Verification of the multi-layer SNOWPACK model with different water transport schemes

N. Wever\textsuperscript{1,2}, L. Schmid\textsuperscript{1}, A. Heilig\textsuperscript{3}, O. Eisen\textsuperscript{3,4,5}, C. Fierz\textsuperscript{1}, and M. Lehning\textsuperscript{1,2}

\textsuperscript{1}WSL Institute for Snow and Avalanche Research SLF, Flüelastrasse 11, 7260 Davos Dorf, Switzerland
\textsuperscript{2}École Polytechnique Fédérale de Lausanne (EPFL), School of Architecture, Civil and Environmental Engineering, Lausanne, Switzerland
\textsuperscript{3}Institute of Environmental Physics, University of Heidelberg, Heidelberg, Germany
\textsuperscript{4}Alfred Wegener Institute Helmholtz Centre for Polar and Marine Research, Bremerhaven, Germany
\textsuperscript{5}University Bremen, Bremen, Germany

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Correspondence to: N. Wever (wever@slf.ch)

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Abstract

The widely-used detailed SNOWPACK model has undergone constant development over the years. A notable recent extension is the introduction of a Richards Equation (RE) solver as an alternative for the bucket-type approach for describing water transport in the snow and soil layers. In addition, continuous updates of snow settling and new snow density parametrisations have changed model behaviour. This study presents a detailed evaluation of model performance against a comprehensive multi-year data set from Weissfluhjoch near Davos, Switzerland. The data set is collected by automatic meteorological and snowpack measurements and manual snow profiles. During the main winter season, snow height (RMSE: <4.2 cm), snow water equivalent (SWE, RMSE: <40 mm w.e.), snow temperature distributions (typical deviation with measurements: < 1.0 °C) and snow density (typical deviation with observations: < 50 kg m\(^{-3}\)) as well as their temporal evolution are well simulated in the model and the influence of the two water transport schemes is small. The RE approach reproduces internal differences over capillary barriers but fails to predict enough grain growth since the growth routines have been calibrated using the bucket scheme in the original SNOWPACK model. The agreement in both density and grain size is sufficient to parametrise the hydraulic properties. In the melt season, a more pronounced underestimation of typically 200 mm w.e. in SWE is found. The discrepancies between the simulations and the field data are generally larger than the differences between the two water transport schemes. Nevertheless, the detailed comparison of the internal snowpack structure shows that the timing of internal temperature and water dynamics is adequately and better represented with the new RE approach when compared to the conventional bucket scheme. On the contrary, the progress of the meltwater front in the snowpack as detected by radar and the temporal evolution of the vertical distribution of melt forms in manually observed snow profiles do not support this conclusion. This discrepancy suggests that the implementation of RE partly mimics preferential flow effects.
1 Introduction

The one-dimensional physics based snowpack model SNOWPACK (Lehning et al., 2002a, b) has been used in many studies to assess various aspects of the snow cover. Recently, the model has been extended with a solver for Richards Equation (RE) in the snowpack and soil, which improved the simulation of liquid water flow in snow from the perspective of snowpack runoff compared to a conventional bucket type approach (Wever et al., 2014). In this study, a comparison of snowpack runoff measured by a snow lysimeter with modelled snowpack runoff showed a higher agreement when simulating liquid water flow with RE, especially on the sub-daily time scale. Additionally, the arrival of meltwater at the base of the snowpack in spring was found to be better predicted. However, these results were solely based on an analysis of liquid water outflow. The study raised questions to what extend the two water transport schemes differ in the simulation of the internal snowpack structure and whether the improvements in snowpack runoff estimations with RE are also consistent with simulations of the internal snowpack.

For many applications, especially in hydrological studies, the primary variables of interest are snow water equivalent (SWE) and snowpack runoff, as the first provides possible future meltwater and the latter provides the liquid water that directly participates in hydrological processes. In spite of its importance, direct measurements of SWE are relatively sparse. In contrast, snow height measurements are relatively easy to obtain either manually or automatically, and long climatological records of snow height are available. Methods have been developed to relate snow height to SWE (Jonas et al., 2009; Sturm et al., 2010). Snow density is another parameter that is variable in time and space (Bormann et al., 2013) and rather cumbersome to measure in the field. Although it is seldom of primary interest, it may serve wide applications as an intermediate parameter between a property that is observed and a property that one is interested in. For example, proper estimates of snow density will increase the accuracy of translating snow height to SWE. Snow density is also required for the conversion of measured...
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Two-way travel time (TWT) from radar applications to snow depth in dry-snow conditions (Gubler and Hiller, 1984; Lundberg and Thunehed, 2000; Marshall et al., 2007; Heilig et al., 2009, 2010; Okorn et al., 2014) or translating dielectric measurements to liquid water content, as for example with the Snow Fork (Sihvola and Tiuri, 1996), or the Denoth meter (Denoth, 1994).

Apart from bulk snowpack properties, there is also a demand for detailed snowpack models to assess the layering and microstructural properties of the snowpack, for example with the purpose of avalanche forecasting. Layer transitions within the snow cover with pronounced contrasts in for example density, grain shape or grain size can act as zones in which fractures can be initialized and slab avalanches release (Schweizer et al., 2003). The presence of liquid water can reduce the strength of a snowpack considerably (Colbeck, 1982; Conway and Raymond, 1993), for which Techel et al. (2011) showed a grain shape dependence. When snowpack models are used to understand wet snow avalanche formation, it is important that the model can reproduce capillary barriers, at which liquid water may pond (Schneebeli, 2004; Baggi and Schweizer, 2009; Hirashima et al., 2010; Mitterer et al., 2011b). Also the arrival of meltwater at the bottom of the snowpack is considered to be a good indicator for the onset of wet snow avalanche activity. However, reliable liquid water content (LWC) measurements for the snowpack are difficult to obtain. Some attempts for continuous monitoring are promising (Schmid et al., 2014; Koch et al., 2014; Avanzi et al., 2014), but are not yet operational. Recently, Mitterer et al. (2011a) and Schmid et al. (2014) demonstrated the potential of upward-looking ground-penetrating radar (upGPR) to monitor the progress of the meltwater front and Heilig et al. (2015) present data for quasi continuous observations of bulk liquid water content over several years and for three different test sites. Here, their results concerning the position of the meltwater front will be compared with snowpack simulations. We also consider temperature measurements taken during manual snow profiling as a reliable and precise way to determine which part of the snowpack has become at melting point (often termed isoother-
mal) and likely contains a fraction of liquid water due to infiltration (i.e. the movement of liquid water in snow) or local snowmelt.

As with snow density, snow temperatures are rarely of primary interest in snow studies. However, a correct representation of the temperature profile of the snowpack is required, as it has a large influence on the snow metamorphism (grain shape and size) and settling rates (Lehning et al., 2002a). Temperature gradients drive moisture transport and have a strong influence on the grain growth (Colbeck, 1982; Pinzer et al., 2012; Domine et al., 2013). Furthermore, temperature profiles are an indicator of whether the combination of the surface energy balance, the ground heat flux, and the internal heat conductivity of the snowpack is correctly approximated.

In this study, the SNOWPACK model is driven by measurements from an automated weather station at Weissfluhjoch (WFJ) near Davos, Switzerland. Simulations are extensively verified for several bulk properties of the snowpack and against snow profiles made at WFJ, with the aim to verify the representation of the internal snowpack structure. Time series of soil and snow temperatures, snow lysimeter measurements and upGPR data from WFJ are used to validate snowpack temperature profiles, snowpack runoff and the progress of the meltwater front within the snowpack in the simulations. This study focusses on snowpack variables that are influenced by liquid water flow with the aim of a more in-depth comparison of differences between RE and the conventional bucket scheme. The comparison is limited to snow height, SWE, liquid water runoff from the snow cover, snow density, snow temperature, and grain size and shape, as for these variables, validation data are available. Internally, the SNOWPACK model also uses additional state variables, like sphericity, dendricity and bond size (Lehning et al., 2002a).

