The past, present, and future viscous heat dissipation available for
Greenland subglacial conduit formation

Kenneth D. Mankoff¹ and Slawek M. Tulaczyk²

¹Department of Geosciences, Pennsylvania State University, University Park, PA 16802
²Earth and Planetary Sciences Department, University of California Santa Cruz, Santa Cruz, CA 95064

Correspondence to: Ken Mankoff (mankoff@psu.edu)

Abstract.

Basal hydrology of the Greenland Ice Sheet (GIS) influences its dynamics and mass balance through basal lubrication and ice/bed de-coupling, or efficient water removal and ice/bed coupling. Variations in subglacial water pressure through the seasonal evolution of the subglacial hydrological system help to control ice velocity. Near the margin, large basal conduits are melted by the viscous heat dissipation (VHD) from surface runoff routed to the bed. These conduits may lead to efficient drainage systems that lower subglacial water pressure, increase basal effective stress, and reduce ice velocity. In this study we quantify the energy available for VHD historically, at present, and under future climate scenarios. At present, 345 km³ of annual runoff delivers 2.1 EJ (2.1x10¹⁸ J) to the base of the ice sheet per year. These values are already ~50% more than the historical 1960 – 1999 average of 1.4 EJ year⁻¹. By 2100 under IPCC AR5 RCP8.5 (RCP4.5) scenarios, 1278 (524) km³ of runoff may deliver 9.8 (3.5) EJ year⁻¹ to the ice sheet base. Hence, the ice sheet may experience a ~5-fold increase in VHD in the near future which will enhance opening of subglacial conduits near the margin and will warm basal ice in the interior. The other significant basal heat source is geothermal heat flux (GHF), with historical values of 1.1 EJ year⁻¹ under the runoff area. There is no significant increase expected in GHF. With increasing surface meltwater penetration to the bed the basal heat budget in the active basal hydrology zone of the GIS will be increasingly dominated by VHD and relatively less sensitive to GHF, which may result in spatial changes in the ice flow field and in its seasonal variability.

1 Introduction

Numerical models and observations of the Greenland Ice Sheet (GIS) link surface meltwater penetration to the bed to both short (hourly, daily) and long (seasonal, decadal) temporal variations in ice velocity (Zwally et al., 2002; Bartholomew et al., 2011; Banwell et al., 2013; Shannon et al., 2013; Mayaud et al., 2014; Tedstone et al., 2015). However, the link between increased basal water inputs and ice sliding is a complex one, largely because viscous heat dissipation (VHD) from water flow beneath ice may melt out efficient drainage tunnels whose presence may decrease, or even reverse, the tendency for ice flow to accelerate with increasing meltwater inputs to the bed (Kamb, 1987; Sundal et al., 2011; Tedstone et al., 2015).

Early in the melt season water is added to the subglacial system but cannot be efficiently removed, increasing subglacial water pressures and ice velocities. Later in the melt season, increased runoff causes efficient drainage conduits to form, at least
near the ice sheet margin. These large drainage conduits reduce the subglacial water pressure and ice velocity (Hewitt, 2013). Even efficient drainage conduits can at times become over-pressured, with associated increase in ice velocity, until basal water is removed or the conduit opens more from additional melting (Schoof, 2010). This dynamic subglacial hydrologic system influences ice velocity during winter months as well. This behavior is less well understood, but in years with above average summer acceleration there is evidence of below average winter velocities and a reduced net annual displacement (Sundal et al., 2011). In addition, a recent observational study shows a regional and decadal velocity decrease coincident with a 50% runoff increase in southwest Greenland (Tedstone et al., 2015). Farther from the margin there is less surface runoff and therefore less subglacial water available. In this interior region channelized flow and subglacial conduits may not form. If they do form, they will in general creep closed more quickly than conduits that form under the thinner ice near the margin. Fewer conduits in the GIS interior, relative to the marginal zone, is one likely cause for the ice accelerations observed there under increased water inputs (e.g. Bartholomew et al. (2011); Shannon et al. (2013); Doyle et al. (2014)).

Studies examining surface melt, supra-glacial routing, subglacial hydrology, and the response of ice sheet outlet glaciers to those various inputs take place predominantly in southwest Greenland, focusing largely on the Russell, Leverett, Paakitsoq, or nearby glaciers (for example, Banwell et al. (2013); Arnold et al. (2014); Andrews et al. (2014); Tedstone et al. (2015)). Furthermore, present day weather, runoff, outflow, and other data are often used in those studies, since daily, hourly, or higher temporal resolution of the data is beneficial to the models. However, this approach limits the focus of these studies to recent seasons for which abundant in-situ sensor data exist. In order to examine future scenarios, Mayaud et al. (2014) built on the work of Banwell et al. (2013), but used a conduit model that includes melt opening and creep closure, driven by a positive degree day runoff model, to examine future changes to year 2095 under various IPCC RCP scenarios (Moss et al., 2010). Those models had hourly or daily resolution and were again limited to the well-studied southwest sector.

