics. Theoretical consideration of the calving process indicates the importance of the near-terminus stress field in controlling the propagation of crevasses and the detachment of icebergs (Nye, 1957; van der Veen, 1998a,b; Benn et al., 2007a,b). Linking calving to crevasse propagation and stress in this way provides a useful and physically-based framework for investigating calving in numerical models of glacier dynamics. Here, we implement a calving model based on the penetration of both surface and basal crevasses (Nick et al., 2009, 2010), and incorporate the full stress solution into the crevasse depth criterion, after Nye (1957). We use this model to investigate the seasonal dynamics of Store Gletscher, a fast flowing outlet glacier in the Uummannaq region of West Greenland, near Uummannaq in West Greenland, which experiences a large seasonal variability in dynamics and front position (Howat et al., 2010), but has been interannually stable for at least four decades (Howat et al., 2010; Weidick et al., 1995, p.C41). The stable, seasonal calving dynamics of Store, along with the recent discovery of a 28km long
tough behind the terminus, extending 900m below sea level, make this glacier an ideal target for stability analysis as well as process study.

To examine the calving process, we focus on the calving front's position and seasonal fluctuation, which have been stable and periodic, respectively, for at least four decades (Weidick et al., 1995). We investigate the effects of submarine melting, mélange buttressing and glacier geometry on calving, with the aim of identifying the role of each mechanism in driving the observed seasonal variability at the front. We find that mélange is likely to be the primary driver, and that submarine melting plays a secondary role. We also find that the topographic setting of Store Gletscher is responsible for its observed stability.

2 Store Gletscher

Store Gletscher, henceforth referred to as Store, is a fast-flowing marine terminating outlet glacier located in Ikerasak Fjord, near Uummannaq in West Greenland (Fig. 1). The glacier drains an area of 35,000 km² and is 5 km wide at the terminus, where surface velocity reaches ~6,600 m a⁻¹ (Joughin et al., 2011). The location of the terminus coincides with a bottleneck in fjord width (Fig. 1), as well as a pronounced basal pinning point (Fig. 2), suggesting that fjord topography may play an important role in calving dynamics.

In terms of climate, data from the Regional Atmospheric Climate Model (RACMO) suggest that ~2 km³ of meltwater forms on the surface of Store between June and August (Ettema et al., 2009). Recent modelling work (Xu et al., 2013) show that submarine melting at the terminus may occur at rates of 8 m d⁻¹ in summer because a large proportion of runoff is discharged subglacially into Ikerasak Fjord. The latter is established from observations, which show upwelling of dirty, subglacially derived meltwater near the centre of the calving ice front during summer months (Chauché et al., 2013) (Chauché et al., 2014) (Fig. 1). The high melt rates are caused by entrainment of warm ambient fjord water into buoyant meltwater plumes, which rise rapidly in front of the glacier, from a depth of 490 m below sea level due to forced convection (Jenkins, 2011). The annual formation of (Chauché et al., 2014; Jenkins, 2011). The glacier is buttressed by a rigid proglacial mélange occurs in, which is typically present from late January
or early February and it tends to collapse around to the end of May (Howat et al., 2010). When present, this rigid ice mélange has been shown to exert a significant backstress on the calving terminus of Store (Walter et al., 2012).

Store exhibits characteristic seasonal variabilities in terms of calving front position and velocity (Howat et al., 2010). Estimates of the terminus velocity of Store differ depending on where and when data were obtained. The most recently collected TerraSAR-X data, obtained from the NASA’s MEaSUREs Project (Joughin et al., 2011), measure a peak velocity of 6,600 m a\(^{-1}\) at the calving front with a seasonal range variability of ~700 m a\(^{-1}\). Howat et al. (2010) measured velocities a few km behind the terminus and found values ranging from 2500 m a\(^{-1}\) to 4200 m a\(^{-1}\) between 2000-10. Howat et al. (2010) also tracked changes in front position through time, finding a seasonal range variability of at least ~500 m, when averaged across the width of the terminus. This is consistent with time-lapse photography showing seasonal advance of ~1 km near the central flowline (J. Box personal communication).

3 Methods

In this work, we use Elmer/Ice in a 2D configuration to model the central flowline of Store. The modelled flowline is 113 km long and covers the region from the 100 m a\(^{-1}\) ice velocity contour to the calving front (Fig. 2a). The flowline was produced using velocity vector data from the MEaSUREs Project (Joughin et al., 2011).

We use a 2D modelling framework in which both calving front and grounding line evolve freely through time. Whereas the representation of processes in 2D requires parameterisation of key out-of-plane effects, as explained below, it is a practical first step which will guide and help the future development of transient implementation of calving processes in full 3D.

