Dear Dr. Radic,

We would like to thank the two reviewers for their reviews, which helped improving the manuscript. The major issue of both referees was to clarify and broaden the sections about the sensitivity analysis and the radiative forcing. We have done so and have added a table with the parameter ranges used in the sensitivity analysis as suggested by anonymous referee #1. Furthermore, we have adjusted the title of our manuscript as proposed by the two reviewers. Anonymous referee #1 pointed out that the used mass absorption coefficient of black carbon is not in accordance with the applied albedo parameterisation. In response, we have changed the value of the mass absorption coefficient and have updated all results accordingly. Anonymous referee #2 proposed to refer to the study of Painter et al. (2013), who suggested that black carbon forced the end of the Little Ice Age, in order to expand the relevance of this paper. We have added an additional section to the discussion-part of the paper where we discuss in detail the findings of Painter et al. (2013) and compare them with our results.

In the following we address the referee comments point by point. The comments of the referees are listed according to the review letter (italic). For each comment, an explanation of the changes applied is given (normal type style). The revised version of the text is given in smaller script size and quotation marks.

We are confident that the changes have resulted in an improved manuscript.

Kind regards,
Jeannette Gabbi and the co-authors

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**Comments of Anonymous Referee #1**

*General comment 1*

More detail should be included on the sensitivity studies described in Section 5. It was not clear exactly how each of the parameter changes should influence the simulated mass balance, and interpretation of this part of the study could be improved with more discussion on these parameter changes. It would be helpful to include a table listing the ranges of parameter values that were applied in the sensitivity studies.

We agree with the reviewers concern and have extended and specified the section about the sensitivity analysis to provide more clarity. More detailed information on the effect of the individual parameters on the mass balance is included in the revised version of the manuscript. Furthermore, the interpretation of this part is broadened. As suggested we added a table showing the parameter ranges used in the sensitivity analysis.

*Pages 16/17, Section 5.2 & Page 27, Table 1*

In order to assess the sensitivity of the model results to the chosen input parameters, we performed a sensitivity analysis. Four parameters of the snow impurity model were examined: (1) removal rates of BC by melt water, (2) fraction of Fe which is presented as Fe-oxides, (3) the proportion of haematite and goethite in the Fe-oxides, and (4) the ratio of the MAC of BC vs. MAC of Fe-oxides. In addition, another four parameters of the SSA model (SSA_{initial}, SSA_{min}, C_1, C_2) and six parameters of the snow density model (\(a_t\), \(c_1\), \(k_0\), \(k_1\), \(F_C\), \(c\), \(d\)) were investigated. Furthermore, we also assessed implications of deviating atmospheric deposition rates of mineral dust and BC on the mass balance as the ice core data is taken from another site (see Section 5.4). The parameters of the melt and accumulation model were not included in the sensitivity analysis.
Table 1: Parameters of the impurity, the SSA and the snow density model and the corresponding parameter ranges (±20%) applied in the sensitivity analysis.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Value Range</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Impurity model</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dust input</td>
<td>µg kg⁻¹</td>
<td>22.3 - 17.8 - 26.8</td>
</tr>
<tr>
<td>BC input</td>
<td>µg kg⁻¹</td>
<td>23.2 - 18.6 - 27.8</td>
</tr>
<tr>
<td>BC removal rate</td>
<td>%</td>
<td>20 - 16 - 24</td>
</tr>
<tr>
<td>Fe in FeO</td>
<td>%</td>
<td>54.5 - 43.6 - 65.4</td>
</tr>
<tr>
<td>MAC FeO/BC</td>
<td>-</td>
<td>0.082 - 0.066 - 0.099</td>
</tr>
<tr>
<td><strong>SSA model</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SSA_initial</td>
<td>m² kg⁻¹</td>
<td>73.0 - 58.4 - 87.6</td>
</tr>
<tr>
<td>SSA_min</td>
<td>m² kg⁻¹</td>
<td>8.0 - 6.4 - 9.6</td>
</tr>
<tr>
<td>C₁</td>
<td>10⁻³ mm³ d⁻³</td>
<td>1.1 - 0.88 - 1.32</td>
</tr>
<tr>
<td>C₂</td>
<td>10⁻⁵ mm³ d⁻³</td>
<td>3.7 - 2.96 - 4.44</td>
</tr>
<tr>
<td><strong>Snow density model</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>a₁</td>
<td>°C mm⁻¹</td>
<td>0.033 - 0.0264 - 0.0396</td>
</tr>
<tr>
<td>c₁</td>
<td>C² h⁻² kg⁻¹</td>
<td>0.001 - 0.0008 - 0.0012</td>
</tr>
<tr>
<td>k₀</td>
<td>m³ kg⁻¹</td>
<td>0.021 - 0.0108 - 0.0252</td>
</tr>
<tr>
<td>k₁</td>
<td>°C⁻¹</td>
<td>0.08 - 0.064 - 0.096</td>
</tr>
<tr>
<td>Fc</td>
<td>-</td>
<td>0.02 - 0.016 - 0.096</td>
</tr>
<tr>
<td>c</td>
<td>m⁻¹ h⁻¹ (d⁻¹)</td>
<td>1.0 - 0.8 - 1.2</td>
</tr>
<tr>
<td>d</td>
<td>-</td>
<td>1.25 - 1.0 - 1.5</td>
</tr>
</tbody>
</table>

because they were directly constrained by the continuous seasonal mass balance measurements at the study sites. The sensitivity of the parameters was assigned by varying each parameter by 5% intervals around to the chosen value in a range of ±20%, keeping all other parameters constant. Tab. 1 shows the used parameter ranges.

According to Anslow et al. (2008) we defined the sensitivity of a parameter as the slope around the origin of the curve defined by the percentage change in the parameter value and the percentage change in the resulting model variable (mass balance in our case). For example a sensitivity of 0.5 designates that an arbitrary percentage change in the parameter value involves a half as large percentage change in the mass balance. A positive sensitivity means that an increase in the parameter value leads to an increase in the mass balance, a negative sensitivity that an increase in the parameter yields a decrease in mass balance.

Results of the sensitivity analysis are shown in Fig. 9. The mass balance was most sensitive to the amount of snow impurities and the parameters of the snow density model while the parameters of the SSA model were clearly less relevant. In contrast to the input quantity of BC, mineral dust had a less pronounced impact on modelled mass balance. A change of 10% in the BC concentration in precipitation led to a 5.8% change in mass balance, whereas the same change in the mineral dust concentration in precipitation only resulted in a 1.6% change in mass balance. The reason for this difference in sensitivity is the stronger absorption of solar radiation by BC compared to mineral dust. An even higher sensitivity could be assigned to the removal efficiency of BC with melt water. A 10% change in the BC removal rate leads to a 1.5 times larger change in the mass balance. This is particularly important since the removal rates are subject to considerable uncertainty (see Section 5.5).

Hence, the removal of BC by melt water seems to be the most critical point of the simulation and strongly controls the impact of BC on the long-term glacier mass balance. Besides the impurity model, also the performance of the density model affected the simulations. In particular, parameter k₀ (Eq. 11), describing the density change due to compaction, and the outflow parameter d (Eq. 10) were found to have sensitivities that are comparable to those of the input concentration of BC (Fig. 9). The higher the values of the density parameters, k₀ and d, the faster is snow compaction. More efficient compaction in turn entails higher impurity concentrations in the surface snow layer and thus enhanced melt rates. The parameters of the SSA model show the lowest sensitivity and therefore are less relevant for the results. The two parameters, SSA_min and SSA_initial (Eq. 5), are the most sensitive ones. An increase in the two parameter values leads to a depletion in pure snow albedo which slightly diminishes the impact on snow impurities. However, this effect is small compared to the other uncertainties."

Specific questions related to these studies are: In the runs with altered concentrations of BC and dust within precipitation, was the total aerosol deposition conserved and the ratio of wet to dry deposition altered, or was the total aerosol deposition altered? (The latter case would presumably produce disagreement with the ice core data).
Indeed, the total aerosol deposition was deliberately altered in order to show the effect of a potential over- or underestimation of dust/BC concentrations as the ice core data is not collected at the study site, but on another glacier in the Swiss Alps (see Section 5.4). The high spatial variability in atmospheric deposition rates of mineral dust and mainly BC makes it likely that dust/BC deposition on Claridenfirn probably slightly deviate from the ice core data. For this reason the amount of dust/BC was changed in the sensitivity analysis.

In our model we do not differentiate between dry and wet deposition as the contributions of dry deposition seems to be negligible (Schwikowski et al., 1995). This assumption is supported by the observation that Saharan dust containing layers in ice/firn cores generally have a thickness of several centimeters which indicates that Saharan dust was deposited during snow fall events. Furthermore, there is evidence that Saharan dust depositions in the Alps coincide with warm fronts causing precipitation (Schwikowski et al., 1995). For these reasons, we assume that all dust/BC is deposited by wet deposition. Hence, we do not consider the type of deposition in our sensitivity analysis.

We will include a table with the parameter ranges (see above) to clarify this issue. Furthermore, we reworded the corresponding sentence to make it clearer.

Page 16, Lines 505–508
"[...] Furthermore, we also assessed implications of deviating atmospheric deposition rates of mineral dust and BC on the mass balance as the ice core data is taken from another site (see Section 5.4).

Secondly, how does variability in the ratio of haematite to goethite impact the simulations? In section 3.1.1 it is mentioned that these minerals have different absorption characteristics, but it seems that a single absorption coefficient is applied to all iron oxides. Is it merely through differences in the molecular weight of the two minerals that different haematite/goethite ratios impact the simulations?

This is correct. The absorption coefficient was the same for both minerals, haematite and goethite, and only the molecular weight of the two minerals is responsible for the difference in the absorption. We do not consider different mass absorption coefficients for haematite and goethite because there are several other simplified assumptions in the calculation of the dust absorption involved (e.g. the constant ratio of haematite/goethite and a fixed amount of Fe encompassed in iron oxides) which introduce larger uncertainties.

General comment 2
One of the stated motivations for conducting this analysis at Claridenfirn is that there are 100 years of mass balance measurements at this location. It would therefore be helpful to include a comparison of the simulated and measured glacier mass balances, e.g., added to Figure 7. Was this excluded because the parameterization was heavily tuned to match the observations, and therefore the simulated and observed mass balances are essentially identical? If so, this should be stated more clearly. It is a bit unsettling that the parameters of the mass balance model were adjusted for each year of simulation (as indicated in section 3.5), though at least the ratio of weights applied to temperature and insolation was held constant throughout the simulation. Does the simulation that includes both black carbon and dust produce the best agreement with measured mass balance?
As suspected by the referee, the observed and simulated mass balance are essentially identical as we have used the seasonal mass balance measurements to calibrate the melt and accumulation parameters for each year in order to reconstruct the mass balance evolution as accurately as possible. We decided to calibrate the accumulation and melt parameters annually in order to receive the “true” sequence of melt and accumulation events and its effect on the dust and BC concentration in the surface snow. Thus, we make optimal use of the long-term direct measurements to constrain our model. We added some further explanation about this issue to make it clearer. With this modelling setup it is thus not possible to answer the question if simulations including mineral dust and BC agree better with observations than simulations without snow impurities.

Page 10, Lines 314–318
"[...] The melt parameters, TF and SRF, and the accumulation parameter, c_{prec}, were calibrated for each year individually by means of the seasonal balance measurements. This annual calibration ensures that simulated mass balances coincide with observations in order to extract an accurate sequence of melt and accumulation events controlling the surface concentrations of light-absorbing impurities."