Here we perform a broader analysis that uses runoff over the entire GIS on annual and decade timescales, and frame the discussion in terms of changes in available heat, rather than focusing on water pressure in a conduit relative to overhead ice pressure. We report both the total GIS-wide energy budgets, and its distribution per basin and at a 5x5 km grid resolution. We also highlight a high-resolution (150 m) calculation near Petermann Glacier and along a single ice flowline in southwest Greenland.

2 Data

We use 150 m resolution basal topography and surface topography (IceBridge BedMachine Greenland, Version 2) from Morlighem et al. (2014, 2015) to calculate both surface and subglacial flow routing and subglacial pressures. Surface runoff, equal to the surface meltwater plus rain less refrozen water, comes from MAR v3.5.2 (Fettweis et al., 2013).

We report results for a historical period (1960 – 1999), the present (2010 – 2019), and IPCC AR5 RCPs 4.5, and 8.5 (2090 – 2099) (Moss et al., 2010). We also highlight a baseline (TB, 1985–1994) and reference (TR, 2007–2014) period that match the baseline and reference periods in Tedstone et al. (2015). It is important to note that while our TB may match the baseline data from Tedstone et al. (2015), there is no expectation that TR matches the reference data from Tedstone et al. (2015).
This is because the TB time frame use ERA-Interim reanalysis products, but the TR time-frame is from a "future" projection simulation (Fettweis et al., 2013), and is unlikely to have simulated the specific annual runoff, including the extreme melt in 2012.

We process the entire GIS at 5 km resolution, the area near Petermann Glacier at 150 m resolution, and part of West Greenland (near the Russell and Leverett glaciers) and at 150 m resolution, where we extract the sample flowline segment.

### 3 Model Description

We use a flow-routing and energy balance model that incorporates common assumptions about glacier hydrology (e.g. Röthlisberger (1972), Shreve (1972)), but does not explicitly resolve subglacial conduits. We lay out our methods and assumptions by tracing the path of a unit parcel of surface meltwater from source to sink (ice surface elevation at the origin of a meltwater parcel to submarine or terrestrial outlet where it discharges from the ice sheet).

We assume all surface runoff that begins at elevations above 2000 m is unable to leave the surface or penetrate to the bed at those elevations (Poinar et al., 2015). Instead we route it on the surface to the 2000 m elevation contour. All surface runoff at or below 2000 m elevation is assumed to access the bed within the 5 km square grid cell in which it originates (Yang and Smith, 2013). In reality water may flow slightly farther before leaving the surface (Yang et al., 2015), but we ignore this horizontal transport because when streams do travel this far on the surface, they are most likely to do so in gently-sloped and crevasse-free regions (Poinar et al., 2015). Horizontal transport of surface meltwater with a small elevation drop implies only a small impact on the calculated VHD. Horizontal surface transport in an area with large surface slopes is unlikely, because such regions have high driving stress, and crevasses routing the stream to the bed are likely to be present.

Water storage may occur in the firn or in crevasses. We assume these volumes are insignificant (at most a few percent) relative to the total runoff amount, that percent is not likely to change much in the future, and englacial storage does not release heat at the bed, which is the focus of this study.

Once at the bed, flow routing moves water in the direction of the negative of the gradient of the hydropotential $\phi$ (Shreve, 1972),

\[ \nabla \phi = \rho_w g \nabla z_b + \alpha \rho_i g (\nabla z_s - \nabla z_b), \]

with $\phi$ the hydropotential (units Pa), $\rho_w$ the density of meltwater (1000 kg m$^{-3}$), $g$ gravity, $z_b$ the bed elevation, $\alpha$ a flotation fraction (set to 0.9) because the subglacial system is often slightly less than the ice-overburden pressure (Engelhardt and Kamb (1997); Fountain (1994); Meierbachtol et al. (2013)), $\rho_i$ the density of ice (917 kg m$^{-3}$), and $z_s$ the surface elevation. All water is assumed to move to the one neighboring cell with the lowest hydropotential with eight total neighbors considered. Flow routing is implemented using the r.watershed tool in GRASS GIS (Neteler et al., 2012) version 7.0.4, with $\phi$ as the "elevation" input with all local minima filled so that all water leaves the ice sheet (see Supplemental Material).
The total hydropotential can be decomposed into an elevation term and a pressure term, where the former is the first term on the right hand side of Eq. 1 and the latter is the second term. We use this decomposition to examine in more detail the spatial distribution of flow driven by changes in the bed elevation, and flow driven by the pressure gradient.