2 Theory

The theoretical basis of the SNOWPACK model regarding the heat advection equation and snow settling has been discussed in Bartelt and Lehning (2002). The treatment
of the snow microstructure and several parametrisations, as for example for snow viscosity, snow metamorphism and thermal conductivity, are presented in Lehning et al. (2002a). Some of those parametrisations have been refined in later versions of SNOWPACK. The treatment of the meteorological forcing for determining the energy balance at the snow surface is discussed in Lehning et al. (2002b). Finally, the liquid water transport schemes are presented and verified in Wever et al. (2014). Here, we will outline theoretical aspects not discussed in the aforementioned literature.

2.1 Water retention curves

To solve RE, the water retention curve and the saturated hydraulic conductivity \(K_{\text{sat}}\) (m s\(^{-1}\)) need to be specified. For the water retention curve, the van Genuchten model is used (van Genuchten, 1980). It uses several parameters: residual water content \(\theta_r\) (m\(^3\) m\(^{-3}\)), saturated water content \(\theta_s\) (m\(^3\) m\(^{-3}\)) and parameters \(\alpha\) (m\(^{-1}\)), \(n\) (–) and \(m\) (–). For the soil part, the ROSETTA class average parameters (Schaap et al., 2001) are implemented to provide these parameters for various soil types.

For snow, the parametrisation for \(\alpha\) in the van Genuchten model as proposed by Yamaguchi et al. (2010) reads:

\[
\alpha = 7.3(2r_g) + 1.9, \quad (1)
\]

where \(2r_g\) is the classical grain size (m), which is defined as the average maximum extent of the snow grains (Fierz et al., 2009). For \(n\), the original parametrisation by Yamaguchi et al. (2010) was modified by Hirashima et al. (2010) to be able to extend the parametrisation beyond grain radii of 2 mm:

\[
n = 15.68e^{(-0.46(2r_g))} + 1. \quad (2)
\]

Here, we will abbreviate this parametrisation of the water retention curve as Y2010. This parametrisation has been used in Wever et al. (2014).
The Y2010 parametrisation was determined for snow samples with similar densities. In Yamaguchi et al. (2012), an updated set of experiments was described for a wider range of snow density and grain size, leading to the following parametrisation of the van Genuchten parameters:

\[
\alpha = 4.4 \cdot 10^6 \left( \frac{\rho}{2r_g} \right)^{-0.98},
\]

and

\[
n = 1 + 2.7 \cdot 10^{-3} \left( \frac{\rho}{2r_g} \right)^{0.61},
\]

where \( \rho \) is the dry density of the snowpack (kg m\(^{-3}\)). This parametrisation will be referred to as Y2012. Both parametrisations will be compared here. \( \theta_r \) and \( \theta_s \) are defined as described in Wever et al. (2014) and \( K_{sat} \) is parametrised following Calonne et al. (2012):

\[
K_{sat} = \left( \frac{\rho_w g}{\mu} \right) \left[ 0.75 \left( \frac{r_{es}}{1000} \right)^2 \exp(-0.013\theta_i \rho_{ice}) \right],
\]

where \( \rho_w \) and \( \rho_{ice} \) are the density of water (1000 kg m\(^{-3}\)) and ice (917 kg m\(^{-3}\)), respectively, \( g \) is the gravitational acceleration (taken as 9.8 m s\(^{-2}\)), \( \mu \) is the dynamic viscosity (taken as 0.001792 kg (m s\(^{-1}\))), \( \theta_i \) is the volumetric ice content (m\(^3\) m\(^{-3}\)) and \( r_{es} \) is the equivalent sphere radius (m), approximated by the optical radius, which in turn can be parametrised using grain size, sphericity and dendricity (Vionnet et al., 2012).

In both parametrisations and for soil layers, the van Genuchten parameter \( m \) is chosen as:

\[
m = 1 - (1/n),
\]
such that the Mualem-model for the hydraulic conductivity in unsaturated conditions has an analytical solution (van Genuchten, 1980). We correct the water retention curve using the approach by Ippisch et al. (2006) for taking into account the air entry pressure. As in Wever et al. (2014), an air entry pressure of 0.0058 m was used, corresponding to a largest pore size of 5 mm.

The method to solve RE requires the calculation of the hydraulic conductivity at the interface nodes. It is common to take the arithmetic mean (denoted AM) of the hydraulic conductivity of the adjacent elements, although other calculation methods have been proposed (e.g., see Szymkiewicz and Helmig, 2011). Here, we compare the default choice of AM with the geometric mean (denoted GM), as proposed by Haverkamp and Vauclin (1979), to investigate the possible influence of the choice on averaging method on the simulations of liquid water flow.

### 2.2 Soil freezing and thawing

Due to the isolating effects of thick snow covers and the generally upward directed soil heat flux, soil freezing at WFJ is mostly limited to autumn and the beginning of the winter, when the snow cover is still shallow. To solve phase changes in soil, we follow the approach proposed by Dall’Amico et al. (2011). They express the freezing point depression in soil as a function of pressure head as:

\[
T^* = T_{\text{melt}} + \frac{gT_{\text{melt}}}{L} h,
\]

where \(T^*\) is the melting point of the soil water (K), \(T_{\text{melt}}\) is the melting temperature of water (273.15 K), \(L\) is the latent heat associated with the phase transition from ice to water (334 kJ kg\(^{-1}\)) and \(h\) is the pressure head (m).

When the soil temperature \(T\) (K) is at or below \(T^*\), the soil is in freezing or thawing state. Then, the pressure head associated with liquid water \(h_w\) (m) can be expressed...
as:

\[ h_w = h + \frac{L}{g T^*} (T - T^*), \]  

(8)

where \( h \) is the total pressure head of the soil (m). The van Genuchten model provides the relationship between pressure head and LWC:

\[ \theta = \theta_r + (\theta_s - \theta_r) \left( 1 + (\alpha |h_w|)^n \right)^{-m} \frac{1}{Sc}, \]  

(9)

where \( \theta \) is the volumetric LWC (m\(^3\) m\(^{-3}\)). Consequently, the ice part can be expressed as:

\[ \theta_i = \theta_r + (\theta_s - \theta_r) \left( 1 + (\alpha |h|)^n \right)^{-m} \frac{1}{Sc} - \theta, \]  

(10)

where \( Sc \) is the correction proposed by Ippisch et al. (2006).

In Dall’Amico et al. (2011), a splitting method is introduced to solve both the heat advection equation and RE for liquid water flow in a semi-coupled manner. We approach the problem by finding the steady state solution for \( T, \theta \) and \( \theta_i \) in Eqs. (8), (9) and (10). This steady state solution is found numerically by using the Bisect–Secant method (Dekker, 1969), where the starting points for the method are taken as all ice melting and all liquid water freezing, respectively. In soil, liquid water flow can advect heat when a temperature gradient is present. In the soil module of SNOWPACK, heat advection associated with the liquid water flow is calculated after every time step of the RE solver, before assessing soil freezing and thawing.
3 Data and methods

3.1 Data (1): meteorological time series

The SNOWPACK model is forced with a meteorological data set from the experimental site Weissfluhjoch (WFJ) at an altitude of 2540 m in the Swiss Alps near Davos. This measurement site is located in an almost flat part of a south-easterly oriented slope. During the winter months, a continuous seasonal snow cover builds up at this altitude. The snow season is defined here as the main consecutive period with a snow cover of at least 5 cm on the ground during the winter months, and is denoted by the year in which they end. The snow season at WFJ generally starts in October or November and lasts until June or July.