General comment 3
The black carbon mass absorption coefficient assumed in this study (7.5 m²/g) is inconsistent with that assumed by Gardner and Sharp (2010) in their parameterization of albedo. They state that the maximum mass absorption coefficient of BC is 6.8 m²/g at a wavelength of 0.4μm. This is relevant for the determination of a BC-equivalent dust concentration, which is based on the ratio of mass absorption coefficients of BC and iron oxides. This determination should be made consistently with the assumed absorptivity of BC in the Gardner and Sharp (2010) albedo model. This issue may not have a large impact on the results, but should be fixed or at least addressed.

We thank the referee for the hint. We changed the value of the mass absorption coefficient to 6.8 m² g⁻¹ and updated the model results accordingly. As already mentioned by the referee the results are only marginally affected by this change.

Page 7, Lines 218–221
"[...] In order to model the effect of mineral dust on snow albedo, the mineral dust (i.e. Fe oxides) was converted to optically equivalent concentrations of light-absorbing carbon using mass absorption coefficients (MACs) of BC and Fe oxides of 6.8 m² g⁻¹ and 0.56 m² g⁻¹, respectively (Alfaro et al., 2004; Kaspari et al., 2014)."

General comment 4
The methodological description for calculating radiative forcing needs more detail. This calculation appears to be based on melt production and is therefore different from other, commonly used (e.g., IPCC AR5) definitions of radiative forcing. If the radiative forcing is derived in terms of the amount of energy used to melt snow, it may underestimate the true radiative forcing, which also operates during the pre-melt season. Implications of such differences in methodology for comparisons with other studies should also be mentioned.

We calculated the radiative forcing based on the melt production as supposed by the referee. According to the referee’s suggestion we added more information about the calculation of the radiative forcing and included also comments about the differences to other studies.

Pages 14–16, Section 5.1
"Converting changes in annual mass balance caused by absorption of dust/BC into the energy consumed for melt allowed calculating the radiative forcing of snow impurities. The radiative forcing (RF, W m⁻²) was calculated based on the change in melt rate, ΔM (m/s), caused by the presence/absence of mineral dust and/or BC in snow:
RF = ΔQ_M = ΔM_L_f ρ_W (1)

where Q_M (W m⁻²) is the energy consumed by melt, L_f (333,700 J kg⁻¹) the latent heat of fusion and ρ_W (1'000 kg m⁻³) the density of water. Changes in melt rates are equal to changes in mass balances as presented in Section 4.2.2. For the measurement site in the accumulation area we found a mean radiative forcing over the 100 year period of +0.3 W m⁻² due to Saharan dust, whereas at the stake close to the equilibrium line the radiative forcing was +0.6 W m⁻². In contrast to Saharan dust, the radiative forcing of BC over 1914–2014 was about seven times larger, and was +2.0 and +3.3 W m⁻² on average for the two sites. In the summer months, July and August, when melting is strongest, the radiative forcing for BC reached values of 8.7–9.7 W m⁻² and for Saharan dust of 3.0–3.7 W m⁻² compared to pure snow at the upper stake, and 12.9–15.9 and 4.7–6.3 W m⁻² at the lower stake, respectively. At the daily scale, maximum modelled radiative forcing was 15–42 W m⁻² for Saharan dust and 43–66 W m⁻² for BC.

At a global scale, the mean radiative forcing from BC in snow is reported to be in the range of 0.02–0.08 W m⁻² (Bond et al., 2013; IPCC, 2013). During boreal spring, when the snow-albedo feedback is maximal, the radiative forcing of mineral dust and BC over Eurasia is higher and amounts to 1.2 and 2.7 W m⁻², respectively (Flanner et al., 2009). For snow-covered surfaces of the Tibetan Plateau the radiative forcing of BC reaches values of up to 5–25 W m⁻² in springtime (Flanner et al., 2007; Kopacz et al., 2011; Qian et al., 2011). Similar peak values are found for desert dust in the mountain snow cover of the Colorado River Basin (25–50 W m⁻², Painter et al., 2007; Skiles et al., 2012). In general, radiative forcing of BC found for Claridenfirn is at the lower end of the range of values obtained for Colorado or Tibetan Plateau. Regarding mineral dust, the effect is also clearly stronger on the Colorado Plateau than in the Alps. In terms of maximum daily radiative forcing, values obtained for Claridenfirn are of similar magnitude as for other regions. However, radiative forcing reported in other studies is not directly comparable to the results of this study as dust/BC sources and the temporal dynamics of melting are different. Furthermore, radiative forcing of some of the above-mentioned studies was calculated by directly accounting for the change in the energy fluxes, rather than using the change in melt rates due to light-absorbing impurities as in our approach. Hence, the radiative forcing reported here represents a lower limit as the radiative impact in the pre-melt season is not taken into account.

General comment 5
I suggest modifying the title to indicate that the study focuses on Swiss or Alpine glaciers, or even specifically to the Claridenfirn. The current title implies a general study of glacier impacts associated with BC and dust, but the analysis is really quite specific to the Swiss Alps.

We agree with the referee’s suggestion and have changed the title accordingly.

Page 1, Title
"The impact of Saharan dust and black carbon on albedo and long-term mass balance of an Alpine glacier."

Minor comments

Comment 1
Page 1134, Line 10: “employed to assess dust/BC-albedo feedback” - To many, “albedo feedback” implies feedback between the atmosphere and land surface, which is not assessed here. The meaning of “feedback” in this context should be clarified.

We have rephrased the corresponding sentence.

Page 1, Lines 7–9
"[...] A combined mass balance and snow/firm layer model was employed to assess the effects of melt and accumulation processes on the impurity concentration at the surface and thus on albedo and glacier mass balance."
Comment 2

Page 1134, Line 16: “dust-enriched layers” - Should this be “dust and BC-enriched layers”?

Right! We have replaced the term “dust-enriched layers” with “dust and BC-enriched layers” where required throughout the whole manuscript.

Page 1, Lines 14–17

“[...] The upper site has experienced mainly positive mass balances and impurity layers were continuously buried whereas at the lower site, surface albedo was more strongly influenced by re-exposure of dust and BC-enriched layers due to frequent years with negative mass balances.”

Comment 3

Page 1135, Line 26: “Since mid-20th century BC concentrations started to decrease and have stabilised over the last few decades (Bond et al., 2007)” - Although European emissions have declined during the past few decades, Figure 6 of Bond et al. (2007) indicates that global BC emissions have continued to rise. It wasn’t clear if this passage was meant to refer to global or European emissions.

We agree with the referee that this statement is confusing and have clarified the sentence.

Page 2, Lines 47–50

“[...] Along with the beginning of the industrialisation global BC emissions sharply increased and continued to rise into the 21th century. In the European region BC concentrations started to decrease since mid-20th century and have stabilised over the last few decades (Bond et al., 2007).”

Comment 4

Page 1136, Line 16: “we examined the dust/BC-melt feedback” - Again, please clearly define this feedback. Here, I believe it refers to enhanced melt induced by BC/dust, which in turn increases the surface layer concentration of BC/dust and thereby further increases melt.

We have rephrased this sentence according to the referee’s suggestion.

Page 3, Lines 63–68

“[...] Using a unique 100-year record of seasonal glacier mass balances, ice core records of past atmospheric deposition of Saharan dust/BC and a sophisticated modelling approach, we examined the contribution of light-absorbing impurities to glacier melt for (1) a site with accumulation conditions over the entire period, where dust is predominately buried by winter snow, and (2) a site at the glacier’s equilibrium line involving a re-exposure of buried dust and BC layers at the surface in years with negative mass balance.”

Comment 5

Page 1138, Line 17: “... an annual cycle of BC concentrations in the atmosphere” - This seems like a useful way of deriving seasonal variations in BC deposition from annually-resolved ice core data, but I wonder if the seasonal cycle of BC deposition could have been different 100 years ago, e.g., due to more generation of BC for winter heating purposes. It would be interesting to include a sensitivity study that varies the seasonal cycle of BC deposition. I would not consider this critical for the paper, though, so I leave it up to the authors.

The referee mentions an interesting point. In fact, BC emissions over populated regions are generally higher in winter than in summer (Herich and Huglin, 2013). However, variations in BC depositions at high altitude sites are not driven by the seasonal cycle of BC emissions in lower regions, but by changes in atmospheric stability (Baltensperger et al., 1991). Only in
summer polluted air masses from the lowlands are transported upwards by thermal convection. In winter, the high-altitude sites are above the mixing layer and are generally not reached by the polluted air masses (Baltensperger et al., 1991). This can also be observed for sulfate, an anthropogenic pollutant, which is also mainly emitted in winter and is transported primarily in summer by thermal convection to high-altitude sites (Schwikowski et al., 1999). Accordingly, we suppose that the seasonal pattern of BC emission has not changed much over the last century. For this reason, we decided not to test the sensitivity of the annual BC cycle.

Comment 6
Page 1139, Line 11: “... the ratio of haematite to haematite plus goethite” - Is this the mass ratio of minerals, or the mass ratio of Fe within the minerals?

It corresponds to the mass ratio of minerals. We have added this information to the manuscript.

Page 5, Lines 138–140
"[...] According to Shi et al. (2011) the mass ratio of the mineral haematite to the minerals haematite plus goethite for Saharan dust is 0.42 on average."

Comment 7
Section 3.3: Does the albedo model provide diffuse or direct-beam albedo? If the latter, how was solar zenith angle incorporated into the model? Please include more detail on this.

The model, as applied in our study, provides direct-beam albedo. The albedo model of Gardner and Sharp (2010) offers the possibility to account for variations in the solar zenith angle. However, the effect of the solar zenith angle on the albedo is largest at high solar zenith angels i.e. in the early morning or evening and in winter when melt rates are low. Furthermore, the model runs on a daily basis. For this reason we do not account for the solar zenith angle on the albedo calculation. We now provide this information in the manuscript.

Page 7, Lines 222–223
"[...] The direct-beam albedo of the impurity-loaded snow is then obtained as \( \alpha = \alpha_{SSA} + d\alpha_{C} \). The effect of the solar zenith angle on the albedo is not considered as the model runs on daily basis."

Comment 8
Page 1143, Equation 6: Is Delta \( R_{opt} \) a rate (e.g., mm/day)? Please include units for this term.

The unit of Delta \( \Delta R_{opt} \) is indeed mm d\(^{-1}\). There is an error in the unit of the empirical coefficients \( C_1 \) and \( C_2 \). Instead of mm d\(^{-1}\) the unit should be mm\(^3\) d\(^{-1}\). We added the unit of \( \Delta R_{opt} \) and changed the units of the empirical coefficients accordingly.

Page 8, Lines 231–238, Equation 6
"[...] The approximation by Brun (1989) is used to simulate the evolution of snow grains under wet conditions with respect to the liquid water content of the snowpack. The growth of the optical radius of snow, \( \Delta R_{opt} \) (mm d\(^{-1}\)), is calculated as

\[
\Delta R_{opt} = \frac{C_1 + C_2 \cdot \theta^3}{R_{opt}^2 \cdot 4\pi},
\]

where \( C_1 = 1.1 \times 10^{-3} \text{ mm}^3 \text{ d}^{-1} \) and \( C_2 = 3.7 \times 10^{-5} \text{ mm}^3 \text{ d}^{-1} \) are empirical coefficients and \( \theta \) is the liquid water content in mass percentage. The SSA decrease is more pronounced when \( \theta \) increases."
Comment 9
Page 1144, Line 1: I think $C_1$ should be $10^{-3}$ rather than $10^3$.

This is correct. We have changed the unit accordingly.

Comment 10
Section 4.2: Please clarify whether the calculated albedo reductions are relative to pure snow, or relative to snow only without BC (in the case of dust estimates) or without dust (in the case of BC estimates)

We have added the missing explanation (see Section 4.2 in the revised manuscript).

Comment 11
Page 1152, Lines 6-9: Please clarify this sentence.