The water remains at the pressure-dependent phase transition temperature (PTT) and energy is released based on the change in hydropotential combined with the changing phase change temperature. Because our focus is on energy available at the glacier bed, we ignore heat released due to changing PTT down the moulin (e.g. Catania and Neumann (2010)), and the model is initialized at the moulin bottom with a depressed PTT.

Our energy budget model tracks energy between inputs at the ice sheet bed where energy begins as either pressure or gravitational potential energy (which may be net positive if the source bed elevation is above the discharge elevation, or negative if it is below), and the output where the energy is in one of three forms: 1) the latent heat of cumulative basal melt caused by VHD released along the subglacial water flow pathway, 2) gravitational potential energy of discharge from land-terminating glaciers with terminii above seal level, or 3) pressure if discharged below sea level from a marine terminating glacier.

Between the input and discharge locations, all energy is assumed to dissipate as heat to the surrounding ice within the grid cell where the energy transfer occurs (Isenko et al., 2005). As water flows down the hydropotential gradient, we track the energy released as heat, $Q$, based on the volume of water, the change in the hydropotential, and the change in the PTT,

$$Q = V(\nabla \phi - C_T c_p \nabla \phi_p \rho_w)$$

where $V$ is the volume of water (Fig. 1), $\nabla \phi$ the hydropotential gradient, $C_T$ the Clausius-Clapeyron slope equal to 8.6x10^{-8} K Pa^{-1} (Hooke, 2005), $c_p$ the specific heat of water equal to 4184 J K^{-1} kg^{-1}, $\nabla \phi_p$ the pressure component of the hydropotential gradient, and $\rho_w$ the density of water. The last term of Eq. (2) is the adjustment for the PTT, which increases the heat released along the flowline when the ice thickens downstream and the PTT drops, and reduces the heat released along the flowline when the ice thins downstream. If the second term on the right hand side of Eq. 2 is larger than the first term, then $Q$ is negative, and basal freeze-on occurs (Alley et al., 1998; Bell et al., 2014)

## 4 Results

### 4.1 Volume of subglacial hydrology

Subglacial hydrology flow volumes are a combination of the surface runoff and the flow routing algorithm. Annual average runoff volume has historically been 244 km$^3$, presently is 345 km$^3$, and in the future will be 524 or 1278 km$^3$ under the 4.5 or 8.5 scenarios. Because we do not account for changes in water storage, total subglacial volumes are the same. The spatial distribution of flow volume at the bed matches the large-scale surface distribution - more occurs in the south than the north, and the bulk occurs in the southwest sector. Most runoff also occurs at the edge of the ice sheet. Under RCP 8.5 it is predicted to occur at all elevations in south Greenland, but here only accesses the bed when the surface elevation is < 2000 m (Fig. 1).
Flow routing of basal hydrology causes orders of magnitude difference in water volume over small spatial distances as streams collect and discharge the water. At present, the largest volume of discharge is \(~7 \text{ km}^3 \text{ year}^{-1}\) from a single grid cell (2% of the total annual runoff - that percentage has not and does not significantly change). The volume flow rate has increased from \(~5 \text{ km}^3 \text{ year}^{-1}\) historically, and is 10 or 31 \text{ km}^3 \text{ year}^{-1} under the future 4.5 or 8.5 scenarios.

4.2 Pressure v. elevation driven flow

The zone around Greenland with active subglacial flow has distinct regions where the flow is driven by changes in elevation (Fig. 2 panel \(\nabla \phi_z\)) or pressure (Fig. 2 panel \(\nabla \phi_p\)). Flow always leaves the ice sheet at the margin due to pressure-driven flow (i.e. from regions with thinning ice, red outer band in Fig. 2), but inland often travels under regions where ice thickens and pressure increases (blue regions in Fig. 2). Distinct regions of flow under thickening ice occur near the Petermann, Zachariae Isstrøm and 79 North Glaciers, and some coherent patches along the west coast.

Large differences in released heat (>35%) are due to flow under thinning or thickening ice. When water flows under thinning ice, \(~35%\) of the heat released by the reduction in pressure is used to warm the water with the rising PTT (Röthlisberger, 1972), and not included in our VHD numbers. In the regions highlighted above where flow occurs under thickening ice, a decrease in the PTT increases the VHD term.