3.1 Elmer/Ice Dynamics

Elmer/Ice is a finite element model, which solves the Stokes equations and uses Glen’s flow law as a constitutive stress/strain relation (see Gagliardini et al. (2013) for details). The finite ele-
ment approach is a flexible solution, which allows us to vary the spatial resolution of the model and thereby focus on the dynamics at the calving ice front (Fig. 2b). Because we are principally interested in capturing processes at the calving terminus, we adopt a spatial resolution which varies from 250 m in the upper region of the glacier to 20 m near the terminus (Fig. 2b). The model evolves through time with a timestep of 1 day.

Temperature is an important factor in the stress-strain relationship of ice (Cuffey and Paterson, 2010). However, near the terminus, which is our region of interest, extensive crevassing makes the implementation of temperature difficult. The ability of subglacial meltwater to penetrate upwards through basal crevasses, as well as the effect of air circulation in surface crevasses, is likely to significantly affect the temperature profile of the ice. Due to these complications, and the lack of observations to constrain ice temperature, we assume for the sake of simplicity that the glacier is isothermal at -10°C.

Because basal friction exerts a critical control on the dynamics of fast flowing glaciers in general, we first use the adjoint inverse method (Gillet-Chaulet et al., 2012) to identify the basal friction profile which results in surface velocity as observed along the flowline. The result of the inverse method is a profile for the basal friction parameter ($\beta^2$) which is related to basal velocity ($U_b$) and basal shear stress ($\tau_b$) by the relation (MacAyeal, 1992):

$$\tau_b = \beta^2 U_b$$  \hspace{1cm} (1)

To integrate seasonal variation in ice flow in response to seasonal change in basal friction, we run the inverse model for both the summer and winter observed velocity profiles, thereby obtaining two basal friction profiles. A seasonal variability in ice flow, very similar to what is observed in reality, is imposed by varying the basal traction coefficient sinusoidally between summer and winter values.

### 3.2 Boundary Conditions

Initial surface elevation along the modelled flowline is prescribed from the GIMP DEM product (Howat et al., 2014). The bed profile is obtained from airborne geophysical surveys carried out by the Greenland Outlet Glacier Geophysics (GrOGG) Project and NASA’s Operation IceBridge.
We use a mass-conservation algorithm similar to that of McNabb et al. (2012) to constrain ice thickness and bed topography in the heavily crevassed region of fast flow near the terminus, where radar data are sparse.

Ice thickness evolves through time according to the mass continuity equation (Cuffey and Paterson, 2010), and we add and subtract mass according to RACMO surface mass balance data averaged between 1985 and 2008. The ice surface is treated as a stress free boundary, as we assume atmospheric pressure to be negligible. At the ice base, friction is prescribed through inverse methods as described above, except under the floating tongue which, when it exists, is a frictionless free surface. At the calving terminus, we apply an external pressure equal to the hydrostatic pressure from seawater (see Equation 5 below). Above sea-level, atmospheric pressure is neglected.

We simulate the seasonal advance and retreat of Store Gletscher’s floating tongue using an implementation of grounding line dynamics developed by Favier et al. (2012). The grounding line algorithm compares external water pressure and ice overburden pressure to detect where the glacier is floating, and modifies basal friction accordingly.

3.3 New scheme for implementation of flow convergence

Similar to most outlet glaciers, Store undergoes significant lateral narrowing as ice flows from catchment to coast. As such, it is important that dynamic effects from sidewall drag (Raymond, 1996) and ice convergence (Thomas et al., 2003) are accounted for.

Gagliardini et al. (2010) implemented a parameterization for sidewall friction in Elmer/Ice, and we use it here. The issue of ice convergence in full-stokes 2D models, however, has thus far received little attention from the glacier modelling community. Here, we developed a routine which adds flux sources to elements along the flowline, corresponding to the downstream narrowing of the glacier. We derive a flux convergence term (see Supplementary Material) and add it to the Stokes incompressibility equation (Eq. S1), such that:

\[ \nabla \cdot \mathbf{u} = -\frac{dW}{dx} W^{-1} u_x A \]  

(2)
where \( \mathbf{u} \) is the velocity vector, \( W \) is glacier width, \( u_x \) is the along-flow component of velocity and \( A \) is the area of the element.

This convergence term represents an important 3D effect, ensures that mass balance is maintained throughout the model domain, and allows for realistic evolution of mass and momentum near the terminus. We note that this prescribed flux convergence differs from implementation of flow convergence in earlier work with flowline models (e.g. Gladstone et al. (2012), Cook et al. (2013)), where the additional mass is added as an input to the surface mass balance. Although the latter will result in correct flux, it neglects the direct effect of the additional flux on the velocity field and may consequently underestimate velocity change while overestimating elevation change.