The data set contains air temperature, relative humidity, wind speed and direction, incoming and outgoing longwave and shortwave radiation, surface temperature, soil temperature at the interface between the snowpack and the soil, snow height, and precipitation from a heated rain gauge (Marty and Meister, 2012; Schmucki et al., 2014). An undercatch correction is applied for the measured precipitation (Wever et al., 2014). Snow temperatures are measured at 50, 100 and 150 cm above the ground surface, using vertical rods placed approximately 30 cm apart. From September 2013 onwards, soil temperatures are measured at 50, 30 and 10 cm depth. The experimental site is also equipped with a snow lysimeter with a surface area of 5 m$^2$, as described in Wever et al. (2014). The rain gauge and snow lysimeter are measuring at an interval of 10 min, whereas most other measurements are done at 30 min intervals.

In the area surrounding WFJ, field data to validate soil freezing and thawing are lacking. For modelling the snowpack, the most important influence of the soil is the heat flux that is provided at the lower boundary of the snowpack. For this purpose, we will use the temperature measured at the interface between the soil and the snowpack to validate the soil module. This temperature measurement is influenced by soil freezing and thawing. Our primary interest here is the investigation to what degree the previ-
ously described soil module of SNOWPACK is capable of providing a realistic lower boundary for the snowpack in the simulations.

SNOWPACK can be forced with either measured precipitation amounts or with measured snow height. In precipitation-driven simulations (Precip driven), measured precipitation is assumed to be snowfall when the air temperature is below 1.2°C and rain otherwise. For these type of simulations, the study period is from 1 October 1996 to 1 July 2014 (1 week after melt out date), consisting of 18 full snow seasons. In case of snow height-driven simulations (HS driven), an additional threshold for relative humidity and a maximum value for the temperature difference between the snow surface and the air is used to determine whether snowfall is possible. Then, snowfall is assumed to occur when measured snow height is exceeding the modelled snow height (Lehning et al., 1999), in combination with a parametrisation for new snow density (Schmucki et al., 2014). In both modes, new snow layers are added for each 2 cm of new snow. An uninterrupted, consistent dataset for this type of simulations is available from 1 October 1999 to 1 July 2014, consisting of 15 full snow seasons. The last snow season (2014) of the studied period has the most data available and will be used as the example snow season to explain how SNOWPACK simulates the snow cover. Results for the other snow seasons are included in the online Supplement.

Many processes in SNOWPACK are based on physical descriptions that require calibration, for example for wet and dry snow settling, thermal conductivity and new snow density. For this purpose, dedicated datasets with some additional detailed snowpack measurements from snow seasons 1993, 1996, 1999 and 2006 have been used when constructing the model. Snow metamorphism processes were mainly calibrated against laboratory experiments (Baunach et al., 2001).

3.2 Data (2): manual snow profiles

Every two weeks, around the 1st and 15th of each month respectively (depending on weather conditions), a manual full depth snow profile is taken at the WFJ, following the guidelines from Fierz et al. (2009). Measurements include snow temperature at
a resolution of 10 cm, and snow density in steps of approximately 30 cm. Density is determined by taking snow cores using a 60 cm high aluminium cylinder with a cross-sectional area of 70 cm² and weighting the snow core using a calibrated spring. SWE is determined from these density measurements. For comparison with the simulations, SWE values are corrected for differences in snow height at the snow pit and at the automatic weather station, to eliminate the effect of spatial variability. Grain size (following the classical definition of average maximum extent of the snow grains) and grain shape are evaluated by the observer using a magnifying glass. The snow profiling is carried out in the morning hours, starting around 09:00 LT.

3.3 Data (3): upward-looking ground-penetrating radar

An upGPR is located within the test site at a distance of approximately 20 m from the meteorological station (Mitterer et al., 2011a; Schmid et al., 2014). The upGPR is buried in the ground with the top edge level to the ground surface and points skyward. The radar instrument and data processing is described in Schmid et al. (2014). Measurement intervals for all observed melt seasons were set to 30 min during daytime. The only difference in the processing scheme applied for this study in comparison to Schmid et al. (2014) is that for an optimized retrieval of the dry-wet transition within the snow cover, we reduced the length of the moving-window time filter to a few days (1–3) instead of six weeks. Since percolating water results in strong amplitude increases at the respective depth of percolation and a decrease in wave speed for electromagnetic waves travelling through wet layers, we searched for occurrences of sharp amplitude contrasts together with diurnal variations in the location of signal responses of the overlying layers. For snow layers in which liquid water is appearing during the day and refreezing during the night, or when LWC reduces through outflow, a clear diurnal cycle in two-way travel time (TWT) of the respective signal reflections can be observed. Schmid et al. (2014) describe first attempts to determine percolations depths automatically within the recorded radargrams. For this study, we manually determined all observations of the dry-wet transition in the snowpack and converted TWT in height
above the radar by assuming a constant wave speed in dry snow of 0.23 m·ns$^{-1}$ (Mitterer et al., 2011a; Schmid et al., 2014). Data on liquid water percolation measured with upGPR have been presented in Schmid et al. (2014) for the snow seasons 2011 and 2012. Here, we present data of two more snow seasons (2013, 2014) and compare all measured depths of the dry-wet transition with simulation results. In snow seasons 2011, 2013 and 2014, additional snow profiles were made in close proximity of the upGPR, with a higher frequency during the melt season than the regular snow profiles discussed in the previous section.

3.4 Methods (1): model setup

For the simulations in this study, the SNOWPACK model is solving the energy balance at the snow surface. The turbulent fluxes are calculated using the stability correction functions as in Stössel et al. (2010). This is an adequate approximation for most of the snow season, when the snow surface cooling due to net outgoing long wave radiation is causing a stable stratification of the atmospheric boundary layer. The surface albedo is calculated from the ratio of measured incoming and reflected shortwave radiation. The net longwave radiation budget is also calculated from the difference in measured incoming and outgoing long wave radiation. The aerodynamic roughness length ($z_0$) of the snow is fixed to 0.002 m.

The soil at WFJ consists of coarse material with some loam content, as was observed when installing the soil temperature sensors. The ROSETTA class average parameters for the loamy sand class are taken for the van Genuchten parametrisation of the water retention curve for the soil ($\theta_r = 0.049$ m$^3$ m$^{-3}$, $\theta_s = 0.39$ m$^3$ m$^{-3}$, $\alpha = 3.475$ m$^{-1}$, $n = 1.746$, $K_{sat} = 1.2176 \cdot 10^{-5}$ m·s$^{-1}$). For the thermodynamic properties, the specific heat for the soil constituents was set to 1.0 kJ·kg$^{-1}$·K$^{-1}$ and the heat conductivity to 0.9 W·m$^{-1}$·K$^{-1}$. The total soil depth in the model is taken as 3 m, with a variable layer spacing of 1 cm in the top layers and 40 cm for the lowest layer. The dense layer spacing in the top of the soil is necessary to describe the large gradients
in soil moisture and temperature occurring here. At the lower boundary, a water table is prescribed, together with a Neumann boundary condition for the heat advection equation, simulating a constant geothermal heat flow of 0.06 W m\(^{-2}\).