We have rephrased this sentence.

Page 13/14, Lines 421–429
"[...] However, changes in mass balance cannot be directly deduced from average dust concentrations because (1) the impurity concentration and albedo changes are not linearly related and thus a higher impurity concentration might lead to smaller changes in albedo, and (2) during years with high melt rates also other particulate impurities accumulate at the surface which limits the total impact of Saharan dust on surface mass balance. Thus, despite the exceptionally high surface concentration in 2007, the change in mass balance is only slightly larger than in years with lower surface concentrations as for example in the deposition intense year 2000 (Fig. 8a and c)."

Comment 12
Figure 6: If this shows an absorption optical depth, as indicated in the caption, over what thickness of snow/ice is it derived from? Optical depth is usually calculated over the entire column. The quantity shown in this figure needs to be defined more clearly.

The absorption/optical depth is calculated as the product of the mass absorption coefficient of dust/BC and the loading in the surface snow layer i.e. the mass of dust/BC in the top 2 cm. We added this information to the caption of Figure 6.

Page 31, Caption Fig. 6
"Figure 6 Mean annual absorption (optical depth) of mineral dust and BC over the period 1914 2014 for (a) the upper and (b) the lower stake. The optical depth is calculated as a product of the mass absorption coefficient of BC/Fe oxides and the corresponding loading in the snow surface layer (top 2 cm)."
Comments of Anonymous Referee #2

General comment 1
There are revisions that would improve this paper. 1) Given than the impurity concentrations, mass balance, and atmospheric forcing measurements did not come from the same location, and some highly simplifying assumptions were made, it is good a sensitivity study was carried out- but I found this section to be too brief, lacking in detail, and would benefit from expansion and clarity.

We agree on referee’s concern and have expanded and clarified the section about the sensitivity analysis for providing the reader with more detailed information. As this point was also raised by the other referee, see answer to general comment #1 of Anonymous Referee #1.

General comment 2
2) The location of the study should be added to title as the relative ratio of dust to black carbon estimated from the core measurements is specific to the Swiss Alps, and would not be the same for glaciers in say, the Himalaya, or the Andes.

The title was changed as suggested.

See answer to general comment #5 of Anonymous Referee #1.

General comment 3
3) I found it very interesting that the impact on mass balance attributed to BC deposition falls within the mass balance impact in the Alps by BC in the 1900s put forth by Painter et al., 2013, a paper which suggested that black carbon was the driver behind the retreat of glaciers in the Alps at the end of the Little Ice Age. The results presented here helps to validate the claims made by this earlier paper, and the relevance of this paper could be greatly expanded by tying back the results of this study (to those in Painter et al., 2013) in the conclusion.

According to the suggestion of the referee, we included a paragraph which links our results with the findings of Painter et al., 2013. We added this section to the Discussion-section in order to explain the differences/similarities between these two studies in more details.

"[...] Painter et al. (2013) suggested that the rapid retreat of Alpine glaciers at the end of the Little Ice Age was forced by increasing BC concentration due to industrialisation. They found BC-induced mass balance anomalies in the order of $-500 \text{ mm w.e. yr}^{-1}$ for the ablation area, which is similar to our results for the accumulation area ($-180$ to $-300 \text{ mm w.e. yr}^{-1}$) despite the different modelling approaches. While Painter et al., (2013) used a sophisticated radiation model (SNICAR, Flanner at al., 2007) to derive BC radiative forcing and in turn equivalent changes in air temperature and mass balance, we used a simple broadband albedo parameterisation in combination with a mass balance model. However, Painter et al. (2013) assume 10 to 20 times higher BC concentrations than reported by the ice core data in order account for altitudinal differences between the high-altitude ice core sites and the ablation area. In our study, we do not alter atmospheric deposition rates (see Section 5.4), but, contrary to Painter et al. (2013), account for changes in the BC surface concentration due to melt and accumulation processes as well as to removal by melt water. As a result, we obtain similar BC concentrations in the surface layer on average and thus, a comparable impact of BC on glacier mass balance. The general agreement of our assessment with that by Painter et al. (2013) indicates the highly relevant role of BC in shaping changes in glacier mass balance over the last century."
General comment 4
4) Don’t be afraid of commas! I found many long sentences in this manuscript that could be clarified with the use of a few commas.

We have checked the manuscript and have inserted commas where needed to make the text easier to understand.

General comment 5
5) Description of radiative forcing calculations needs to be broadened/clarified.

Done.

See answer to general comment #4 of Anonymous Referee #1.

Line by line comments

Comment 1
Page 1134, Line 4: Remove “Saharan” qualifier here, it unnecessarily specific for the abstract

Done.

Page 1, Lines 2–4
“[...] Here, we investigate the long-term effect of snow impurities, i.e. mineral dust and black carbon (BC), on albedo and glacier mass balance.”

Comment 2
Page 1134, Abstract: Consider including impact on mass balance.

According to the referee’s suggestion we have added the impact of dust/BC on the mass balance to the abstract.

Page 1, Lines 9–13
“[...] Compared to pure snow conditions, the presence of Saharan dust and BC lowered the mean annual albedo by 0.04–0.06 depending on the location on the glacier. Consequently, annual melt was increased by 15–19% and the mean annual mass balance was reduced by about 280–490 mm w.e.”

Comment 3
Page 1135, Line 6: Consider changing “involving” to “perturbing”.

We changed “involving” to “resulting in” to make it clearer.

Page 2, Lines 29–31
“[...] Snow impurities are mainly retained at the surface during conditions of melt and surface concentrations
might be enhanced by up to one order of magnitude resulting in a pronounced melt amplification (Sterle et al., 2013)."

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Comment 4
Page 1135, Line 13: Long-range transported crustal impurities accounts for 2/3 of the dust... where does the rest come from? Local landscape?

Yes. Around two thirds of the total are long-range transported crustal impurities and about one third has a local origin. We have added this information to provide more clarity.

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Page 2, Lines 34–37
"[...] Analyses of firn cores from high-alpine sites, resolving the signal of the continental background aerosols, indicated that long-range transported crustal impurities account for about two thirds and local impurities for about one third of the total mineral dust deposited (Wagenbach and Geis, 1989)."

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Comment 5

The suggested reference was added.

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Page 2, Lines 43–45
"[...] BC has become a focus of interest as it has been identified recently as one of the major contributors to global climate change (Ramanathan and Carmichael, 2008; Bond et al., 2013 )."

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Comment 6
Page 1136, Line 7: Consider including the region for the studies completed by Skiles and Painter (Colorado River Basin, Western US) as you do for the other cited studies.

We have added the study site for Skiles et al., 2012 and Painter et al., 2010.

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Page 2/3, Lines 56–58
"[...] Investigations in the Colorado River Basin, Western US, show that the radiative forcing of mineral dust deposition may shorten the duration of snow cover by several weeks (Skiles et al., 2012) and also affects the timing and magnitude of runoff (Painter et al., 2010)."

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Comment 7
Page 1136, Line 20: The sentence starting with “We have chosen...” should be restructured with commas, split into two sentence, or rewritten.

We have split this sentence.

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Page 3, Lines 68–71
"[...] We have chosen Claridenfirn (Swiss Alps) for which the worldwide longest data series of seasonal glacier mass balance exist. This comprehensive data set enables an accurate and field data-based simulation of ablation and accumulation processes."
Comment 8
Page 1137, Line 9: Were density measurements made in the snow pits or with a SWE sampler?

The density measurements were made in the snow pits. This information has been added.

Page 3, Lines 84–85
"[…] Simultaneously snow density measurements in snow pits have been carried out."

Comment 9
Page 1138 (study site and data): Please clarify how black carbon is estimated after 2002 and dust after 2007.

We have added this missing information.

Page 4, Lines 113–116
"[…] For BC and mineral dust concentrations of the years 2002-2014 and 2007-2014, respectively, which are not covered by the ice core data, a mean concentration averaged over the entire period was assigned (Fig. 2a)."

Comment 10
Section 3.1.1, Lines 5–15: Consider clarifying here that study done by Kaspari et al., 2014 was carried out in the Himalaya, not the Alps. Also, this study used gravimetric mass for their analysis, but found that there is linear relationship between Fe concentration and gravimetric mass (using a very small set of samples).

We have added the missing information to the corresponding paragraph.

Page 5, Lines 132–135
" […] The absorption of mineral dust in the visible spectrum is highly sensitive to the content of iron oxides. Kaspari et al. (2014) determined light-absorption of mineral dust in snow and ice of a Himalayan glacier based on gravimetrically determined Fe concentrations. Accordingly, we used records of iron (Fe), provided by the ice core, to infer mineral dust concentrations."

Comment 11
Section 3.4, Lines 19–20: Reword this sentence. You used wet deposition in the model, this is fine, I suppose, but you should use caution in stating this is the predominant mechanism! This is not well known or well established. Dust deposition events in particular are almost pre-frontal, when wind speeds are high enough to transport dust from the source region.

We have rephrased the corresponding sentence.

Page 10, Lines 293–294
" […] Mineral dust and BC entered the system by liquid or solid precipitation as wet deposition is expected to be the predominant mechanism (Raes et al., 2000; Koch, 2001)."

Comment 12
Section 4.1.3 Lines 1-5: Rewrite. Basically you are trying to say there was more dust, but black
carbon is more absorbing, but your wording is confusing.

We have reworded this paragraph for clarity.

Page 12, Lines 374–378
"[...] In contrast to BC, mineral dust concentrations at the surface were up to five times larger. However, as BC is much more absorptive than mineral dust (mass absorption coefficient about 10 times higher), the overall absorption by BC and dust are in a similar range."

Comment 13
Section 4.1.3, Line 9: “Absorbent” to “absorber”.

Done.

Page 12, Lines 380–381
"[...] In all other years, the absorption of BC outweighed the absorption of mineral dust and over the entire period BC was clearly the dominant absorber."

Comment 14
Section 4.1.3, Line 9: The influence of BC is already stronger than dust. Reword.

We have reworded this sentence.

Page 12, Lines 385–386
"[...] If removal rates of BC and mineral dust would be in a similar range, the influence of BC on the absorption would be even larger."

Comment 15
Page 1151, Lines 5–8: This sentence is circular and confusing – reword.

We have rephrased this sentence.

Page 13, Line 400–401
"[...] The overall impact of BC on the surface albedo was substantially higher than that of Saharan dust.”

Comment 16
Page 1153, Line 22: is the mountain snow cover of the Colorado River Basin, not the Colorado Plateau, which is a desert.

Changed.

Page 15, Lines 470–472
"[...] Similar peak values are found for desert dust in the mountain snow cover of the Colorado River Basin (25–50 W m$^{-2}$, Painter et al., 2007; Skiles et al., 2012)."
Comment 17
End of Section 5.1: I think it would be sufficient to say the results are not directly comparable because dust/BC sources and melt dynamics are different. (I think you have an extra word “often” on the last line of page 1153).

We agree and have rephrased this sentence.

Page 15, Lines 477–479
"[...] However, radiative forcing reported in other studies is not directly comparable to the results of this study as dust/BC source and the temporal dynamics of melting are different."

Comment 18
Section 5.2: Can you give an overall estimate of uncertainty?