### 3.4 Numerics for implementing calving

We implement the crevasse-penetration calving criterion (Benn et al., 2007a,b; Nick et al., 2010), based on the work of Nye (1957) and van der Veen (1998a,b). This model is based on the assumption that calving occurs when surface and basal crevasses meet. Surface and basal crevasse depths are calculated from the balance of forces:

\[
\sigma_n = 2\tau_e \text{sgn}(\tau_{xx}) - \rho_i gd + P_w
\]

where the result, \( \sigma_n \), is the ‘net stress’, which is positive in a crevasse field and negative in unfractured ice (van der Veen, 1998a). The first term on the right hand side of Equation 3 represents the opening force of longitudinal stretching, and is adapted from Otero et al. (2010); \( \tau_e \) represents effective stress, which is related to the second invariant of the deviatoric stress tensor and which, in 2D, is defined by (Cuffey and Paterson, 2010):

\[
\tau_e^2 = \tau_{xx}^2 + \tau_{zx}^2
\]

where \( x \) is the direction of ice flow, and \( z \) the vertical. We multiply \( \tau_e \) in Equation 3 by the sign function of longitudinal deviatoric stress (\( \tau_{xx} \)) to ensure crevasse opening is only predicted under longitudinal extension (\( \tau_{xx} > 0 \)).
The second term on the right hand side of Equation 3 represents *ice overburden pressure*, which leads to creep closure, where $\rho_i$ is the density of glacier ice, $g$ is the force of gravity and $d$ is depth through the ice.

The final term in Equation 3 is water pressure ($P_w$) which acts to open crevasses when present. In basal crevasses, $P_w$ is controlled by the subglacial hydrological system, and in surface crevasses, it is related to the depth of water in the crevasse.

Crevasses will exist wherever $\sigma_n$ is positive, and ice remains intact elsewhere. Evaluating Equation 3 for both surface and basal crevasses at every node in our model allows us to define ‘zero contours’ which represent the base and top of surface and basal crevasse fields, respectively. The modified crevasse-penetration calving criterion (Nick et al., 2010) predicts that calving will occur where and when these zero contours meet. By calculating the crevasse depth criterion as an index at every node, and interpolating the nodal values to find the zero contours (Fig. 3), we arrive at a calving implementation which accounts for changes in stress between surface and interior and which is *independent of reasonably insensitive to* the model’s mesh resolution.

The magnitudes of the force components of Equation 3 vary greatly between the surface and bed. Specifically, the *rate of viscous creep closure cryostatic pressure* will be much higher at the bed. However, when the terminus is near flotation, high basal water pressure will almost completely counteract this closing force. High basal water pressure is, thus, an essential condition for significant basal crevasse penetration (van der Veen, 1998a). Because our study focuses specifically on calving dynamics, we make the simplifying assumption that an efficient subglacial drainage system exists near the terminus and, thus, that there is negligible difference in basal water pressure *for any given depth* within the region where calving may occur. With this assumption, basal water pressure is simply a function of sea level and bed elevation (van der Veen, 1998a):

$$P_w = -\rho_w g z$$  \hspace{1cm} (5)

where $z$ is the z-coordinate which is negative below sea level.

Water pressure is essential for basal crevasse penetration, but it may also be significant in surface crevasses (Benn et al., 2007b). The process of ‘hydrofracturing’ by water in surface
crevasses is believed to have been a critical factor in the collapse of the Larsen B Ice Shelf (Scambos et al., 2003). However, while water in surface crevasses may be important, it is extremely difficult to quantify. The relationship between surface melt rate and crevasse water depth depends on the distribution, shape and depth of crevasses, melting and refreezing on crevasse walls, as well as potential drainage of water from crevasses into englacial, subglacial or proglacial water bodies. As such, it is currently impossible to estimate even an order of magnitude for crevasse water depth at Store Gletscher in summer. However, outside the 3 month summer melt season, surface crevasses must be assumed to be dry.

Modelling calving in a 2D continuum model involves some implicit assumptions which may affect the accuracy of the calving criterion presented above. Firstly, the implementation of valley sidewall friction assumes that the calving terminus runs straight from one side of the valley to the other. However, Store’s terminus is usually arcuate in shape, with the centreline being further advanced in the fjord than the sidewalls. Thus, our implementation will overestimate lateral drag at the terminus. Secondly, by assuming a constant temperature of -10°C throughout the glacier, we neglect temperature dependent variations in viscosity and, thus, the stress field. Finally, Equation 3 slightly overestimates ice overburden pressure by assuming constant bulk density within the glacier. In fact, the presence of a crevasse field significantly reduces bulk density; this represents a positive feedback whereby the growth of a crevasse field reduces ice overburden pressure, leading to further crevasse deepening.