All simulations are run on the same desktop computer as a single-core process, using a model time step of 15 min. In the solver for RE, the SNOWPACK time step may be subdivided in smaller time steps when slow convergence is encountered (Wever et al., 2014). The computation time is in the order of a few minutes per year, where RE takes about twice as much time as the bucket scheme (Wever et al., 2014). Checks of the overall mass and energy balance reveal that the mass balance for all simulations is satisfied well within 1 mm w.e. and the energy balance error is generally around 0.05 W m\(^{-2}\) (see Table 1). We consider these errors to be well acceptable for our purpose.

3.5 Methods (2): analysis

The analysis of the simulations is done per snow season, ignoring summer snowfalls. The snow season at the WFJ is characterized by an early phase at the end of autumn or beginning of winter, when the snow cover is still relatively shallow and occasionally melt or rain-on-snow events are occurring. End of November to mid March can be defined as the accumulation period, in which snowpack runoff is virtually absent and the snowpack temperature is below freezing. This implies that in this period, all precipitation is added to the snow cover as solid mass, either by rain refreezing inside the snowpack, or by snowfall. Small amounts of snowmelt occurring near the surface refreeze during night or, after infiltration, inside the snowpack. Therefore, the increase in SWE between the biweekly profiles can be used to verify the undercatch correction in case the SNOWPACK model is driven with measured precipitation from the heated rain gauge, or to verify the combined effect of parametrised new snow density and snow settling in case snow height is used to derive snow fall amounts. The final phase is the melting phase, starting in April in most snow seasons, when the snowpack is isothermal and wet and produces snowpack runoff.
The snow temperature sensors may be influenced by penetrating shortwave radiation in the snowpack. Therefore, snow temperature measurements are only analysed when the measured snow height is at least 20 cm above the height of the sensor. Comparing snow temperatures between snow seasons was done by first standardising the measurement time of the temperature series between 0 and 1, for the start and end of the snow season, respectively. Then the data were binned in steps of 0.01 and bin averages were calculated. These series were then used for calculating the average and SD of differences between snow seasons. The same procedure was followed for snow height.

To compare manual snow profiles with the model simulations, several processing steps are required (Lehning et al., 2001). The snow height at the snow pit is generally different from the simulated snow height. This is not only due to the model not depicting the snowpack development perfectly but also because the snow pit is made at some distance from the snow height sensor which is used to drive the simulations. Therefore, we scale the simulated profile to the observed profile by adjusting each layer thickness, without adjusting the density. This implies that mass may be added or removed from the modelled domain. Then, the model layers are aggregated to match the number and thickness of the layers in the observations. Model layers are assigned to observed layers based on the centre height of the model layer. The typical thickness of a model layer is around 2 cm, so possible round-off errors are expected to be small. For temperature, the matching with modelled layer temperatures is achieved by linear interpolation from the measured temperature profile to the centre point of the modelled layer.

The cold content of the snowpack is the amount of energy necessary to bring the snowpack to 0°C, after which an additional energy surplus will result in net snowmelt. The total cold content \( Q_{cc} \) (J m\(^{-2}\)) of the snowpack is defined in discrete form as the sum of the cold content of each layer:

\[
Q_{cc} = \sum_{i=1}^{n} \rho_i c_i \Delta z_i (T_i - T_{\text{melt}}),
\]  

(11)
where \( i \) is an index to a snow layer, \( n \) is the number of snow layers in the domain, \( \rho_i \) is the density of the layer (kg m\(^{-3}\)), \( c_i \) is the specific heat of the layer (J kg\(^{-1}\) K\(^{-1}\)), \( \Delta z_i \) is the layer thickness (m) and \( T_i \) is the temperature of the layer (K). The cold content is calculated for both the observed and modelled profiles, where the modelled profile is first aggregated onto the observed layer spacing with the procedure described above.

4 Results and discussion

4.1 Snow height and snow water equivalent

Figure 1 shows the snow height for several simulation setups. Per construction, the snow height-driven simulations provide a high degree of agreement between measured and modelled snow height. The general tendency of the precipitation-driven simulations is to follow the measured snow height, although it can be clearly seen that some precipitation events are overestimated, whereas others are underestimated. These differences are caused by inaccuracies when measuring solid precipitation with a rain gauge (Goodison et al., 1998), imperfections in the undercatch correction, or the effect of aeolian wind transport causing either erosion or accumulation of snow at the measurement site. As snow drift is mainly occurring close to the surface, the rain gauge is rather insensitive to these effects as its installation height is higher than the typical depth of a drifting snow layer. On the other hand, at WFJ, snow drift is expected to play a relatively small role.

As listed in Table 1, the RMSE of snow height for all simulated snow seasons is significantly larger for precipitation-driven simulations than for snow height-driven ones. Furthermore, the difference between measured and modelled snow height tends to be negative, denoting an underestimation of snow height by the model. In the Supplement Figs. S1 and S2, snow height for the various model setups is shown for each snow season. Typical year-to-year variability of inconsistencies in the precipitation-driven simulations are present, whereas the snow height-driven simulations follow the measured
snow height more closely. In Fig. 2, the average snow height difference is shown for all simulated snow seasons, relative to the standardized date in the snow season. It shows that the underestimation of the snow height is occurring mainly near the end of the snow season, thus during the melt season. This does not necessarily imply that the melt rates are overestimated, as snow height is the combined result of snow accumulation, settling and melt.

SWE is generally a better indicator of snow accumulation and snowmelt than snow height. A comparison between observed SWE in manual profiles and modelled SWE (Fig. 3a) shows that the agreement between both is high. The linear fits to the data points show that on average, the prediction of SWE in the model is accurate, for both snow height and precipitation-driven simulations. The scatter is larger for precipitation-driven simulations and there seems to be an underestimation of low SWE values and an overestimation of high ones.

The modelled SWE is a result of several effects: (i) snowfall amounts, which rely on an accurate estimation of new snow density in case of snow height-driven simulations or an adequate undercatch correction in case of precipitation-driven simulations, (ii) snow settling, in case of snow height-driven simulations, (iii) snowmelt and (iv) liquid water flow in snow and subsequent snowpack runoff. To separate the effects of liquid water flow and snowpack runoff from the other effects, Fig. 3b shows the increase in SWE in biweekly profiles during the accumulation phase of the snow season at the WFJ, when only factors (i), (ii), and (iii) are playing a role. The snow height-driven simulations are on average providing a high degree of agreement with the measured increase in SWE during the accumulation phase, with only a marginal difference between the bucket scheme and RE. Here, it needs to be mentioned that in snow height-driven simulations, the snow settling formulation is able to compensate for errors in the estimation of new snow density and vice versa. For example: when new snow is initialized with a too high density, and thus too much mass is added, the snow settling will be underestimated and consequently, the next snow fall amount is also underestimated. Because the snowfall amounts in precipitation-driven simulations are independent of
the settling of the snow cover, the increases in SWE are independent of the predicted settling. The results show that in the accumulation phase, the combined effect of new snow density and snow settling is providing a slightly underestimated SWE increase, whereas the opposite is found for precipitation-driven simulations.

Figure 4 shows the difference in SWE between model simulations and the snow profiles for all simulated snow seasons. The difference in snow height-driven simulations is rather small, compared to precipitation-driven simulations. All simulations show that in the melt phase, the model underestimates SWE. This points towards either an overestimation of melt rates, or a too early release of meltwater at the base of the snowpack, or a combination of both. The fact that the discrepancies for the precipitation-driven simulations are larger than for the snow height-driven ones, is related to the underestimation of snow height during the melt phase. In the snow height-driven mode, an overestimated decrease in snow height during snowmelt is compensated for by a continuous adding of fresh snow in case the snowfall conditions are met.