As there are many poorly constrained variables involved in our assessment it is not possible to provide one single value for the uncertainty. Basically, the uncertainty in the selected parameter values is largely unknown and could only be narrowed down based on highly challenging field and laboratory experiments. However, our sensitivity analysis covers all individual factors determining the final uncertainty in our results and indicates processes for which additional research is required.
References


The impact of Saharan dust and black carbon on albedo and long-term glacier mass balance of an Alpine glacier

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Abstract. Light-absorbing impurities in snow and ice control glacier melt as shortwave radiation represents the main component of the surface energy balance. Here, we investigate the long-term effect of snow impurities, i.e. Saharan mineral dust and black carbon (BC), on albedo and glacier mass balance. The analysis was performed over the period 1914–2014 for two sites on Claridenfirn, Swiss Alps, where an outstanding 100 year record of seasonal mass balance measurements is available. Information on atmospheric deposition of mineral dust and BC over the last century was retrieved from two firn/ice cores of high-alpine sites. A combined mass balance and snow/firn layer model was employed to assess the dust/BC-albedo feedback effects of melt and accumulation processes on the impurity concentration at the surface and thus on albedo and glacier mass balance. Compared to pure snow conditions, the presence of Saharan dust and BC lowered the mean annual albedo by 0.04–0.06 and increased melt by 15–19% on average depending on the location on the glacier. Consequently, annual melt was increased by 15–19% and the mean annual mass balance was reduced by about 280–490 mm w.e. BC clearly dominated absorption which is about three times higher than that of mineral dust. The upper site has experienced mainly positive mass balances and impurity layers were continuously buried whereas at the lower site, surface albedo was more strongly influenced by re-exposure of dust-enriched dust and BC-enriched layers due to frequent years with negative mass balances.

1 Introduction

Deposition of mineral dust and BC have a fundamental impact on the energy balance of glaciers and snow-covered areas by increasing the absorption of solar radiation. Along with the enhanced melting
due to the darkening of the snow surface, the growth of snow grains is accelerated, which further reinforces snow melt rates (Painter et al., 2007). While light-absorbing impurities control the snow albedo mainly in the visible wavelengths, the snow grain size affects the albedo in the near-infrared. Shortwave radiation is the dominant energy source for melting of snow, firn and ice, and consequently the surface albedo has an important influence on the mass budget of glaciers (Oerlemans et al., 2009).

Repeated years with negative glacier mass balances lead to a shift in the equilibrium line to higher elevations and to the re-exposure of dust-enriched dust and BC-enriched firn layers at the surface. Snow impurities are mainly retained at the surface during conditions of melt and surface concentrations might be enhanced by up to one order of magnitude involving resulting in a pronounced melt amplification (Sterle et al., 2013).

Absorptive impurities consist of mineral dust, carbonaceous particles and coloured organic matter (Warren, 1984). Advection of dust-loaded air masses from the Saharan desert leads to episodic deposition of large amounts of mineral dust in the Alps. Analyses of firn cores from high-alpine sites, resolving the signal of the continental background aerosols, indicated that long-range transported crustal impurities account for about two thirds and local impurities for about one third of the total mineral dust deposited (Wagenbach and Geis, 1989). One single Saharan dust deposition event may even supply 30% of the total annual dust budget at high-altitude mountain glaciers (Schwikowski et al., 1995). Most prominent Saharan dust episodes in the Alpine region occurred in the years 1936/1937, 1977, 1990 and 2000 leaving marked dust horizons in firn/ice cores (Schwikowski et al., 1995; Jenk et al., 2009; Sigl, 2009).

BC refers to the strongly light-absorbing component of soot and is emitted naturally and anthropogenically by incomplete combustion of fossil fuels and by biomass burning. BC has become a focus of interest as it has been identified recently as one of the major contributors to global climate change (Ramanathan and Carmichael, 2008; Bond et al., 2013). BC contributes to global warming by absorption of sunlight, firstly when it is suspended in the atmosphere, and secondarily when it is deposited on snow and ice by reducing the albedo and hence accelerating melting. Along with the beginning of the industrialisation, global BC emissions sharply increased and continued to rise into the 21st century. Since mid-20th century In the European region, BC concentrations started to decrease since mid-20th century and have stabilised over the last few decades (Bond et al., 2007).

Recently different studies investigated the impact of light-absorbing impurities on snow albedo and melting of snow. Based on a 10 year record of mineral dust and BC concentrations retrieved from an ice core at Mera Peak, Nepalese Himalaya, Ginot et al. (2014) found that light-absorbing particulates cause up to 26% of the total annual surface melting. Another study performed at Mera Peak shows that mineral dust dominates absorption and may reduce the albedo of snow by up to 40% (Kaspari et al., 2014). The Investigations for the Colorado River Basin, Western US, show that the radiative forcing of mineral dust deposition may shorten the duration of snow cover by several weeks
(Skiles et al., 2012) and also affects the timing and magnitude of runoff (Painter et al., 2010). It was suggested that increasing anthropogenic emissions of black carbon during the Industrial Revolution have forced the end of the Little Ice Age in the Alps (Painter et al., 2013).

In this study we assess the significance of natural mineral dust and anthropogenic BC particles in snow and firn on the mass balance of a high-mountain glacier over a centennial period (1914–2014). Using a unique 100 year record of seasonal glacier mass balances, ice core records of past atmospheric deposition of Saharan dust BC and a sophisticated modelling approach, we examined the dust/BC-melt feedback of light-absorbing impurities to glacier melt for (1) a site with accumulation conditions over the entire period, where dust is predominately buried by winter snow, and (2) a site at the glacier’s equilibrium line involving a re-exposure of buried dust and BC layers at the surface in years with negative mass balance. We have chosen Claridenfirn (Swiss Alps) where the worldwide longest data series of seasonal glacier mass balance exists which enables an accurate and field data-based simulation of ablation and accumulation processes. In order to simulate the feedback between melt, accumulation and snow impurities, a mass balance model was coupled with a snow density model, which tracks the position and the thickness of deposited snow layers and impurities. The mass balance model incorporates an enhanced temperature-index melt model including the shortwave radiation balance and a parameterisation for albedo, which is based on the specific surface area of snow and the impurity concentration in the surface snow.

2 Study site and data

Claridenfirn is a mountain glacier with an area of approximately 5 km² and is located on the northern Alpine Ridge of the Swiss Alps. The glacier is exposed to the southeast and covered an elevation range of 2540 to 3267 m a.s.l. in 2003 (Fig. 1).

First mass balance measurements date back to 1914 and provide a unique data set covering a period of 100 years. At two different sites, at a lower stake (2680 m a.s.l.) and an upper stake (2890 m a.s.l.), winter, summer and annual mass balance have been measured every year using stakes and snow pits in mid-May and end of September, respectively. Simultaneously snow density measurements in snow pits have been carried out. The measurements at Claridenfirn are the longest continuous glacier mass balance observations worldwide. More details about the monitoring programme on Claridenfirn are provided by Müller and Kappenberger (1991) and Huss and Bauder (2009).

The forcing of the mass balance model requires daily air temperature and precipitation data for 1914–2014. We used air temperature recorded by the MeteoSwiss weather station Säntis (2490 m a.s.l.), the closest station with long-term records and homogenized time series (Fig. 1, Begert et al., 2005). Monthly air temperature lapse rates were derived by comparison of nearby
weather stations to transpose the temperature to the elevation of the study sites. Time series of daily precipitation were taken from a local weather station, Elm (965 m a.s.l.), situated at a distance of 22 km from Claridenfirn (Fig. 1).

Furthermore, our model requires daily time series of incoming shortwave radiation that were derived from a simple parameterisation based on daily temperature ranges (see Sect. 3). Daily maximum and minimum temperature were provided from the MeteoSwiss weather station at Davos over the period 1914–2014 (Fig. 1). For calibrating the parameterisation, daily values of incoming solar radiation of 1981–2014 recorded at the same station were used. In addition, a unique data set of monthly means of global solar radiation for Davos, covering the period 1936–2014, is provided by the Global Energy Balance Archive (GEBA; Ohmura et al., 1989), and was employed to improve the performance of the cloud factor parameterisation.

A firn/ice core from the cold glacier saddle of Colle Gnifetti (4455 m a.s.l., Monte Rosa, Switzerland), retrieved in 2003, provides a continuous record of annual iron (Fe) concentrations over 1914–1997 (Sigl, 2009), which was used to infer the mineral dust concentration in precipitation (Fig. 2a). For the years 1998–2007, which are not covered by the Fe data, the Fe concentration was derived from the calcium record, extending the 2003 data set with a shallow core collected at the same site in 2008 (Sigl, 2009), taking advantage of the high correlation between the two dust tracers. Concentrations of BC were obtained from a firn/ice core from Fiescherhorn (3900 m a.s.l., Bernese Alps, Switzerland) drilled in 2002 (Fig. 2a; Jenk et al., 2006). This core provides mean yearly concentrations of elemental carbon (EC) over the period 1914–2002, which can be used as proxy for BC, as EC and BC are constituted of the same fraction of carbonaceous particles (Lavanchy et al., 1999). For BC and mineral dust concentrations of the years 2002–2014 and 2007–2014, respectively, which are not covered by the ice core data, a mean concentration averaged over the entire period was assigned (Fig. 2a). Furthermore, daily BC aerosol measurements of Jungfraujoch (3580 m a.s.l., Fig. 1) conducted in the frame of the Global Atmosphere Watch (GAW) monitoring programme covering the period 1995–2000, were used to derive an annual cycle of BC concentrations in the atmosphere.

3 Methods

In order to determine the impact of Saharan dust events on surface albedo and glacier melt, a mass balance model including a parameterisation for snow, firn and ice albedo was coupled with a snow/firn density model to track the position and thickness of the snow layers and dust. The physical albedo parameterisation is based on the evolution of the specific surface area of snow grains and includes the option to simulate the effect of snow impurities on pure snow albedo. Atmospheric input of mineral dust and BC was derived based on the ice/firn core data. The mass balance model was forced by daily time series of air temperature, precipitation and incoming shortwave radiation and was run over a 100 year period (1 October 1914 to 30 September 2014). Hereafter, the data series of
mineral dust and BC and the individual components of the employed mass balance and snow density model are described in detail.

3.1 Input of mineral dust and black carbon

3.1.1 Mineral dust

The absorption of mineral dust in the visible spectrum is highly sensitive to the content of iron oxides. Following Kaspari et al. (2014) determined light-absorption of mineral dust in snow and ice of a Himalayan glacier based on gravimetrically determined Fe concentrations. Accordingly, we used records of iron (Fe), provided by the ice core, to infer mineral dust concentrations. Iron oxides mainly consist of the minerals goethite and haematite (Sokolik and Toon, 1999; Lafon et al., 2006). Since they have different light absorption spectra (e.g. Lafon et al., 2006) their relative proportion has to be known for calculating the radiative properties of dust. According to Shi et al. (2011) the ratio of haematite to mass ratio of the mineral haematite to the minerals haematite plus goethite for Saharan dust is 0.42 on average. Based on the assumption that about 45–64 % of the total Fe is encompassed in light-absorbing oxides (Lafon et al., 2004), the mass of goethite and haematite is calculated following Kaspari et al. (2014) and used as proxy for the absorption of mineral dust.

Most of the dust peaks can be related to long-range transported crustal impurities, which account for about 70 % of the total deposited mineral dust (Wagenbach et al., 1996). This is a conservative assumption since local dust contains a lower portion of Fe-oxides. We therefore assume that all mineral dust is made up by Saharan dust.

Errors in the annual layer counting of the ice cores might involve uncertainties of ±1–2 years (Eichler et al., 2000). However, we consider this having a minor impact on mass balance simulations since dates of intense Saharan dust events are well known and smaller events might have a minor effect on average mass balance over a 100 year period.

The annual amount of mineral dust (i.e. Fe-oxide) was distributed over the year according to the Saharan dust climatology reported by Collaud Coen et al. (2004). They analysed the number and duration of Saharan dust events per month based on measurements of the aerosol scattering coefficient performed at Jungfraujoch in the years 2001 and 2002. Higher probability of occurrence was observed in the March–June and the October–November period. Extended time series of the years 2001–2012 confirm this distribution (MeteoSwiss, 2014a). Three different classes of Saharan dust events were defined: Saharan dust events lasting between 4 and 10 h, between 10 and 24 h and longer than 24 h. The inferred average distribution of the number of events per month and the mean duration of each class were scaled by the annual dust concentrations obtained from the ice core analysis in order to derive daily atmospheric deposition rates of Saharan dust.