For the reasons outlined above, we expect our model to slightly underestimate the penetration of surface and basal crevasses near the present terminus position. As such, we apply a constant scaling factor of 1.075 to the effective stress term in Equation 3. This scaling procedure is equivalent to the assumed presence of water in crevasses throughout the year in earlier work (Nick et al., 2010; Vieli and Nick, 2011). We note, in this context, that for a typical value of effective stress ($\tau_e = 300$ kPa), our 7.5% scaling factor equates to just 2.3 m water depth added to crevasses. As there are several factors, aside from water depth, which may explain why the calving criterion does not predict full crevasse penetration exactly at the observed terminus location, we consider the scaling factor to simply be a tunable parameter, encompassing the
above processes, and which we keep constant. A more robust treatment of the issues outlined above will most likely require a 3D model for calving.

3.5 Model Forcing

We investigate the calving dynamics of Store in three stages. First, we set up a baseline run in which flow is affected only by a seasonal variation in basal traction. We then explore the glacier’s response to 1) undercutting of ice front by submarine melting in summer, and 2) buttressing of the ice front by rigid mélange in winter. The aim of these numerical experiments (henceforth referred to as experiment 1) is to identify which forcing has the greatest influence on the glacier’s flow, and the outcome represents a ‘present day’ simulation in which the glacier’s frontal position varies seasonally as observed under current climatic conditions. Finally, we perform perturbation experiments by altering mélange and submarine melt forcing in terms of their magnitude and duration. This set of experiments (experiment 2) investigates the response of Store to changes at its calving ice front in a warming climate.

3.5.1 Submarine melting

Time-lapse photography show a meltwater plume at the central section of the terminus of Store in summer months (Chauché et al., 2013)(Chauché et al., 2014). Because the location of this plume corresponds with the terminus position in our model, we apply summer melt rates at the calving front which vary linearly from 8 m d$^{-1}$ at the base to 0 m d$^{-1}$ at sea level. This melt distribution is a simplification of the one found by Xu et al. (2013), who used the MITgcm to investigate plume-induced ice front melting at Store, based on previous estimates of fjord water temperature (Rignot et al., 2010) and subglacial meltwater discharge (van Angelen et al., 2012). Their results suggest an average melt rate across the entire face of 3.6 m d$^{-1}$ in summer, with a local maximum at the base of the plume of 8 m d$^{-1}$. Because subglacial discharge is strongly influenced by surface runoff in summer months, we assume, for the sake of simplicity, that no submarine melting occurs in winter. If and when the floating tongue exists during the melt
season, we apply a bottom melt rate of 1/10th of that applied on the vertical face, based on the ‘geometrical scale factor’ proposed by Jenkins (2011).

In experiment 1, ice front melting is assumed to occur at a constant rate between June and August, both months included, as $>90\%$ of all surface runoff in the Store catchment occurs over this period. In experiment 2, we investigate the effects of increasing summer melt rates by a factor of 1.5 and 2, and increasing its duration by 1 and 2 months, respectively.

3.5.2 Mélange backstress

We simulate the effect of mélange backstress by applying an external pressure on the calving terminus in addition to that exerted by the sea (Fig. 4). The applied pressure is similar to that found by Walter et al. (2012) from a force-balance study of Store, based on the observed speedup of the glacier following mélange collapse. Their result shows that the mélange yields a supporting pressure equivalent to a backstress of 30-60 kPa acting on the entire face of the terminus. In reality, this stress is applied only through the thickness of the mélange, a property not measured by Walter et al. (2012). To obtain a realistic forcing scenario at the calving front of our model, we convert Walter et al.’s backstress ($\sigma_{fb}$) into an equivalent mélange-glacier contact pressure,: 

$$\sigma_{sik} = \sigma_{fb} \frac{H_{term}}{H_{sik}}$$  \hspace{1cm} (6)

where $H_{term}$ and $H_{sik}$ are the thicknesses of the glacier terminus and the mélange respectively.

In the baseline experiment, we take the midpoint of the range estimated by Walter et al. (45kPa), acting over a mélange thickness of 75 m, as estimated from laser altimeter data collected by NASA’s Operation IceBridge (https://espo.nasa.gov/missions/oib/). Based on the work of Howat et al. (2010), we assume mélange to be present and rigid from February to May, both months included, and absent from June to January. In experiment 2, we investigate the effect of reducing mélange strength by 25% and 50%, and its duration by 33% and 66%.
4 Results

4.1 Baseline run

The baseline configuration of our model includes only one seasonal effect: the prescribed sinusoidal variation in the basal friction parameter between winter and summer values. The result is a slight increase in flow speed at the terminus, from a minimum of 4,700 m a$^{-1}$ in winter to a maximum of 4,900 m a$^{-1}$ in summer (Fig. 5b). When the calving criterion is implemented, calving activity is periodic and characterised by 80-90 m bergs breaking off with a frequency of one per 8.7 days (Fig. 5a). Terminus velocity increases when calving occurs and is reduced afterwards as the front advances. The amplitude of these velocity fluctuations is about 200 m a$^{-1}$, (Fig. 5b), a similar magnitude to the seasonal effect of varying basal friction, indicating that the position of the calving front has a strong influence on terminus velocity. However, the terminus position varies less than 100 m through the entire simulation and there is no discernible seasonality of the glacier’s frontal position. This shows that the observed seasonal advance and retreat of the calving front cannot be attributed to seasonal variation in basal friction.