4.2 Liquid water content and snowpack runoff

Figure 5a and b show the distribution of liquid water within the snowpack for the example snow season 2014 for the bucket scheme and RE, respectively. Here, liquid water is present during the beginning of the snow season and during the melt season, which is a typical pattern for WFJ. The simulations with RE show a quicker downward routing of meltwater from the surface, where the meltwater is produced, than the simulations with the bucket scheme. Furthermore, the latter provides a rather homogeneous LWC distribution throughout the snowpack, except for the lighter surface elements, where LWC is significantly higher. A diurnal cycle is not visible in the simulations, except for layers close to the surface. With RE, there is both a strong variation in the vertical direction as well as in time. Marked accumulations of liquid water can be seen at transitions between layers with different characteristics. These accumulations peak to around 10 % LWC and are occurring during the first wetting of the snowpack and above capillary barriers inside the snowpack. Natural snow covers show such high LWC as
well (e.g., Techel and Pielmeier, 2011), and this is considered to contribute to wet snow avalanche formation (Schneebeli, 2004; Baggi and Schweizer, 2009). This effect is particularly present during the first wetting, as later in the melt season, wet snow metamorphism reduces the contrast between microstructural properties. Furthermore, the increase in hydraulic conductivity when the snowpack below the capillary barrier gets wet, reduces its function as a barrier. RE also introduces a strong diurnal cycle in LWC in the simulations. The results for other snow seasons can be found in the Supplement Figs. S3–S5, and they illustrate that the differences occurring between both water transport schemes in the example snow season are consistent for the other snow seasons as well.

Direct comparison of these model results with measurements is difficult, as continuous, non-destructive observations of the vertical distribution of LWC are not available. However, snowpack runoff is strongly coupled to the LWC distribution. Snowpack runoff at the measurement site WFJ is typically occurring in the melt season and in some snow seasons during autumn when early snow falls may be alternately followed by short melt episodes or rain-on-snow events. This is illustrated by the cumulative runoff curves in the Supplement Figs. S6 and S7. Table 1 shows the ratio of modelled to measured snowpack runoff. Snowpack runoff from precipitation-driven simulations is on average 2% less than observed, whereas snow height-driven simulations show about 8–14% more runoff than is observed. From the snow height-driven simulations, simulations with RE again have higher runoff sums than the simulations with the bucket scheme. This behaviour is found in most simulated snow seasons, as shown by Fig. S8 in the Supplement. The overestimation of total runoff in snow height-driven simulations is caused by the previously described mechanism where the snow height-driven simulations add snow layers in spring when the snow height decrease is overestimated. The approach is inadequate during the melt season, as these new snow layers have low densities compared to the rest of the snowpack and snow settling will quickly reduce the modelled snow height again below the measured one. As the wet snow settling is a little stronger when using RE, this effect is slightly larger for those simulations.
A common measure to quantify the agreement between measured and modelled snowpack runoff is the Nash-Sutcliffe model efficiency (NSE, Nash and Sutcliffe (1970)), which is shown in Table 1 and Figs. S9 and S10 in the Supplement for completeness. Further discussion can be found in Wever et al. (2014). NSE coefficients increase for simulations with RE, especially on the 1 hour time scale, as well as the $r^2$ value. The NSE coefficients and $r^2$ values tend to be lower for precipitation-driven simulations than for snow height-driven ones, especially in the simulations with RE. This likely is a result of a more accurate prediction of percolation time of liquid water through the snowpack in snow height-driven simulations. This is also indicated by the difference in time lag correlation (see Table 1) between precipitation-driven simulations and snow height-driven ones. The best timing of snowpack runoff on the hourly time scale is achieved with snow height-driven simulations with RE.

4.3 Soil temperatures

At WJF, soil temperatures are available at three depths, but only for the last snow season in this study (see Fig. 6a). The simulated soil temperatures are satisfactory simulated, although the soil never showed temperatures well below 0°C. This indicates that no significant soil freezing occurred, limiting the usefulness of these data to validate the new soil module. However, it is primarily important for this study that the soil as modelled by SNOWPACK serves as an adequate lower boundary condition for the snowpack simulations. For this purpose, we examine the soil temperature in the topmost soil part at the snow–soil interface, which is available for the snow seasons 2000–2014 (see Fig. 6b). For most of the time when a snow cover is present, the interface temperature at the snow–soil interface is close to 0°C, except in the beginning of the snow season when the snow cover is still shallow. This is common for deep alpine snowpacks due to the isolating effect of thick snow covers and the generally upward directed soil heat flux. Figure 6b shows that the simulations capture the variability in early season soil–snow interface temperature to a high degree in most years.
4.4 Snow temperatures

Figure 7a and b show the simulated temperature distribution within the snowpack for the example snow season 2014 for the bucket scheme and RE, respectively. The other snow seasons are shown in the Supplement Figs. S11–S13. For each snow season, the snowpack temperature at WFJ is below freezing for an extended period of time and for these periods, no noticeable differences are found between simulations with the bucket scheme or RE. As a result of the differences in liquid water flow depicted in Fig. 5a and b, the parts of the snowpack that are isothermal differ significantly. Table 1 shows that the $r^2$ value between the relative part of the snowpack that is isothermal, as determined from measurements in the observed snow profiles and from the simulated ones, increases from 0.74 to 0.87 when solving liquid water flow with RE.

The temperature distribution of the snowpack is strongly related to the combination of the net energy balance of the snowpack and snow density. The latter influences the snow temperature through the thermal inertia of dense snow layers and through the strong dependence of density on thermal conductivity (e.g., Calonne et al., 2011). Errors in either the energy balance or snow density may result in errors in snow temperatures. The cold content of the snowpack may be considered a more robust method to verify the simulated energy balance of the snow cover. Table 1 shows that the RMSE in cold content in the snow height-driven simulations is larger for the bucket scheme than RE, with a RMSE of around 670 kJm$^{-2}$, which is equivalent to 2 mm w.e. snowmelt. This shows that the estimation of cold content in the simulations is adequate when, for example, estimating the onset of snowmelt and refreezing capacity inside the snowpack. Larger RMSE for precipitation-driven simulations can be associated with the larger discrepancy between measured and modelled snow height. The bias in the cold content is small compared to the RMSE, denoting that the average simulated energy input in the snowpack is accurate compared to its temporal variation. This conclusion is only valid for the period when the snowpack temperature is below freezing, as in the melt season, the cold content is by definition 0 Jm$^{-2}$. Furthermore, the surface energy
balance is normally a self-balancing process, which is disrupted when phase changes occur.

Figure 8a shows the measured and modelled snow temperature time series at three heights for the example snow season. The change of snow temperature over the snow season is adequately captured. There is almost no difference between simulations with the bucket scheme or RE, except for the timing when the snowpack gets isothermal, associated with the meltwater front moving through the snowpack. For this example snow season, simulations with RE seem to better capture when the snowpack becomes 0°C, suggesting a better prediction of the movement of the meltwater front through the snowpack. In the Supplement Figs. S14 and S15, results for each snow season are shown. In most snow seasons, simulations with the RE provide a better agreement with measured temperatures in spring than the bucket scheme. However, in some snow seasons (e.g., 2001 and 2011), simulations with RE show an increase in snow temperature before the measured temperature increases, which suggest a too fast simulated progress of the meltwater front.