Days within a month were randomly selected except for extraordinarily large events of the years 1936, 1977, 1990 and 2000 for which the date of deposition is exactly known from literature (SMA-
Annalen, 1864–2014; Prodi and Fea, 1979; Schwikowski et al., 1995). We assigned 30 % of the total annual dust amount to these extraordinary large events according to Schwikowski et al. (1995).

3.1.2 Black carbon

While Saharan dust transport has an episodic character, deposition of BC is controlled by seasonal variations in atmospheric stability, which is higher in winter than in summer. In order to mimic the yearly cycle of BC input, daily ambient BC measurements at Jungfraujoch, performed in the frame of the GAW monitoring programme, were used. Based on these measurements, daily anomalies averaged over the period 2002–2013 were derived and applied to the annual BC concentrations provided by the firn/ice core in order to infer daily atmospheric deposition rates of BC (Fig. 2b).

3.1.3 Scaling to study site

Several studies performed detailed investigations of the regional and altitudinal distribution of major ions in the high Alpine region (e.g. Nickus et al., 1997; Rogora et al., 2006). They found a marked regional variability but no clear trends, neither in distance nor in altitude. Due to a lack of clear indication, we assumed that Fe/BC concentrations at Claridenfirn are in a similar range as the concentrations observed on Colle Gnifetti and Fiescherhorn, respectively, and employed measured Fe/BC concentrations directly without a transfer function. In order to estimate the influence of potential differences in their input concentration we performed a sensitivity analysis (see Sect. 5).

3.2 Mass balance model

For simulating snow and ice melt, the enhanced temperature-index (ETI) model (Pellicciotti et al., 2005) was employed. This model computes melt as a function of air temperature and shortwave radiation and accounts for the effects of albedo and cloudiness on melting:

\[
M = \begin{cases} 
TF T_a + SRF(1 - \alpha)G : & T_a > T_T \\
0 : & T_a \leq T_T 
\end{cases}
\]  

(1)

where \(T_a\) is the air temperature, \(TF\) (mm d\(^{-1}\) C\(^{-1}\)) and \(SRF\) (mm m\(^2\) d\(^{-1}\) W\(^{-1}\)) are the tuning parameters, \(\alpha\) the surface albedo and \(G\) the global incoming shortwave radiation (W m\(^{-2}\)). \(T_T\), the threshold temperature above which melt occurs, is set to 0 °C. \(G\) is calculated from a cloud transmissivity factor, \(cf\), and the clear-sky incoming solar radiation, the latter based on the approaches by Iqbal (1983) and Corripio (2003).

Snow accumulation was computed by the station precipitation and a correction factor, \(c_{\text{prec}}\), accounting for the elevation difference between the station and the glacier and gauge undercatch. A threshold temperature of 1.5 °C with a linear transition range of ±1.0 °C was applied to calculate the occurrence of solid and/or liquid precipitation.
Cloud factor parameterisation

The cloud transmissivity factor, cf, accounts for the attenuation of solar radiation by clouds and is derived as a function of daily temperature ranges ($\Delta T$, Pellicciotti et al., 2011):

$$ cf = d_1 \Delta T + d_2. \tag{2} $$

The two coefficients, $d_1$ and $d_2$, were derived by linear regression of the daily air temperature range and the difference between actual and potential clear-sky incoming solar radiation. Using the weather station data from Davos (Fig. 1), parameters were calibrated over the period 1981–2013. Monthly means of global solar radiation of 1936–2014 allowed verifying the performance of the cloud factor parameterisation over decadal periods. Despite the simplicity of the approach, simulated shortwave radiation agreed well with observations (Fig. 3). During the 1940s, when very high incoming solar radiation was recorded, the cloud factor parameterisation, however, exhibited difficulties in reproducing the observations. In order to obtain as reliable as possible radiation values in daily resolution, the monthly averages of daily incoming shortwave radiation derived from the cloud factor parameterisation were adjusted to match the monthly means measured at Davos for the years with data (i.e. 78% of the study period, Fig. 3).

3.3 Albedo model

Snow albedo was derived according to the physical snow albedo parameterisation by Gardner and Sharp (2010) as the sum of pure snow albedo and its change due to impurities. The albedo of ice was kept constant at 0.2 (Pellicciotti et al., 2005). Pure snow albedo, $\alpha_{\text{SSA}}$, is calculated as a function of the specific surface area, SSA, of snow as

$$ \alpha_{\text{SSA}} = 1.48 - \text{SSA}^{-0.07}. \tag{3} $$

Details on the calculation of SSA are given below. The change in pure snow albedo due to loading of light-absorbing impurities is derived according to

$$ d\alpha_C = \max \left( 0.04 - \alpha_{\text{SSA}}, \frac{-C^{0.55}}{0.16 + 0.6\text{SSA}^{0.5} + 1.8C^{0.6}\text{SSA}^{-0.25}} \right), \tag{4} $$

where $C$ is the concentration of BC in mg kg$^{-1}$ (Gardner and Sharp, 2010). In order to model the effect of mineral dust on snow albedo, the mineral dust (i.e. Fe oxides) was converted to optically equivalent concentrations of light-absorbing carbon using mass absorption coefficients (MACs) of BC and Fe oxides of 7.5–6.8 and 0.56 m$^2$ g$^{-1}$, respectively (Alfaro et al., 2004; Kaspari et al., 2014). The direct-beam albedo of the impurity-loaded snow is then obtained as $\alpha = \alpha_{\text{SSA}} + d\alpha_C$. The effect of the solar zenith angle on the albedo is not considered as the model runs on daily basis.
3.3.1 SSA model

The specific surface area of the snow grains was calculated relying on the approach by Roy et al. (2013) that considers both dry and wet snow metamorphism. In the case of dry snow conditions, the evolution of SSA is computed according to Taillandier et al. (2007), as a logarithmic function of snow age and snow temperature, \( T_{\text{snow}} \), as

\[
\text{SSA}(t) = [0.629 \cdot \text{SSA}_{\text{initial}} - 15.0 \cdot (T_{\text{snow}} - 11.2)]
- [0.076 \cdot \text{SSA}_{\text{initial}} - 1.76 \cdot (T_{\text{snow}} - 2.96)]
\cdot \ln \left\{ t + e^{-0.371 \cdot \text{SSA}_{\text{initial}} - 15.0 \cdot (T_{\text{snow}} - 11.2)} \right\}.
\] (5)

The approximation by Brun (1989) is used to simulate the evolution of snow grains under wet conditions with respect to the liquid water content of the snowpack. The growth of the optical radius of snow, \( \Delta R_{\text{opt}} \) (mm d\(^{-1}\)), is calculated as

\[
\Delta R_{\text{opt}} = \frac{C_1 + C_2 \cdot \theta^3}{R_{\text{opt}}^2 \cdot 4\pi},
\] (6)

where \( C_1 = 1.1 \times 10^{-1} \) mm\(^3\) d\(^{-1}\), \( C_2 = 1.1 \times 10^{-3} \) mm\(^3\) d\(^{-1}\), and \( C_3 = 3.7 \times 10^{-5} \) mm\(^3\) d\(^{-1}\) are empirical coefficients and \( \theta \) is the liquid water content in mass percentage. The SSA decrease is more pronounced when \( \theta \) increases. If the liquid water content is greater than zero, the model-derived SSA value is converted into its equivalent optical radius, \( R_{\text{opt}} \), with

\[
R_{\text{opt}} = \frac{3}{\rho_{\text{ice}} \cdot \text{SSA}},
\] (7)

where \( \rho_{\text{ice}} \) is the density of ice. Then, Eq. (6) is applied and \( R_{\text{opt}} \) is reconverted to SSA using Eq. (7).

The initial SSA was set to 73.0 m\(^2\) kg\(^{-1}\) (Domine et al., 2007). Following Taillandier et al. (2007), a minimal SSA value of 8.0 m\(^2\) kg\(^{-1}\) was used to avoid unrealistically low values. The liquid water content of the snowpack is provided by a snow density model (see below).

3.3.2 Snow density model

A snow densification model is required to determine the position and the thickness of each snow layer. The simple point model by De Michele et al. (2013) for bulk snow density and snow depth was employed and applied to each snow layer. The two-constituent model solves mass balance equations for the dry and liquid mass of the snow pack, as well as momentum balance and rheological equations for the dry part. It results in a system of three differential equations for depth and density of the dry part of the snowpack, and the depth of liquid water. Sublimation and evaporation are not considered. The main characteristics of the model are shortly described in the following. For more detailed information see De Michele et al. (2013).

A simplified energetic description of the snowpack assuming thermal equilibrium between constituents is used. The temperature profile, \( T_{\text{snow}}(z) \), is calculated according to Kondo and Yamazaki (1990) as a bilinear function with snow depth, \( h_z \):
\[ T_{\text{snow}}(z) = \begin{cases} 
 T_a - a_t \cdot (z - h_s) & : \quad h_s \geq z \geq z_0 \\
 0^\circ C & : \quad z_0 \geq z \geq 0 
\end{cases} \]  

where \( z \) is the snow depth, \( z_0 \) the maximum value of \( z \) where the snow temperature reaches \( 0^\circ C \) and \( a_t \approx 0.033^\circ C \text{mm}^{-1} \) the temperature gradient in the surface-near layer.

The change in snow depth, \( \frac{dh_s}{dt} \), is calculated by considering the effects of snow density changes, fresh snow and melt \( M \):

\[ \frac{dh_s}{dt} = \frac{h_s}{\rho_d} \frac{d\rho_d}{dt} + \frac{\rho_f}{\rho_d} s - M, \]  

where \( \rho_d \) is the density of dry snow, \( \rho_f \) the density of fresh snow, and \( s \) the snow precipitation rate. The fresh snow density is derived as a sole function of air temperature following Anderson (1976).

The height of liquid water, \( h_w \), is controlled by the amount of liquid precipitation, melt and outflow of the snow pack. Water outflow is calculated according to Nomura (1994) and Singh (2001) by a kinematic wave approximation. If the liquid water content, \( \theta \), is larger than the residual water content, \( \theta_r \), then the outflow \( O \) is obtained as \( O = c \rho_w \theta h_w^d \) with \( c \) and \( d \) as constants and \( \rho_w \) as the density of water. The residual water content is computed as \( \theta_r = F_c \rho_d / \rho_w \) with \( F_c = 0.02 \) (Tarboton and Luce, 1996; Kelleners et al., 2009) the mass of water retained per mass of dry snow. The exponent \( d \) is set to \( d = 1.25 \) as proposed by Nomura (1994) and the site-specific coefficient \( c \) is assumed to be equal to \( 1 \text{m}^{-1} \text{h}^{-(d-1)} \) (De Michele et al., 2013). The change in liquid water height, \( \frac{dh_w}{dt} \), is calculated with

\[ \frac{dh_w}{dt} = p + \frac{\rho_d}{\rho_w} M - c \theta h_w^d, \]  

where \( p \) is the liquid precipitation rate.