4.2 Experiment 1

To attain a realistic ‘present day’ simulation, we start by adding submarine melting, as described above, with rates up to 8 m d$^{-1}$ from June to August. This forcing slightly increases the frequency and reduces the magnitude of calving events, though the overall terminus position varies only negligibly (Fig. 5a). Terminus velocity during the melt season is slightly suppressed compared with the melt-free simulation (Fig. 5b). This experiment suggests that neither seasonal variability in basal dynamics nor submarine melting explain the seasonal calving dynamics observed at Store. Only when the stabilizing effect of mélange buttressing is included does our model respond by significant frontal advance and retreat. Figure 6 shows the evolution of calving terminus position through time for each of the two seasonal forcings as well as the combined effect.
In our model, the formation of the mélange triggers the immediate formation of a floating ice tongue, which advances into the fjord. The terminus advances by 1,300 m between February and May, while the mélange is present, and begins to retreat rapidly when the mélange disappears, irrespective of whether or not submarine melting is applied (Fig. 6). Figure 7 shows the evolution of the floating tongue through the mélange season. As the floating tongue advances, both the surface and basal crevasse fields are suppressed near the terminus. Note that the surface elevation rises as the floating tongue extends into the fjord, indicating that the dynamic regime near the grounding line leads to super-buoyancy which is forcing the terminus below flotation level. This is only overcome once the floating tongue is long enough to exert sufficient upward bending moment on the grounding line. Once significant upward bending is exerted, this is manifested as a suppression of surface crevasse field, clearly visible in Figure 7.

When the mélange effect is combined with submarine melting, the collapse of the floating tongue is followed by further 250 m retreat beyond the stable terminus position at 113km. After this retreat, the terminus slowly readvances through the melt season to 113km, where it remains, calving periodically, until the mélange forms during the following winter.

Our simulations in this experiment demonstrate a strong correlation between terminus position and velocity. Seasonal dynamics imposed by changing basal friction (Fig. 5) are dwarfed by the deceleration which occurs when the floating ice tongue develops and advances (Fig. 6). The dynamic effect of this slowdown is transmitted up to 30km inland (Fig. 8a). During the mélange season, surface velocity is reduced and thickness increases slightly (Fig. 8b) between 90km and the terminus. Following mélange collapse, velocity immediately rebounds to values similar to those prior to the mélange formation, and this speedup is followed by a gradual deceleration through the rest of the year. Interestingly, surface velocity around 85 km is consistently faster than January 1st throughout the seasonal cycle, peaking at 7.5% faster halfway through the year. Figure 8b also indicates slight thickening upstream and thinning downstream of this location, which coincides with a significant basal pinning point and large surface slopes as the glacier flows into a deep basal trough (Fig. 2).
The outcome of experiment 1 is a seasonally variable calving model of Store which is in overall good agreement with observations (Howat et al., 2010; Walter et al., 2012). The stable position adopted by the modelled terminus (113 km) following the summer melt season matches the observed summer terminus position. As observed, the modelled terminus retreats rapidly soon after mélange has collapsed in the fjord. The total seasonal variability in modelled front position (1.3 km) is in good agreement with the range that observed by Howat et al. (2010), as well as time-lapse imagery collected by the Extreme Ice Survey (www.eis.com), which show that the frontal position of Store can vary by more than ~1 km between summer and winter (J. Box Personal Communication).

**4.3 Experiment 2**

In this experiment, we perturb the stable ‘present day’ simulation obtained in experiment 1 in order to investigate the response of Store to climate change. We specifically investigate the glacier’s response to changes in mélange buttressing and submarine melting because these forcing factors are poorly understood.

When mélange strength is reduced from 45 kPa to 33.75 kPa to 75% of its baseline value (Fig. 9a-c, green lines), the floating tongue does not begin to form until halfway through the mélange season. As a result, the maximum length of the tongue is reduced from 1.3 to 0.7 km (Fig. 9a). When mélange strength is further reduced to 22.5 kPa (50% Fig. 9a-c, red lines), no floating tongue forms in spring, though there remains a clear change in calving dynamics throughout the mélange season. These results suggest that any future climate related reduction in the strength of mélange may significantly affect the calving dynamics and seasonality of Store.