In Fig. 9a and b, the average and SD, respectively, of the difference between modelled and measured temperatures are shown, including snow surface and snow–soil interface temperatures, determined over all 15 snow seasons of the snow height-driven simulations and plotted as a function of the relative date in the snow season. During the main winter season, the temperatures at 50 and 100 cm height are on average up to 0.5°C lower in the model than in the measurements, whereas the temperature at 150 cm is on average up to 1.0°C too high in the simulations. Interestingly the snow surface temperature is generally underestimated, whereas the highest snow temperature sensor is too warm. The contrasting result suggests that the snow layers near the top of the snowpack have a too low density in the simulations. This provides a stronger isolation of the snowpack, causing heat from inside to escape at a slower rate and allowing the surface to cool more. Errors in diagnosing the snowpack energy balance would be suspected to influence all temperature sensors in the same direction.
The SD of the difference between modelled and measured temperatures shows an increase with height above the ground. This can be attributed to higher temporal variations in temperature in the upper snowpack due to highly variable surface energy fluxes. The SD for the snow and snow–soil interface temperature typically is less than 1.0°C, and decreases towards the melt season. For the surface temperature, the SD is typically high in the beginning and the end of the snow season. In the beginning of the snow season, lower snow densities, low air temperatures and reduced incoming shortwave radiation allow for a strong radiative cooling of the snow surface, which is delicate to simulate correctly and may result in errors in simulated snow temperatures up to 10°C. In the melt season, discrepancies in the duration the snow surface needs to refreeze at night may contribute to the increase in SD between modelled and measured surface temperatures.

Figure 9a also shows that in the beginning of the melt season, the difference between snow temperatures simulated with RE and measurements is on average smaller than with the bucket scheme at 0, 50 and 100 cm depth, suggesting a better timing of the movement of the meltwater front through the snowpack and the associated temperature increase to 0°C. The reason why this is not expressed in the temperature series at 150 cm remains unclear.

4.5 Snow density

Figure 10a and b show simulated snow density profiles for the bucket scheme and RE, respectively, for the example snow season 2014. In Supplement Figs. S16–S18, the other snow seasons are shown. Differences in density mainly arise when liquid water is involved. The accumulation and subsequent partial refreeze of meltwater at some layers form denser parts, whereas other layers remain less dense because less meltwater is retained. This type of stratification is known to happen, although verification is difficult, because density is sampled at a low spatial resolution in the manual snow profiles.
In Fig. 11a, average snow density as observed in the manual profiles is compared with the modelled snow densities for the snow height-driven simulations for the period 1999–2013. Generally, the seasonal trend in snow density is captured well in the model. Discrepancies between modelled and observed profiles are larger than the differences arising from the different water transport schemes. In general, SNOWPACK overestimates the density near the base of the snow cover, while it underestimates the density of the upper part of the snowpack. This is consistent for all simulated snow seasons, as illustrated in Supplement Fig. S19. It supports the argumentation in the previous section. These over- and underestimations are larger than the differences between water transport schemes. In Fig. 11b, the average and SD of the difference between simulated and observed density is shown, determined over the 15 snow seasons of the snow height-driven simulations. Average discrepancies in snow densities are less than 25 kg m\(^{-3}\), increasing to 50–100 kg m\(^{-3}\) shortly before melt out. The SD of the discrepancies is less than 50 kg m\(^{-3}\), increasing to 100–150 kg m\(^{-3}\) near the end of the melt season. This illustrates that the new snow density parametrisation and the snow settling formulation are able to provide accurate predictions of snow density. During the snow melt season, the deviations between observed and simulated snow density increase as a result of new snow fall events that are simulated to compensate for the overestimated SWE depletion.

The depletion rate is the result of many interacting processes. First of all, it is strongly coupled to snowmelt, and thus dependent on the surface energy fluxes. Given the high agreement in cold content in the main winter season, errors in diagnosing the surface energy balance due to uncertainties in atmospheric stability and measurement errors in radiation, wind speed or air temperature, seem to be small on average. However, a consistent or incidental overestimation of the energy input in the snow cover during the snow melt period may result in overestimated snow melt. Once the melt water is leaving the snowpack, the mass associated with it is definitely lost. Additionally, we would argue that an insufficient simulation of the densification during spring, under the influence of liquid water flow, may also be important here. A too low snow density
will result in a deeper penetration of shortwave radiation, effectively providing heat transport into snowpack. Furthermore, heat conductivity will be underestimated, with the consequence that the simulated snowpack in spring is too isolated to be able to release heat during night.

### 4.6 Grain size

Grain size plays an important role in liquid water flow, as it has a strong influence on the water retention curves (Eqs. 1–4). Figure 12a and b show modelled grain size profiles for the example snow season 2014 for the bucket scheme and RE, respectively. Differences between the schemes are mainly found in the melt season where the bucket scheme produces slightly larger grains. This is associated with the typically higher liquid water content using that scheme (Fig. 5a) compared to RE (Fig. 5b). This results in a stronger wet snow grain growth rate. Figure 12b also illustrates the cause of the liquid water accumulation found near a height of 120 cm in the beginning of April in Fig. 5b. The layer below the ponding water consisted of significantly larger grains and was creating a capillary barrier for the liquid water. In the Supplement Figs. S20–S22, results are shown for each snow season and a comparison with the LWC distribution (see Supplement Figs. S3–S5) shows that capillary barriers are a typical occurrence in simulations with RE for the deep, non-isothermal, stratified snow cover as found at WFJ.

Figure 13a and b show the average and SD of the grain sizes from the manual profiles and the simulations for the snow seasons 2000–2014. Most distinguishable is the steady increase in grain size towards and during the melt season. Both simulations show an increase in grain size towards the end of the snow season, although the average observed grain size is often underestimated. The underestimation of grain size in simulations with RE is consistent for most snow seasons compared to the bucket scheme. It results from generally lower LWC values in the snowpack in simulations with RE and, consequently, lower wet snow grain growth rates. This contributes to a reduced $r^2$ value for grain size (see Table 1). Most of the variation in grain size that exists
before the initial wetting of the snow, remains present throughout the snow season in
the simulations. However, the vertical variation of grain size typically decreases dur-
ing the melt season, as shown in Fig. 13b. However, opposite trends can be found,
mainly caused by snow falls during the melt season. The simulations tend to provide
a decrease of the SD in the melt season and the agreement with the observations
varies from year to year. Especially large variations in grain size in the profiles are not
captured in the simulations.

4.7 Comparison of simulated dry-wet transition with upGPR

Detailed comparisons of radar-determined dry-wet transitions with simulations of the
water transport schemes for the snow seasons 2011 through 2014 are presented in
Fig. 14. Measured snowpack runoff (by the snow lysimeter) is included in this pre-
sentation together with grain shapes observed in snow pits, which both are indicative
of water flow processes in snow. The dry-wet transition is only plotted when the up-
gPR signal indicated that parts of the snowpack were wet (see Sect. 3.3), or, for the
simulations, when the modelled snowpack was partly wet. Due to beam divergence,
a preferential flow path that forms in the vicinity above the upGPR could potentially be
detected, although generally the upGPR would be particularly sensitive to matrix flow.
However, liquid water accumulations above ponding layers are clearly visible in radar-
grams independent from matrix or preferential flow that formed such accumulations. It
is impossible to discriminate from the radar data which flow regime caused the respec-
tive liquid water accumulations. In addition, layer transitions within the resolution limit
of the radar (∼0.07 m for dry-snow conditions (Schmid et al., 2014)) are impossible
to discriminate as well and as a consequence, percolation depths of the wetting front
close to the ground surface (< 10 cm above the ground) cannot be accurately allocated
anymore. Interferences with the reflection signal from the cover box of the radar prevent
an accurate location of such signals.

From the four snow seasons presented in Fig. 14, the following observations can
be made: snowpack runoff measured by the snow lysimeter consistently starts ear-
liest in the snow season. The progress of the meltwater front is always faster in the simulations with RE, compared to the bucket scheme. The radar-derived meltwater front progresses generally slower through the snowpack than in both water transport schemes in the model. The manual snow profiles mostly show melt forms in parts of the snowpack that have been wet according to the radar data, whereas the simulations often show larger parts of the snowpack becoming wet earlier than indicated by the profiles. These observations will now be discussed in more detail.