The momentum balance equation, \( \sigma - \rho_d gh_s \), and the rheological equation, \( \eta = \sigma / \dot{\epsilon} \), are used to infer snow density changes, where \( \sigma \) is the vertical stress, \( g \) the gravitational acceleration, \( \dot{\epsilon} \) the vertical strain rate, and \( \eta \) the coefficient of viscosity computed as an exponential function of snow density and snow temperature. Accordingly, snow density changes are calculated as

\[ \frac{d\rho_d}{dt} = c_1 h_s \rho_d^2 e^{(k_1(T_{\text{snow}} - T_r) - k_0 \rho_d)}, \]  

where \( c_1 \), \( k_1 \) and \( k_0 \) are constants set to 0.001 m² h⁻² kg⁻¹, 0.08 °C⁻¹ and 0.021 m³ kg⁻¹, respectively (Kongoli and Bland, 2000; Ohara and Kavvas, 2006; Zhang et al., 2008). Equation (11) describes the change in density due to compaction and temperature change, and is calculated as an exponential function of snow density and snow temperature following Kojima (1967) and Mellor (1975).

### 3.3.3 Snow layer model

Each precipitation event was considered as a single snow layer which is stacked atop of the snow pack. Snow layers with a thickness of less than 1 cm were merged with the underlying layer in order
to reduce computational efforts and to avoid arithmetic errors. If snow density exceeded the pore
close-off density (830 kg m\(^{-3}\)), snow was treated as ice, and the corresponding snow layers were
removed from the system.

### 3.4 Snow impurity model

Mineral dust and BC entered the system by liquid or solid precipitation, as wet deposition is expected
to be the predominant mechanism (Raes et al., 2000; Koch, 2001). Particulate impurities were sup-
posed to be evenly distributed in precipitation and consequently also in the snow layers. Particulates
remained in the corresponding snow layer as long as there was no melt. When melt occurred, im-
purities of the melted snow were accumulated in the top 2 cm of the remaining snow layers (e.g.
Flanner et al., 2007). When a snow fall event occurred, the dust-enriched and BC-enriched top
layer became an independent snow layer and was buried by fresh snow. We assumed constant ice
albedo and no dust reservoir for ice since the effects of snow impurities on the ice albedo and the
removal of snow impurities by melt water on ice are only poorly understood and subject to a high
spatial variability. Hence, when firn turned into ice, the dust and BC of the corresponding layer was
removed from the system.

Melt water percolation may lead to vertical redistribution of snow impurities. Different studies
have investigated the removal of particulate impurities by melt water (e.g. Conway et al., 1996;
Flanner et al., 2007). They found that larger particles (> 5 µm) remain mostly in the snow and are
not efficiently removed by percolation of melt water (Conway et al., 1996), whereas smaller snow
impurities (~0.2 µm) are washed out by about 10–30% per mass of melt (Doherty et al., 2013).
According to these results, we assumed that mineral dust (particle size 2.5–4.5 µm) is not affected
by wash-out due to melt water, whereas for BC (particle size 0.2–0.3 µm) a removal efficiency (the
amount of BC which is removed by melt water with each increment of melt) of 20% was assumed
(Flanner et al., 2007).

### 3.5 Calibration

The melt parameters, TF and SRF, and the accumulation parameter, \(c_{\text{prec}}\), were calibrated for
each year individually by means of the seasonal balance measurements. This annual calibration
ensures that simulated mass balances coincide with observations in order to match modelled and
observed extract an accurate sequence of melt and accumulation rates events controlling the surface
concentration of light-absorbing impurities. In a first step, \(c_{\text{prec}}\) was adjusted according to the mea-
sured winter accumulation, then TF and SRF were tuned to the annual mass balance records. This
procedure is repeated until the difference between simulated and observed mass balance was less
than 10 mm water equivalent (w.e.). The ratio between TF and SRF was kept constant over the en-
tire period in order to reduce the degrees of freedom and to avoid changes in air temperature/radiation
sensitivity of the model among individual years. The ratio was set to 0.04 according to extensive test-
ing for another Alpine glacier (Gabbi et al., 2014). During calibration the complete snow impurity and snow density model was used.

4 Results

4.1 Snow impurity concentration

4.1.1 Saharan dust

At the upper measurement site, located in the accumulation area of Claridenfirn, the mean annual Fe-oxide concentration in the surface layer was \(0.92 \pm 1.04 \text{ mg kg}^{-1}\) on average. Exceptionally high surface loads were observed in years with increased deposition of Saharan dust, particularly in 1936, 1977, 1990 and 2000 (Fig. 4a). Annual Fe-oxide concentrations of up to \(6.3 \text{ mg kg}^{-1}\) occurred at the upper stake. Concentrations of similar magnitude as in years with high Saharan dust input were reached in the late 1940s. Periods of intense solar radiation, such as in the 1940s, led on the one hand to increased melting due to higher transmissivity of the atmosphere (Huss et al., 2009b) and on the other hand to an enhanced re-exposure of snow impurities, and thus to a distinct darkening of the glacier surface which further reinforced ablation.

At the lower measurement site, located near the glacier’s equilibrium line altitude (ELA), the mean Fe-oxide concentration was more than twice as high as at the upper stake and was \(2.24 \pm 3.33 \text{ mg kg}^{-1}\) on average. Consistent with the upper site, increased mineral dust amounts were observed during years with high Saharan dust activity and during periods with intense melting (Fig. 4b). In addition to the 1940s, a second period with pronounced accumulation of mineral dust due to enhanced melting occurred in the 2000s. In 2007, the mean Fe-oxide concentration reached a maximum value of \(26.8 \text{ mg kg}^{-1}\) as a result of the almost complete melting of the firn layers and thus, the re-exposure of heavily dust-loaded layers (e.g. extraordinarily large Saharan dust events of 2000). From 2008 onwards, surface Fe-oxide concentrations at the lower stake declined sharply as all firn layers have been depleted and the bare ice surface was exposed. Thus, due to the prescribed constant ice albedo, the remaining dust did not have an influence on albedo and was assumed to be washed out at the impermeable ice surface.

In the accumulation area (upper stake) most of the mineral dust exposed at the surface originated from deposition occurring during the same year. Only in the few years with negative mass balances mineral dust of previous years reappeared and reinforced the darkening of the glacier surface. In specific years (e.g. 1947 and 1991), mineral dust of previous years accounted for 45–65 % of the total mineral dust at the surface (Fig. 5a). On average, however, the fraction of mineral dust of preceding years becoming albedo-relevant was small and made up only 8 % of the total surface dust budget. At the ELA (lower stake) mineral dust of previous years more effectively influenced surface dust concentrations and accounted for about 30 % of the total exposed mineral dust. Particularly in
the 1940s and 2000s, but also in the early 1960s and the 1990s, large quantities of previously buried dust were re-exposed at the surface. Up to 97% of the total surface dust in 2006 and 2007 originated from deposition in preceding years (Fig. 5b). Accordingly, mineral dust of much older layers was re-exposed at the surface of the lower measurement site in comparison to the upper stake. While at the stake in the accumulation area, surface dust had a maximum age of three years, mineral dust at the lower stake was found to have an age of up to 21 years (Fig. 5c, d).

4.1.2 Black carbon

Mean surface concentrations of BC showed a distinctly different pattern than mineral dust concentrations. BC concentrations at the glacier surface were mainly controlled by the melt regime and were less influenced by episodic deposition compared to Saharan dust (Fig. 4). An exception was the year 1982, when exceptionally high deposition of BC were recorded (see Fig. 2a). Mean concentrations of BC over the entire period were \(0.26 \pm 0.14\) and \(0.46 \pm 0.29\) mg kg\(^{-1}\) on average for the upper and lower stake, respectively. For both locations, highest BC concentrations were observed in the melt-intense years around 1947 and the deposition-intense year 1982 (Fig. 4). BC concentrations of up to \(0.78\) mg kg\(^{-1}\) (upper stake) and \(2.12\) mg kg\(^{-1}\) (lower stake) were found.

4.1.3 Absorption of mineral dust vs. black carbon

In contrast to BC, mineral dust concentrations at the surface were up to five times larger. In return, the mass absorption coefficient of BC is about one order of magnitude higher than that of mineral dust and hence, reduction in albedo due to BC and mineral dust was in a. However, as BC is much more absorptive than mineral dust (mass absorption coefficient about 10 times higher), the overall absorption by BC and dust are in a similar range. In individual years with extraordinarily high Saharan dust input, such as in 1936, 1977, 1990 and 2000, mineral dust dominated the absorption of solar radiation (Fig. 6). In all other years, the absorption of BC outweighed the absorption of mineral dust and over the entire period BC was clearly the dominant absorber. While at the upper stake, the absorption due to BC was 3.3 times higher on average compared to mineral dust, at the lower stake BC resulted in a 2.2 times higher absorption. These statements are based on the assumption that BC is more efficiently removed by melt water than mineral dust and therefore depend on the chosen removal efficiency. If removal rates of BC and mineral dust would be in a similar range, the influence of BC on the absorption would be markedly stronger than that of mineral dust even larger.

4.2 Effect of Saharan dust and black carbon on albedo and mass balance

4.2.1 Surface albedo

On average the reduction of mean annual surface albedo due to Saharan dust was less than 0.01 compared to snow with BC only. At the upper measurement site the mean annual albedo was reduced
by 0.004±0.004, at the lower stake by 0.008±0.009. Regarding summer albedo (April–September), i.e. the albedo during the period with snow, firn and ice melting, the effect of Saharan dust was larger and reduced the mean summer albedo at the upper stake and lower stake by 0.006±0.006 and 0.011±0.012, respectively. However, in individual years with a high accumulation of Saharan dust (i.e. years with a high Saharan dust input and/or melt-intense periods) the impact on snow albedo was significantly larger. At the lower measurement site, at the transition between accumulation and ablation zone, the largest reduction in albedo occurred in 2007, when the mean annual albedo was reduced by about 0.060. At the upper stake, highest influence of Saharan dust on the surface albedo was observed in the dust-intense year 2000 with a maximal albedo reduction of 0.025.

The overall impact of BC on the surface albedo was substantially higher and was about seven times larger than that of Saharan dust. Our results suggest that BC reduced the albedo over 1914–2014 by 0.027±0.009 at the upper stake and by 0.038±0.013 at the lower stake compared to snow with dust only. The largest contribution of BC to albedo reduction occurred in the melt dominated periods in the 1940s and the 2000s, when the albedo was lowered by up to 0.06. In total, Saharan dust and black carbon reduced the mean annual albedo by 0.041 and 0.062 on average compared to pure snow at the upper and lower stake.

4.2.2 Mass balance

The impact of Saharan dust on the total mass change over the 100 year period was in the order of a few meters and was less pronounced in the accumulation area than at the ELA (Fig. 7). At the upper measurement site, the difference in total cumulative mass balance due to Saharan dust was 2.8 m w.e. compared to the measured total 100 year cumulative mass balance of 125.8 m w.e. At the lower stake, the absolute difference was twice as large and was 5.8 m w.e. (with a total cumulative mass balance of 26.4 m w.e.). Regarding annual balance, Saharan dust thus accounted for about −28 mm w.e. yr⁻¹ at the upper stake and for about −58 mm w.e. yr⁻¹ at the lower stake compared to snow with BC only (Fig. 8a and c). Mean annual melt was increased by about 1.4 % (upper stake) and 2.0 % (lower stake) by the presence of Saharan dust. In specific years, Saharan dust enhanced the overall annual melt by up to 13 %.

Maximum deviations in annual mass balance due to Saharan dust were up to −142 mm w.e. yr⁻¹ for the upper and −271 mm w.e. yr⁻¹ for the lower measurement site in individual years. In years with high dust concentrations at the surface (Fig. 4) also largest changes in mass balance were observed (Fig. 8a and c). However, changes in mass balance cannot be directly deduced from average dust concentrations, because (1) the impurity concentration and albedo changes are not linearly related and thus a higher impurity concentration might lead to smaller changes in albedo, and (2) during years with high melt rates also other particulate impurities accumulate at the surface, which limits the total impact of Saharan dust on surface mass balance. Hence, Thus, despite the exceptionally high mineral dust concentrations surface concentration in 2007 at the lower stake led to a...
change in mass balance due to Saharan dust which is comparable to the mass balance impact is only slightly larger than in years with very high Saharan dust supply such as lower surface concentrations as for example in the deposition intense year 2000 (Fig. 8a and c).