Reducing the length-duration of the mélange season from 0.32 to 0.21 years to 66% (Fig. 9b) limits the length of the floating tongue to 0.8 km for the 45 kPa case (Fig. 9a). However, further reduction to 0.11 years has no reduction to 33% (Fig. 9c) has no further effect on calving dynamics, and the floating tongue continues to advance for a month following mélange breakup. This is a surprising result, which suggests that the floating tongue is at least temporarily self-stabilising. In the 33.75 kPa 75% mélange strength case, when season length is reduced from 0.32 to 0.21 duration is reduced to 66% (Fig. 9b, green line), the floating tongue begins to ad-
vance slightly sooner and so the final length is slightly higher. However, in the 0.11-year, 33.75 kPa case, no floating tongue forms when season duration is further reduced to 33% (Fig. 9c, green line).

An increase in the duration of submarine melting, from 0.25 years to 0.33 and 0.41 years respectively by 33% and 66% (Fig. 9e and 9bf, respectively), leads to more rapid collapse of the floating tongue, though in no case does the tongue collapse while rigid mélange is still present. As in experiment 1 (Fig. 6), submarine melting has an appreciable effect on the calving dynamics of the grounded terminus in late summer. As such, a longer submarine melt season leads to a longer period of larger, less frequent calving events and a retreat in average terminus position (Fig. 9b). The response of the modelled terminus to increasing melt magnitude, on the other hand, appears somewhat stochastic. In some cases, the average terminus position during the melt season is further inland, but in other cases the reverse is true. It should be noted, however, that the positions shown in Figures 5, 6 and 9 represent the terminus at the surface, which is able to advance into the fjord when undercutting takes place, due to the fact that the glacier’s topography exerts a control on the position of the grounding line. Broadly speaking, however, the calving dynamics appear to be, according to this model, relatively unaffected by increasing melt magnitude. In even the most severe ‘warming climate’ scenario, with melt rate double present-day values and duration increased from 3 to 5 months, the modelled terminus remains stable.

5 Discussion

The results of our modelling experiments shed new light on marine terminating glacier dynamics and the calving mechanism. The calving dynamics of the modelled glacier vary significantly through the year (experiment 1, Fig. 6), from high frequency (8.7 days), low magnitude (~80 m) calving events when no seasonal forcing is applied, to complete cessation of calving during the mélange season, with rapid retreat following mélange collapse, and seemingly stochastic calving behaviour during the melt season. This behaviour is in good overall agreement with year-round observation of Store (N. Chauché, Personal Communication). Our model captures
two important aspects of Store’s behaviour. Seasonally, Store’s terminus position is highly sensitive to external perturbation. However, on interannual timescales, Store’s calving dynamics are stable, and the terminus position remains fairly constant (Howat et al., 2010).

In our model, the seasonal advance and retreat is specifically related to a floating tongue, which forms during winter in response to the buttressing effect of rigid mélange (Fig. 5b, Figs. 6, 7) and breaks apart once the buttressing effect of the mélange disappears. This finding provides theoretical understanding for the observed temporal correlation between mélange break up and frontal retreat at Store and other glaciers in the Uummannaq region (Howat et al., 2010), as well as Jakobshavn Isbræ (Amundson et al., 2010) farther south, and glaciers such as Kangerdlugssuaq and Daugaard-Jensen on the east coast (Seale et al., 2011). Our results from experiment 2 suggest that the estimate of Walter et al. (2012) of a mélange strength of 30-60 kPa is most likely correct, and that any future climate driven reduction in mélange strength or thickness could significantly impact the seasonal dynamics of Store (Fig. 9).

When we isolated the effect of submarine melting of the ice front (experiment 1, Fig. 5), we found a slight increase in calving frequency, an associated decrease in calving event size, and a slight dampening of the glacier’s velocity response to calving events. However, the overall effect of submarine melting alone was minimal. Only when combined with mélange forcing was submarine melting capable of significantly affecting calving dynamics (Fig. 6). This suggests that some process during the mélange season preconditions the glacier for slight instability later in the season. Potentially, the upward bending associated with the formation of the floating tongue (Fig. 7) changes the glacier geometry near the grounding line such that it is more susceptible to the effect of undercutting by submarine melting.