Since preferential flow can route liquid water efficiently through the snowpack (Kat telmann, 1985; Waldner et al., 2004; Techel and Pielmeier, 2011), upGPR-determined depths of dry-wet transitions are not necessarily linked to the onset of measured snowpack runoff (Heilig et al., 2015). Studies by Katsushima et al. (2013) and Hirashima et al. (2014) found that ponding plays a crucial role in forming preferential flow in both laboratory experiments as well as model simulations. The ponding of liquid water in the simulations for WFJ (see Fig. 5) suggests that preferential flow may have developed. The amount of snowpack runoff measured before the arrival of the meltwater front is highly variable. From 1 until 8 April in snow season 2011, large amounts of snowpack runoff were observed, most likely due to lateral flow processes, whereas in snow season 2014, only marginal amounts were observed. In the latter snow season, there is a strong increase in observed snowpack runoff close to the time of the arrival of the radar-derived meltwater front at the snowpack base. This variability between years is not necessarily caused by different preferential flow path structures, but may also result from the limited capturing area of the snow lysimeter (Kattelmann, 2000).

The vertical distribution of the melt forms in the observed snow profiles may be considered particularly representative for matrix flow and for the four presented years it generally corresponds well with the parts of the snowpack that may be considered wet from the upGPR signal. As the bucket scheme shows a higher correspondence with the upGPR data than RE, the convenient improvement in the accuracy of simulated snowpack runoff with RE, as found in Wever et al. (2014), seems to be partly caused by (unintentionally) mimicking some preferential flow effects. To what extent
this is caused by parametrisations of the water retention curve or hydraulic conductivity, or by the specifics of the implementation of RE in SNOWPACK, remains unclear. Although the bucket scheme may seem to better coincide with the meltwater front in the upGPR data, it may as well be argued that the differences between both water transport schemes are smaller than the discrepancies with the upGPR data. It is likely that the limits of one-dimensional models with a single water transport mechanism will prevent a correct simulation of both snowpack runoff as well as the internal snowpack structure at the same time.

In the beginning of the melt season, when the meltwater front is disappearing regularly during night, the depth to which the liquid water infiltrates the snowpack is underestimated in the simulations. Here, the RE scheme shows larger infiltration depths, which are in better agreement with the upGPR data, although again differences between both simulations are smaller than the discrepancies with the upGPR data. This result is contradictory with the main melt phase, where the speed with which the meltwater front progresses through the snowpack is largely overestimated in the simulations. Furthermore, the distribution of melt forms in the snow profiles does not always coincide with the deeper infiltration depths detected by the upGPR.

An exception to the discussion above is snow season 2012, for which the results are consistent to a high degree. The progress of the meltwater front through the snowpack is accurately modelled by RE, and only slightly less accurately by the bucket scheme for this snow season when comparing with the upGPR signal. The snow lysimeter measurements show runoff almost directly at the time the meltwater front as detected from the upGPR reaches the soil. In the first snow profile made afterwards, melt forms were found for most parts of the snow cover. However, it is important to note that the progress of the meltwater front is much quicker than in the other snow seasons. Firstly, due to large snow falls in that snow season, the snow stratification was rather homogeneous, limiting the amount of possible capillary barriers or impermeable layers in the snowpack that could hinder the liquid water flow. The relatively homogeneous stratification can be found in snow density (Supplement Fig. S18) as well as in grain size (Supple-
ment Fig. S22). Second, the onset of the snowmelt was initiated by a very warm period, leading to sufficient snowmelt to infiltrate the complete snowpack in a short amount of time. These factors all provide fewer challenges for the model.

Figure 14 also illustrates the effects of the choice of averaging method for the hydraulic conductivity at the interface nodes. The progress of the meltwater front is following a stepwise pattern. The arithmetic mean is reducing the contrast in hydraulic conductivity, causing a smearing of liquid water between layers as well as over microstructural transitions inside the snowpack. The geometric mean is putting more weight on the lowest hydraulic conductivity, which is found in dry snow. This results in a strengthened capillary barrier, indicated by the temporal flatter position of the meltwater front compared to the arithmetic mean.

5 Conclusions

The one-dimensional physics based multi-layer SNOWPACK model has been evaluated against measured time series and manual snow profiles for the measurement site WFJ in the Swiss Alps near Davos. Two water transport schemes, the bucket scheme and RE, were taken into consideration as well as two modes to provide the precipitation forcing for the simulations: snow height-driven (15 snow seasons) and precipitation-driven (18 snow seasons). Along with the implementation of the solver for RE, the soil module of SNOWPACK has also been updated. Comparing simulated and measured temperatures at the snow–soil interface confirmed that the updated soil module can provide a correct lower boundary for the snowpack in the model.

The snow height-driven simulations provide good agreement with measured snow height (RMSE around 4 cm) and, during the accumulation phase of the snow cover, with SWE. This indicates that the model adequately simulates the combination of snow settling and new snow density. In precipitation-driven simulations, the SWE in the accumulation phase exhibits a slightly larger spread than in snow height-driven simulations, which is mainly caused by deficiencies in the precipitation undercatch correction and
possibly snow drift effects. This results in a lower RMSE for snow height (20–23 cm). For the simulations at WFJ, SNOWPACK consistently overestimates the depletion rate of SWE during the spring melt season, resulting in an underestimation of SWE of typically 200 mm w.e. near the end of the snow season, accompanied by an underestimation of snow height up to 30–40 cm. In snow height-driven simulations, this is compensated for by simulating regular snowfalls in order to match measured snow height. This procedure has as a drawback that too much mass is added to the snowpack in spring, resulting in an about 8–14 % overestimation of cumulative runoff over the snow season, whereas precipitation-driven simulations provide on average 2 % less snowpack runoff than measured.

The comparison of simulated snow density with snow density measurements made in snow profiles has shown that both the average snow density and the seasonal trend is well simulated in SNOWPACK during the main winter season. Average bias is around 25 kg m$^{-3}$ and the density of deep snow layers is slightly overestimated, whereas the density of upper layers is slightly underestimated. The discrepancies grow in the melt season, when SNOWPACK underestimates snow density on average up to 100 kg m$^{-3}$ as a result of new snow fall events that are simulated to compensate for overestimated SWE depletion in snow height-driven simulations. The model provides simulations of grain size which are consistent with observations in manual snow profiles. Although RE is causing a slight underestimation of grain size compared to the bucket scheme, snow density and grain size are adequately simulated for the parametrisation of the water retention curves.