The BC-induced albedo changes led to an average reduction in annual mass balance of 183 mm w.e. yr\(^{-1}\) at the upper and of 301 mm w.e. yr\(^{-1}\) at the lower stake compared to snow with dust only. In individual years, annual mass balance anomalies might reach up to −494 mm w.e. yr\(^{-1}\) at the upper stake and up to −754 mm w.e. yr\(^{-1}\) at the lower stake (Fig. 8b and d). Thus, mean mass balance changes due to BC were about six to seven times larger and peak values up to three times larger compared to the effect of Saharan dust. The difference in cumulative mass balance between the real situation, being consistent with direct field observations (including mineral dust and BC in the model), and simulations without BC (but with mineral dust) over 1914–2014 is 18.3 m w.e. for the upper and 30.1 m w.e. m.w.e. for the lower stake (Fig. 7). Annual melt rates were amplified by 9% (11%) at the upper (lower) stake on average and by 19% (22%) at maximum.

The combined effect of Saharan dust and BC on melt resulted in an overall amplification of melt of about reduced the mean annual mass balance by 282 mm w.e. yr\(^{-1}\) and 485 mm w.e. yr\(^{-1}\) at the upper and lower stake, respectively. Annual melt was amplified by 15% (upper stake) and 19% (lower stake) on average by the presence of two light-absorbing impurities. In the year 1947, characterized by exceptionally high melt rates, Saharan dust and BC intensified annual melt by up to 36%.

5 Discussion

5.1 Radiative forcing

Converting changes in annual mass balance caused by absorption of dust/BC into the energy consumed for melt allowed calculating the radiative forcing of snow impurities. The radiative forcing (RF, W m\(^{-2}\)) was calculated based on the change in melt rate, \(\Delta M\) (m s\(^{-1}\)), caused by the presence/absence of mineral dust and/or BC in snow:

\[
RF = \Delta Q_M = \Delta M L_f \rho_W
\]  

where \(Q_M\) (W m\(^{-2}\)) is the energy consumed by melt, \(L_f\) (333\,700 J kg\(^{-1}\)) the latent heat of fusion and \(\rho_W\) (1\,000 kg m\(^{-3}\)) the density of water. Changes in melt rates are equal to changes in mass balance as presented in Section 4.2.2.

For the measurement site in the accumulation area we found a mean radiative forcing over the 100 year period of +0.3 W m\(^{-2}\) due to Saharan dust, whereas at the stake close to the equilibrium line the radiative forcing was +0.6 W m\(^{-2}\). In contrast to Saharan dust, the radiative forcing of BC over 1914–2014 was about seven times larger, and was +1.9 and +3.2 W m\(^{-2}\) on average for the two
sites. In the summer months, July and August, when melting is strongest, the radiative forcing for BC reached values of 8.7–9.7 W m$^{-2}$ and for Saharan dust of 3.0–3.7 W m$^{-2}$ compared to pure snow at the upper stake, and 12.9–15.9 and 4.7–6.3 W m$^{-2}$ at the lower stake, respectively. At the daily scale, maximum modelled radiative forcing was 15–42 W m$^{-2}$ for Saharan dust and 43–66 W m$^{-2}$ for BC.

At a global scale, the mean radiative forcing from BC in snow is reported to be in the range of 0.02–0.08 W m$^{-2}$ (Bond et al., 2013; IPCC, 2013). During boreal spring, when the snow-albedo feedback is maximal, the radiative forcing of mineral dust and BC over Eurasia is higher and amounts to 1.2 and 2.7 W m$^{-2}$, respectively (Flanner et al., 2009). For snow-covered surfaces of the Tibetan Plateau the radiative forcing of BC reaches values of up to 5–25 W m$^{-2}$ in springtime (Flanner et al., 2007; Kopacz et al., 2011; Qian et al., 2011). Similar peak values are found for desert dust on snow-covered surfaces in spring on the Colorado Plateau in the mountain snow cover of the Colorado River Basin (25–50 W m$^{-2}$, Painter et al., 2007; Skiles et al., 2012). In general, radiative forcing of BC found for Claridenfirn is at the lower end of the range of values obtained for Colorado River Basin or Tibetan Plateau. Regarding mineral dust, the effect is also clearly stronger on the Colorado Plateau in the Western US than in the Alps. In terms of maximum daily radiative forcing, values obtained for Claridenfirn seem to be of similar magnitude as for other regions. However, radiative forcing reported in other studies is not directly comparable to the results of this study as often only the effect of snow impurities on winter snow cover and relative to sites at lower elevation was examined. Dust/BC source and the temporal dynamics of melting are different.

Furthermore, radiative forcing of some of the above-mentioned studies was calculated by directly accounting for the change in energy fluxes, rather than using the change in melt rates due to light-absorbing impurities as in our approach. Hence, the radiative forcing reported here represents a lower limit as the radiative impact in the pre-melt season is not taken into account. Painter et al., 2013 suggested that the rapid retreat of Alpine glaciers at the end of the Little Ice Age was forced by increasing BC concentration due to industrialisation. They found BC-induced mass balance anomalies in the order of $\sim$500 mm w.e. yr$^{-1}$ for the ablation area, which is similar to our results for the accumulation area ($\sim$180 to $\sim$300 mm w.e. yr$^{-1}$) despite the different modelling approaches. While Painter et al., 2013 used a sophisticated radiation model (SNICAR, Flanner et al., 2007) to derive BC radiative forcing and in turn equivalent changes in air temperature and mass balance, we used a simple broadband albedo parameterisation in combination with a mass balance model. However, Painter et al., 2013 assume 10 to 20 times higher BC concentrations than reported by the ice core data in order account for altitudinal differences between the high-altitude ice core sites and the ablation area. In our study, we do not alter atmospheric deposition rates (see Section 5.4), but, contrary to Painter et al., 2013, account for changes in the BC surface concentration due to melt and accumulation processes as well as to removal by melt water. As a result, we obtain similar BC concentrations in the surface layer on average and thus, a comparable impact of BC on glacier
mass balance. The general agreement of our assessment with that by Painter et al., 2007 indicates the highly relevant role of BC in shaping changes in glacier mass balance over the last century.

5.2 Sensitivity analysis

In order to assess the sensitivity of the model results to the chosen input parameters, we performed a sensitivity analysis. Four parameters of the snow impurity model were examined: (1) removal rates of BC by melt water, (2) fraction of Fe which is presented as Fe-oxides, (3) the proportion of haematite and goethite in the Fe-oxides, and (4) the ratio of the MAC of BC vs. MAC of Fe-oxides. In addition, another four parameters of the SSA model (SSA_{\text{ini}}, SSA_{\text{min}}, C_1, C_2) and six parameters of the snow density model (a_1, c_1, k_0, k_1, F_c, c, d) were investigated. Furthermore, we also assessed the importance of the amount-implications of deviating atmospheric deposition rates of mineral dust and BC in precipitation on the mass balance as the ice core date is taken from another site (see Section 5.4). The parameters of the melt and accumulation model were not included in the sensitivity analysis because they were directly constrained by the continuous seasonal mass balance measurements at the study sites. The sensitivity of the parameters was assigned by varying each parameter by 5% intervals around to the chosen value in a range of ±20%, keeping all other parameters constant. Tab. 1 shows the used parameter ranges. According to Anslow et al. (2008) we defined the sensitivity of a parameter as the slope around the origin of the curve, defined by the percentage change in the parameter value and the percentage change in the resulting model variable (mass balance in our case). For example a sensitivity of 0.5 designates that an arbitrary percentage change in the parameter value involves a half as large percentage change in the mass balance. A positive sensitivity means that an increase in the parameter value leads to an increase in the mass balance, a negative sensitivity that an increase in the parameter yields a decrease in mass balance.

Results of the sensitivity analysis are shown in Fig. 9. The mass balance was most sensitive to the amount of snow impurities and the parameters of the snow density model, while the parameters of the SSA model were clearly less relevant. In contrast to the input quantity of BC, mineral dust had a less pronounced impact on modelled mass balance. A change of 10% in the BC concentration in precipitation led to a 5.8% change in mass balance, whereas the same change in the mineral dust concentration in precipitation only resulted in a 1.6% change in mass balance. The reason for this difference in sensitivity is the stronger absorption of solar radiation by BC compared to mineral dust. An even higher sensitivity could be assigned to the removal efficiency of BC with melt water. A 10% change in the BC removal rate leads to a 1.5 times larger change in the mass balance. This is particularly important since the removal rates are subject to considerable uncertainty (see Section 5.5). Hence, the removal of BC by melt water seems to be the most critical point of the simulation and strongly controls the impact of BC on the long-term glacier mass balance. Besides the impurity model, also the performance of the density model affected the simulations. In particular, parameter k_0 (Eq. 11), describing the density change due to compaction, and the outflow parameter...
More efficient compaction in turn entails higher impurity concentrations in the surface snow layer and thus enhanced melt rates. The parameters of the SSA model show the lowest sensitivity and therefore are less relevant for the results. The two parameters, SSA_{min} and SSA_{initial} (Eq. 5), are the most sensitive ones. An increase in the two parameter values leads to a depletion in pure snow albedo, which slightly diminishes the impact on snow impurities. However, this effect is small compared to the other uncertainties.

5.3 Spatial distribution of the effect of light-absorbing impurities

The extent of the impact of Saharan dust and BC on the glacier mass balance is spatially variable and strongly depends on prevailing conditions. According to our results, the effect of light-absorbing impurities increase from the accumulation area towards the equilibrium line as higher melt rates lead to a re-exposure of old firn layers bearing light-absorbing impurities. In the ablation area where most glacier mass loss occurs, however, the processes are different. Winter accumulation is not preserved over multiple years and thus light-absorbing snow impurities affect only the albedo of the winter snow cover until it has been melted away. During the summer season when bare ice is exposed at the surface, snow impurities are removed by melt water which might limit the impact of impurities on glacier melt, although a darkening on gently-sloping glacier tongues has also been observed (Oerlemans et al., 2009). Hence, we suppose that the effect of Saharan dust and BC in the ablation area is lower compared to areas near the equilibrium line.

5.4 Transferring mineral dust/black carbon to Claridenfirn

Our analysis is based on the general assumption that concentrations of Saharan dust and BC in precipitation at Colle Gnifetti and Fiescherhorn (Fig. 1) are comparable to those at Claridenfirn. In order to receive undisturbed records of past aerosol concentrations only few sites in the Alpine region are suitable. Prerequisites are high elevation to exclude chemical disturbance by melt water percolation, sufficient ice thickness to ensure long enough records and flat terrain to limit the effect of ice flow (Wagenbach and Geis, 1989). For this reason we relied on time series at locations other than Claridenfirn and had to transpose the measurements to the study site for which long-term mass balance measurements were available.

In the 1990s a large-scale study about the chemical composition of high-alpine winter snow packs was carried out in the Alps with the aim of detecting the regional and altitudinal distribution of major ions (SNOSP; Nickus et al., 1997). It was found that the concentration of most ionic species in winter snow increases by about one third from west to east and that ionic loads show no regional preference due to opposite gradients in the prevailing precipitation patterns. The same also applies to variations with altitude: at higher elevation ion concentrations are lower compared to valleys, but the general
increase in precipitation with elevation compensates for this effect, so that ionic loads are expected to be in the same order of magnitude independent of absolute elevation. A more detailed investigation of selected sampling locations in the vicinity of Colle Gnifetti/Fiescherhorn (Breithorn, Gorner- /Theodulgletscher, Colle Vincent, Jungfraujoch) revealed that there is no distinct altitudinal trend in ionic loads (Nickus et al., 1997). A recent study about atmospheric deposition in alpine and subalpine areas confirms these results and concludes that there are no clear regional gradients, but a significant spatial variability of atmospheric ion deposition over the Alps (Rogora et al., 2006). Another study concluded that sites with large quantities of precipitation exhibit highest ion concentrations because they receive generally the first, more contaminated fraction of a precipitation event (Nickus et al., 1998).