Despite doubling melt rates and increasing melt duration by 66% in experiment 2 (Fig. 9), the terminus of Store remained stable at 113 km, suggesting that there is no direct link between submarine undercutting and longer-term calving stability of the grounded terminus at present. This result contradicts previous work suggesting that undercutting of the terminus promotes calving (Motyka et al., 2003; Rignot et al., 2010) by intensifying extensional stresses near the terminus (O’Leary and Christoffersen, 2013). We propose, however, that this apparent contradiction is a feature specific to Store, due to the strong stabilising influence of topography.
The location of the terminus of Store coincides with a significant basal pinning point (Fig. 2), as well as a ‘bottleneck’ in the fjord width (Fig. 1). The combined effect of these topographical features is to significantly affect the stress field and crevasse depth (Fig. 4). The suppression of crevasses penetration depth at the stoss side of the basal pinning point at the terminus exceeds the deepening of crevasses in response to undercutting of the ice front by submarine melting. As such, the latter alone cannot cause the front to retreat in this case. This suggests that so as long as the melt rate is less than the rate of ice delivery to the front, the terminus position of Store will be relatively insensitive to the rate of ice front melting. Thus, the rate of iceberg production will be solely controlled by the velocity at the terminus. The topographic setting of Store explains why this glacier remained stable during a period when others in the same region experienced rapid retreats (Howat et al., 2010) and, more generally, why neighbouring glaciers are often observed to respond asynchronously to similar climate forcing (Moon et al., 2012).

Inland of Store’s stable frontal pinning point is a 28 km long overdeepening reaching 950 m below sea level (Fig. 2), which could make Store susceptible to sudden retreat, i.e. if the terminus becomes ungrounded from its current pinning point at 113 km. We found that, by forcing the model with unphysically large values for submarine melt rate (not shown), we were able to force the terminus back off its pinning point, which led to rapid retreat through this trough. However, none of our climate forcing scenarios were able to trigger such a retreat which suggests that the current configuration of Store is stable and will most likely remain so in the near future.

As laid out above, our model is capable of reproducing the flow and seasonal calving dynamics of Store simply by perturbing the backstress exerted by mélange and the rate of submarine melting. Our model excludes the effect of water in surface crevasses, which may conceivably affect calving due to hydrofracture if water levels are high (Benn et al., 2007a). Although recent work included this effect (Nick et al., 2010), we ignore it because high resolution images captured in repeat surveys of Store with an unmanned aerial vehicle in July 2013 detected water in only a small number of surface crevasses near the terminus (Ryan et al., 2014). Although we cannot exclude the possibility that undetected water is contributing to crevasse penetration, it is not necessary to invoke this process to explain the observed behaviour of Store. This exclusion
of hydrofracturing is a useful model simplification, as it is difficult and potentially impossible to accurately estimate the depth of water in crevasses. The latter would require knowledge of surface meltwater production as well as the number and size of surface crevasses, which is infeasible with the type of model used here.

Although our model captures the flow and seasonal calving dynamics of Store in a realistic manner, it is important to note that the outcome of our study is specifically limited to this glacier and that multiyear dynamics remains to be fully investigated. We use inverse methods to determine basal traction, rather than a hydrological model; this ensures that the flow field matches observations, allowing us to focus on processes at the terminus. However, prescribing basal traction means we are unable to investigate its interannual evolution in response to dynamic thinning, rising sea level or hydrological processes. The difficulty of implementing realistic hydrological routing in a flowline model suggests that only a 3D model will be fully capable of representing these processes.

It is useful, at this point, to compare the development of time-evolving models for calving with recent developments in the implementation of grounding line dynamics. The lack of consistency of grounding line treatment in ice flow models was raised by Vieli and Payne (2005), and this issue has since received a great deal of attention from the ice-sheet modelling community. A comprehensive intercomparison study, MISMIP (Pattyn et al., 2012), compared the ability of various 2D ice flow models to simulate grounding line dynamics, before MISMIP3d (Pattyn et al., 2013), did the same for 3D models. Similarly, we hope that the 2D model presented here will guide the future development of full 3D time-evolving models for calving.

Finally, we note that in terms of accounting for the feedback between crevasse formation and bulk density and flow characteristics, a damage mechanics approach may prove useful (Pralong and Funk, 2005; Borstad et al., 2012). A counterpart study to this one by Krug et al. (2014) attempts to couple a damage model with a calving model for a synthetic glacier geometry Helheim Glacier using Elmer/Ice.
6 Conclusions

Here we have presented results from a seasonally transient but interannually stable calving model of Store Gletscher in West Greenland. The calving numerics in our model differ from previous implementations of the crevasse depth criterion (Nick et al., 2010; Vieli and Nick, 2011; Cook et al., 2013) in that the balance of crevasse opening and closing forces is calculated through the entire thickness, not just at the boundaries, meaning that changes through depth are taken into account. In agreement with recent related work (Nick et al., 2010), we find that the inclusion of basal crevasses in the calving criterion is important. We propose the addition of a new divergence term to the Stokes equations, which is not only practical, but most likely essential for accurate simulation of glaciers in 2D flowline models. We also find that the frequently assumed presence of water in surface crevasses is not necessary for seasonal calving dynamics at Store.