Modelled and measured snow temperatures showed a satisfying agreement with average discrepancies of around 0.5°C. The discrepancies in the surface temperature were found to be larger, likely associated with the above mentioned underestimation of snow density in the upper layers and consequently the effect on thermal conductivity. The discrepancy in the cold content of the snow cover from simulations and field measurements was found to be small, suggesting that the surface energy balance and the soil heat flux are on average satisfactorily estimated. However, this conclusion only
The temporal evolution and the vertical distribution of the LWC in the snowpack differ significantly between the bucket scheme and RE. The latter provides a faster downward propagation of the meltwater front. This is accompanied by a higher $r^2$ value and NSE coefficient between simulated and measured snowpack runoff for the simulations with RE compared to the bucket scheme. RE also provides a higher $r^2$ value for the isothermal part of the snowpack compared to the manual snow profiles as well as a closer agreement with snow temperatures during the melt season. These results suggest a more accurate simulation of the progress of the meltwater front through the snowpack with RE. Although the data from the upGPR supports the deeper meltwater infiltration in the snowpack in the early melt phase as simulated with RE, the opposite is found for the main wetting phase. Additionally, the distribution of melt forms in the observed snow profiles shows a higher agreement with the upGPR signal than with the simulations. Both type of observations may be considered particularly representative of matrix flow processes. The high agreement between simulations with RE and snowpack runoff therefore suggests that the use or implementation of RE is unintentionally mimicking preferential flow effects. However, the differences between both water transport schemes are relatively small, compared to the differences between simulations and the observed melt water front in the upGPR data. The results suggest that the ability of a one-dimensional approach to correctly estimate both snowpack runoff as well as the internal snowpack structure in wet snow conditions is rather limited. As the simulation of ponding of liquid water on capillary barriers and crusts is only captured with RE and not with the bucket scheme, RE seems promising however for the ability of SNOWPACK to assess wet snow avalanche risks. Future studies may also focus on the possibilities to assimilate radar derived vertical snowpack structure (e.g., density, ice layers, liquid water) into the SNOWPACK model. This would allow to better understand to what extend discrepancies between simulations and radar data is caused by devi-
ations in the simulated snowpack state at the onset of snowmelt or by an insufficient process representation in the model.

The validation has shown that SNOWPACK has sufficient agreement with measurements for snow temperatures, snow density and grain size in the main winter season for a wide range of applications. When using RE, we found that the Y2012 water retention curve provides better results than the Y2010 parametrisation, whereas different averaging methods to determine the hydraulic conductivity at the nodes between layers seem to have little influence. In general, several aspects of the simulations related to liquid water flow improve with RE, although often, the differences between simulations tend to be smaller than differences between the simulations and the observations and the improvements are often inconsistent with the representation of the internal snowpack structure as indicated by the upGPR data.

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References


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Table 1. Average bulk snowpack statistics for various simulation setups (bucket or Richards equation (RE) water transport scheme, snow height (HS) or precipitation (Precip) driven simulations, Y2010 (Yamaguchi et al., 2010) or Y2012 (Yamaguchi et al., 2012) water retention curves, and arithmetic or geometric mean for hydraulic conductivity) for all simulated snow seasons. Differences are calculated as modelled value minus measured value, ratios are calculated as modelled value divided by measured value. The isothermal part is only considered during the melt phase (from March to the end of the snow season).

<table>
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<tbody>
<tr>
<td>RMSE HS (cm)</td>
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<td>4.12</td>
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<td>0.73</td>
<td>0.67</td>
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<td>0.91</td>
<td>0.91</td>
<td>0.83</td>
<td>0.85</td>
</tr>
<tr>
<td>$r^2$ isothermal part (-)</td>
<td>0.74</td>
<td>0.87</td>
<td>0.86</td>
<td>0.85</td>
<td>0.75</td>
<td>0.86</td>
</tr>
<tr>
<td>$r^2$ avg. grain size (-)</td>
<td>0.75</td>
<td>0.74</td>
<td>0.74</td>
<td>0.74</td>
<td>0.63</td>
<td>0.61</td>
</tr>
<tr>
<td>Mass balance error (mm w.e.)</td>
<td>0.01</td>
<td>0.01</td>
<td>0.01</td>
<td>0.01</td>
<td>0.09</td>
<td>0.02</td>
</tr>
<tr>
<td>Energy balance error (Wm$^{-2}$)</td>
<td>0.03</td>
<td>0.06</td>
<td>0.06</td>
<td>0.05</td>
<td>-0.05</td>
<td>0.05</td>
</tr>
<tr>
<td>CPU time (min)</td>
<td>0.57</td>
<td>1.39</td>
<td>1.44</td>
<td>1.45</td>
<td>0.61</td>
<td>1.55</td>
</tr>
</tbody>
</table>
Figure 1. Measured and modelled snow height for different model setups (bucket or Richards equation (RE) water transport scheme, snow height (HS) or precipitation (Precip) driven simulations, Y2010 (Yamaguchi et al., 2010) or Y2012 (Yamaguchi et al., 2012) water retention curves, and arithmetic (AM) or geometric mean (GM) for hydraulic conductivity) for the example snow season 2014, from October 2013 to July 2014.
Figure 2. Difference in modelled and measured snow height relative to the snow season for both snow height (HS) and precipitation (Precip)-driven simulations, determined over 15 and 18 years, respectively, using the bucket scheme or Richards equation with Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM). For every snow season, the first day with a snow cover is set at 0, the last day at 1.
Figure 3. Comparison of measured and modelled SWE (mm w.e.) (a) and increase in SWE in the biweekly profiles and the simulations during the accumulation phase (b) for both snow height (HS) and precipitation (Precip)-driven simulations, using the bucket scheme or Richards equation with Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM). Coloured lines denote the linear fits to the corresponding data, the black line indicates the line $y = x$. The blue and cyan dots in (b) perfectly overlap.
Figure 4. Difference in modelled and observed SWE in the biweekly profiles for both snow height (HS) and precipitation (Precip)-driven simulations, using the bucket scheme or Richards equation with Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM).
Figure 5. Snow LWC (%) for the snow height-driven simulation with the bucket scheme (a) and with Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM, (b), for the example snow season 2014.
Figure 6. Measured and modelled soil temperatures at 10, 30 and 50 cm below the surface for the example snow season 2014 (a) and measured and modelled snow–soil interface temperature for snow seasons 2000–2014 (b). Only the snow height-driven (HS driven) simulations with the bucket scheme and Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM) are shown.
Figure 7. Snow temperature (°C) for the snow height-driven simulation with the bucket scheme (a) and with Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM, (b), for example snow season 2014. Snow at exactly 0°C is coloured black to mark areas of the snowpack that are melting or freezing.
**Figure 8.** Measured and modelled snow temperatures at 50, 100 and 150 cm above the ground for snow height-driven (HS driven) simulations using the bucket scheme or Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM) for the example snow season 2014. Values are only plotted when the snow height was at least 20 cm more than the height of the temperature sensor.
Figure 9. Average (a) and SD (b) of the difference between modelled and measured snow temperatures, surface temperature and ground temperature (°C) relative to the snow season. For every snow season, the first day with a snow cover is set at 0, the last day at 1. The statistics are determined over the 15 snow seasons of the snow height-driven simulations using the bucket scheme or Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM).
Figure 10. Snow density (kg m$^{-3}$) for the snow height-driven simulation with the bucket scheme (a) and with Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM, (b), for example snow season 2014.
Figure 11. Average simulated and measured snow density (kg m$^{-3}$) (a) and average and SD of the difference between simulated and measured snow density (kg m$^{-3}$) (b), relative to the snow season for the lower, middle and upper part of the snowpack. For every snow season, the first day with a snow cover is set at 0, the last day at 1. The statistics are determined over the 15 snow seasons of the snow height-driven simulations using the bucket scheme or Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM).
Figure 12. Grain size (mm) for the snow height-driven simulation with the bucket scheme (a) and with Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM, (b), for the example snow season 2014.
Figure 13. Average (a) and SD (b) of observed and modelled grain size (mm) from snow height driven (HS) simulations using both the Bucket scheme and Richards equation using the Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM).
Figure 14. Snow height (dashed line), manual snow profiles (coloured bars, legend provided in (e)) and the position of the meltwater front as detected from the upGPR data (cyan dots), modelled with the bucket scheme (black dots), Richards equation with Yamaguchi et al. (2012) water retention curve and arithmetic mean for hydraulic conductivity (RE-Y2012AM, green dots) and similar but with geometric mean (RE-Y2012GM, brown dots) for snow season 2011 (a), 2012 (b), 2013 (c) and 2014 (d). Measured snowpack runoff is denoted by blue bars. The simulations were snow height-driven.