The above mentioned studies are mainly focused on anthropogenic impurities of winter snow packs and can not be directly transferred to the situation at Claridenfirn. We suppose that concentrations at Claridenfirn might be higher than at Colle Gnifetti/Fiescherhorn due to (1) its eastern location, (2) the lower elevation and thus proximity to the polluted mixing layer, and (3) the higher precipitation rates (MeteoSwiss, 2014b). However, we are unable to conclude with certainty whether and to what extent ion concentrations differ between the ice cores and our study site. For these reasons we adopted the impurity concentrations measured at Colle Gnifetti/Fiescherhorn directly to the study site without a transfer function. Our assumption is supported by a supplementary analysis carried out on Claridenfirn. Kappenberger and Steingruber (2014) collected and analysed winter snow samples for major ions between 1995 and 2013. Comparison of bulk winter snow concentrations with those at Colle Gnifetti revealed that concentrations at both locations are in the same order of magnitude. In contrast to Saharan dust which is transported by large-scale upper air flows, BC concentrations are more influenced by the regional environment. Therefore, the assumption of using concentrations from a remote location might be less valid for BC than for Saharan dust. Actual BC input concentrations are thus subject to a higher uncertainty.

5.5 Removal by melt water

When a snowpack begins to melt, the insoluble snow impurities are partly retained and concentration of impurities in the surface snow increases as snow melt proceeds, thus reducing snow albedo. Consequently, melt is amplified and therefore provides a positive feedback on radiative forcing by light-absorbing impurities. To what extent snow impurities are removed by melt water percolation has not been fully clarified and only a small number of studies has addressed this issue so far. Important contribution is made by Conway et al. (1996), who found that particles of volcanic ash remained at or near the surface throughout the melting process while a large part of soot particles was flushed through the snow with the melt water. They suppose that the difference in the particle’s diameters is responsible for the different behaviour of ash and soot during the melting process. Doherty et al. (2013) concluded that removal rates due to melt water percolation of BC are in the order of 10–30 %
which is in agreement with the results by Conway et al. (1996). Based on the limited information available, a removal efficiency of 20% for BC seems to be a reasonable assumption. The sensitivity study indicated that the results are more sensitive on the removal rate than the amount of mineral dust and BC input. Hence, this issue needs further investigation. However, ignoring flushing-out of BC with melt would lead to an overestimation of surface concentrations and thus to an excessive melt amplification through BC (Doherty et al., 2013).

5.6 Mass balance model

The performance of the albedo parameterisation mainly depends on an accurate modelling of the specific surface area of snow grains and the fraction of snow impurities in the surface snow. Roy et al. (2013) demonstrate that the simulated snow grain sizes are in good agreement with measurements and that despite the simplicity of the SSA model results are comparable to well-established snow models (i.e. Crocus, Brun et al., 1989, 1992). The root-mean-square error in the overall SSA is $8.0 \text{ m}^2 \text{kg}^{-1}$ and corresponding to an albedo uncertainty in the order of ±3% for small grains and of ±6% for large grains. The main limitation of the SSA model is the performance during wet conditions due to the simplification regarding the 1-layer model for liquid water. As for the SSA model, the liquid water content is important also for the snow density model (De Michele et al., 2013). Snow density measurements, performed twice a year during the winter and late summer surveys on Claridenfirn, were used to validate the snow density model. Correlation of observed and simulated snow densities reveals a $r^2$ of 0.52 and 0.47. Mean absolute differences are 10.8 and 9.4 kg m$^{-3}$ (corresponding to a relative difference of ~2%) for the lower and upper measurement site, respectively. This indicates that the density model well captures the typical snow density, but does not fully reproduce interannual variability.

6 Conclusions

In this study we analysed the impact of Saharan dust and black carbon on the mass balance of an Alpine glacier over a centennial period (1914–2014) covered by exceptional observational data sets. A mass balance model including a parameterisation for albedo was combined with a snow density model in order to track snow layers and impurities over time. The combined model was forced with temperature and precipitation time series in daily resolution, the latter being assigned by mineral dust and BC concentrations retrieved from ice/firn cores.

On average the presence of Saharan dust at the glacier surface reduced mean annual albedo by less than 0.01. The associated decrease in the mean annual mass balance was 28–58 mm w.e. depending on the location on the glacier (accumulation area, equilibrium line). However, in individual years with very high supply of Saharan dust, surface albedo can be reduced substantially with a strong impact on snow and ice ablation. In addition to years with large atmospheric dust deposition, also
periods of strong melting may lead to significantly enhanced dust concentrations due to re-exposure of buried firn layers with a high impurity content. In contrast to mineral dust, BC affected the mass balance more efficiently and clearly dominated light absorption in snow except for years with large Saharan dust events. On average BC lowered the annual albedo by 0.03 and reduced the mean annual mass balance by 183–301 mm w.e. Due to the combined effect of BC and Saharan dust annual ablation on Claridenfirn was increased by 15–19% on average over 1914–2014 compared to pure snow conditions. In the accumulation area, the impact of Saharan dust and BC on the mass balance was clearly less pronounced due to the prevailing positive mass balances that tend to continuously bury snow impurities. The most sensitive parameter of our assessment is the removal rate of snow impurities by melt water, a process which is until now only poorly understood.

Our study demonstrates that the influence of snow impurities on glacier melting should be taken into consideration when modelling the mass balance of alpine glaciers over long-term periods in order to increase the reliability of the simulations. Particularly in years with large deposition of Saharan dust or BC and during periods with negative glacier mass balance, re-exposure of old firn layers can importantly impact on the rate of snow and ice ablation and thus enhance the albedo feedback. Furthermore, the study emphasizes the crucial role of BC in melt processes taking place on Alpine glaciers.
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Table 1. Parameters of the impurity, the SSA and the snow density model and the corresponding parameter ranges (+20%) applied in the sensitivity analysis.

<table>
<thead>
<tr>
<th>Parameter</th>
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<tr>
<td><strong>Impurity model</strong></td>
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<tr>
<td>Dust input</td>
<td>µg kg⁻¹</td>
<td>22.3</td>
<td>17.8 - 26.8</td>
</tr>
<tr>
<td>BC input</td>
<td>µg kg⁻¹</td>
<td>23.2</td>
<td>18.6 - 27.8</td>
</tr>
<tr>
<td>BC removal rate</td>
<td>%</td>
<td>20</td>
<td>16 - 24</td>
</tr>
<tr>
<td>Fe in FeO</td>
<td>%</td>
<td>54.5</td>
<td>43.6 - 65.4</td>
</tr>
<tr>
<td>MAC FeO/BC</td>
<td></td>
<td>0.082</td>
<td>0.066 - 0.099</td>
</tr>
<tr>
<td><strong>SSA model</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>SSA_initial</td>
<td>m² kg⁻¹</td>
<td>73.0</td>
<td>58.4 - 87.6</td>
</tr>
<tr>
<td>SSA_initial</td>
<td>m² kg⁻¹</td>
<td>8.0</td>
<td>6.4 - 9.6</td>
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<tr>
<td>C₁</td>
<td>10⁻³ mm³ d⁻¹</td>
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<td>0.88 - 1.32</td>
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<tr>
<td>C₂</td>
<td>10⁻⁵ mm³ d⁻¹</td>
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<td>2.96 - 4.44</td>
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<tr>
<td><strong>Snow density model</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>α₁</td>
<td>°C mm⁻¹</td>
<td>0.033</td>
<td>0.0264 - 0.0396</td>
</tr>
<tr>
<td>c₁</td>
<td>m² h⁻² kg⁻¹</td>
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<td>0.0008 - 0.0012</td>
</tr>
<tr>
<td>k₀</td>
<td>m³ kg⁻¹</td>
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<td>0.0168 - 0.0252</td>
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<tr>
<td>k₁</td>
<td>°C⁻¹</td>
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<tr>
<td>F₀</td>
<td></td>
<td>0.02</td>
<td>0.016 - 0.096</td>
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<tr>
<td>e</td>
<td>m⁻¹ h⁻¹(d⁻¹)</td>
<td>1.0</td>
<td>0.8 - 1.2</td>
</tr>
<tr>
<td>d</td>
<td></td>
<td>1.25</td>
<td>1.0 - 1.5</td>
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Figure 1. Study site overview. The red dots on Claridenfirn indicate the lower and the upper stake. The inset shows the location of the study site within Switzerland (red point), of the ice core sites Colle Gnifetti and Fiescherhorn (black dot). The aerosol measurement station Jungfraujoch and the weather stations used to derive meteorological time series (black triangles) are indicated.
Figure 2. (a) Concentrations of Fe (Sigl, 2009) and BC (inferred from EC; Jenk et al., 2006) over the period 1914–2014 retrieved from the Colle Gnifetti and Fiescherhorn ice core, respectively (Fig. 1). (b) Mean annual cycle of BC concentrations in the atmosphere measured by GAW at Jungfraujoch averaged over the years 1995–2000. Dots refer to the monthly means and the solid red line refers to the running mean.

Figure 3. Comparison of mean annual global radiation measured at Davos (bold grey, 1936–2014) and global radiation modelled by the cloud factor parameterisation (blue). The dashed black line shows annual averages of modelled daily radiation adjusted by the measurements to fit measured monthly means which are used to force the mass balance model.
Figure 4. Average Fe-oxide and BC concentrations in the surface snow at the upper and lower measurement site on Claridenfirn for the period 1914–2014. The crosses mark years with exceptionally high Saharan dust activity. Note that the scales for upper and lower stake are different.

Figure 5. Total Fe-oxide amount of the surface snow layer of each year and the amount of Fe-oxides of previous years emerging at the surface through melt-out over the period 1914–2014 for (a) the upper and (b) the lower stake. (c) and (d) illustrate the age of the oldest mineral dust present at the glacier surface for each year for both sites. Note that the scales for the upper and lower site are different.
Figure 6. Mean annual absorption (optical depth) of mineral dust and BC over the period 1914–2014 for (a) the upper and (b) the lower stake. The optical depth is calculated as product of mass absorption coefficient of BC/Fe oxides and the corresponding loading in the snow surface layer (top 2cm).

Figure 7. Cumulative mass balance over the period 1914–2014 at (a) the upper and (b) the lower measurement site. The solid blue line refers to the cumulative mass balance under real conditions (including Saharan dust and BC) and is consistent with the direct observations on Claridenfirn. The dash-dotted lines correspond to simulations (1) without Saharan dust (with BC), (2) without BC (but with Saharan dust), and (3) with pure snow conditions. The grey shaded area indicates the thickness of the entire firn column in m w.e.
**Figure 8.** Effect of Saharan dust on annual mass balance for the period 1914–2014 for (a) the upper and (c) the lower stake and the effect of BC for (b) the upper and (d) the lower stake. Bars show differences in annual mass balance between model results including or neglecting Saharan dust/BC. The dashed line refers the mean over the period 1914–2014 and the solid blue line to the 10 year average. Crosses mark years with exceptionally high Saharan dust activity.

**Figure 9.** Sensitivity of annual surface mass balance (i.e. the percentage change in the parameter value vs. the percentage change in annual mass balance) to the different parameters of the impurity, the specific surface area and the snow density model, as well as the sensitivity to the input of mineral dust and BC.