We find that basal traction varies very little between winter and summer; basal lubrication by surface meltwater is therefore unlikely to play an important role in the seasonal advance and retreat of the ice front. This does not imply, however, that calving and flow dynamics are not strongly coupled. Our results indicate a strong correlation between terminus position and velocity (Figs. 5, 6). The deceleration which results from advance of the floating tongue is transmitted up to 30km inland (Fig. 8). This finding supports previous studies which found that dynamic change at Helheim Glacier (Nick et al., 2009) and Jakobshavn Isbræ (Joughin et al., 2012) were triggered at the terminus.

A key outcome from this study is that the buttressing pressure from rigid melange is principally responsible for observed seasonal advance and retreat. However, sensitivity analysis revealed that, in a warming climate, reduction in melange strength or duration could prevent Store from advancing a floating tongue in winter. The model also indicates that submarine melting has only a limited effect on calving dynamics and that even large changes to melt rates in the future are unlikely to destabilize the terminus of Store. We propose that Store’s highly stable terminus configuration is due to its topographic setting, being located at both a basal pinning point and a ‘bottleneck’ in fjord width. We also find, however, that behind this basal pinning...
point, Store flows across a very large trough, reaching 950 m below sea level and extending 28 km inland from the current grounding line. This suggests that, were the terminus to be forced to retreat from its current pinning point, further retreat may be rapid and sudden, of a similar magnitude to that experienced by Jakobshavn Isbrae which resulted in a sustained increase of ice flux and contribution to sea level rise (Joughin et al., 2012).

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Fig. 1. Store Gletscher in Ikerasak Fjord, Greenland. Colour scale shows summer velocity (m a\(^{-1}\)) from the MEaSUREs program (Joughin et al., 2011). Yellow line indicates the flowline used in this study, and the green star indicates the location of the main proglacial plume forming where subglacial water is discharged into the fjord.
Fig. 2. a) Surface and basal geometry of central flowline used in this study. b) Model mesh of region outlined by green box in (a). Blue line represents sea level.
Fig. 3. The terminus of the flowline mesh of Store Gletscher. White line indicates the net stress ($\sigma_n$) zero contour for both surface and basal crevasses. Blue line indicates sea level. Net stress (MPa) is $>0$ where crevasses exists and $<0$ in solid and unfractured ice. Calving occurs in the model when the surface and basal crevasses-zero contours meet. Blue line indicates sea level.
Fig. 4. **Proximal**—**Schematic diagram showing proximal** and distal processes affecting calving. **a)** Varying basal friction ($\tau_b$) affects the stress field in the glacier. **b)** Changing fjord water temperatures and, more importantly, subglacial water flux affect the rate of submarine melting of the calving face and floating tongue (when present). **c)** The seasonal formation of mélange provides a buttressing force which suppresses surface crevasse depth and, thus, calving. **d)** Surface melt water in crevasses causes hydrofracturing, which acts to deepen surface crevasses. **e)** Glacier geometry exerts a strong influence on crevasse field depth. **Compressional**: compressional forces on the stoss side of Store’s pinning point suppress the depth of crevasses, while rapid loss of basal traction in the lee side deepen them.
**Fig. 5.** Plots showing variations in terminus position (a) and velocity (b), over the course of a year for baseline model run (blue line) and run with submarine melting applied (red line). Red shading indicates melt season. The saw-toothed pattern in both panels is a result of calving.
Fig. 6. Plots showing changes in calving terminus position (a) and velocity (b) during a five-three year period within a 40 year long stable simulation, with coloured solid lines illustrating the effect of four different combinations of melting and ice mélange perturbation. Blue and red shade indicates mélange and melt season respectively.
Fig. 7. Sequential profiles of Store Gletscher during advance of its calving terminus due to mélange backstress. As the floating tongue advances from the grounding line (marked GL), it rises upwards due to buoyant forces, which also act to close surface crevasses near the grounding line. This indicates that flow dynamics at the grounding line are forcing the terminus \textit{below} flotation.
**Fig. 8.** Plots showing velocity (a) and thickness (b) perturbations through a single calendar year. Line colour indicates time of year. Velocity and thickness have been normalised against their Jan 1st values.
Fig. 9. Plots showing terminus position through one year for varying mélange season length-duration (aa-c) and melt season length-duration (bd-f). Durations of mélange and melt season are indicated by blue and red shading (and panel title), respectively, varying from left to right, with. Line colour indicating the magnitude indicates varying magnitude of the perturbation melt rate and mélange backstress. Moving from left to right: The blue line in panels (a) and moving (d) represent the baseline model from blue, through green, to red (experiment 1 (Fig. 6). Changing panels and line colours indicate perturbations under progressively more severe ‘warming warmer’ climate scenarios.