4.3 Flow-routed spatial distribution of VHD

A spatial map of basal VHD is shown in Fig. 3 with the energy calculated based on Eq. (2). Summing the spatial data in Fig. 3 gives annual GIS-wide VHD of 1.4, 2.1, 3.5, and 9.8 EJ year\(^{-1}\) (1 EJ = 1x10\(^{18}\) J) for the historical, present, RCP4.5 and RCP8.5 cases respectively (Table 1). At present a maximum up to \(~1 \text{ W m}^{-2}\) is released where the largest volumes of water leave the ice sheet, over an entire 5x5 km grid cell. More generally, between 0.1 and 1 W m\(^{-2}\) is released in the marginal zone, but by year 2100 under RCP8.5, this amount of heat is likely to be released throughout almost the entire area of GIS where runoff is projected to reach the bed. In the future, regions with high discharge may experience 10 W m\(^{-2}\) VHD rates.

In some regions, heating is "negative" which indicates basal freeze-on. These regions are a subset of the regions where pressure increases due to ice thickening along-flow (\(\nabla \phi_p\) in Fig. 2). Locations of basal freeze-on occur throughout the GIS, including near Petermann where Bell et al. (2014) provides observational evidence of packages of basal freeze-on. Our model estimated locations (blue in Figure 7), and the Bell et al. (2014) observed locations (black in Figure 7) show some agreement and some disagreement. We interpret the disagreements as a combination of artifacts in the basal DEM and artifacts due to limitations in our routing model. We address each of these in the discussion section.

4.4 Basin-scale changes of VHD

Basin-scale changes between the three different time periods considered here are well illustrated when viewed as change (units Joule) in VHD per basin (Fig. 4) or percent increase (units %) in VHD per basin (Fig. 5). Basin size influences results for the
former, and the effect is removed for the latter. Because integrated per basin VHD removes the effect of flow routing, VHD per basin is approximately proportional to runoff per basin, and changes in basin VHD are proportional to changes in basin runoff.

Change between the Tedstone et al. (2015) reference period (TR) and the Tedstone et al. (2015) baseline period (TB, Fig. 4a) shows a 2 PJ year$^{-1}$ (1 PJ = 1x10$^{15}$ J) increase in the energy in each basin in the southwest sector where Tedstone et al. (2015) observed a general velocity decrease. (A 2 PJ year$^{-1}$ increase means a cumulative increase of 2 PJ in the future years, not a rate of change of 2 PJ each year between the two time periods). Elsewhere, increases were minimal (southeast) or negative. A similar pattern emerges between the historical and present cases (Fig. 4b), with the bulk of the change in the southwest sector, but larger than for TB-TR. At present there is a 10 PJ year$^{-1}$ difference compared to the historical rate. Between the present and the 2090s under the RCP 4.5 scenario, 10 PJ year$^{-1}$ increases occur in all sectors except the northwest (Fig. 4c). In the RCP 8.5 scenario, 100 PJ year$^{-1}$ increases occur in several basins (Fig. 4).

Percent increase between historical and present shows that the increases scale with latitude. All of Greenland has experienced an increase, with many regions showing a 2- to 3-fold increase (+100-200%) in VHD (Fig. 5 panel P/H). Runoff, and therefore VHD, in the north of Greenland has experienced the largest percent increase. This is because VHD values are so small there that all increases appear large when viewed on a percentage scale.

However, the choice of baseline matters. The historical and present periods are 1960 – 1999 and 2010 – 2019 respectively. If the TR (1985 – 1994) and TB (2007 – 2014) periods are used instead, our results instead match the results from Tedstone et al. (2015), which showed a 50% increase in runoff in the basins just south of Jakobshavn Isbær. The issue with our TR data produced by a future simulation and not using reanalysis products may be the cause of the difference between a ~50% increase in runoff reported by Tedstone et al. (2015) and the ~10-20% increase in VHD obtained here.

### 4.5 VHD along a flowline in southwest Greenland

Viewing results along a flowline highlights that the hydropotential gradient driving the flow becomes spatially both larger and more variable toward the margin (Fig. 6a). Along a single flow-line, step-increases in volume occur where other major tributaries join the tributary displayed here, causing 3 to 4 orders of magnitude increase in flow volume (Fig. 6b). This increase in water volume leads to a 3 to 4 orders of magnitude increase in VHD (Fig. 6c). Variations in bed topography and ice thickness create variations in the gradient of $\phi$ along the flowline (Fig. 6a) and therefore variations in VHD along the flowline (Fig. 6c). Although the general trend of VHD increases from inland to the margin (Fig. 6c) due to increasing flux (Fig. 6b), the hydropotential gradient (Fig. 6a) adds a high variability signal to the background flux-driven signal, with 1-2 orders of magnitude change in VHD over just a few of the 150 m grid cells. Gaps in Fig. 6c are due to low gradients at those locations causing the release of only minor amounts of VHD.

### 4.6 VHD and GHF

Frictional basal heating is up to 0.2 W m$^{-2}$ near the Russell and Leverett glaciers (Brinkerhoff et al., 2011), while geothermal heat flux (GHF) is estimated at ~0.050 W m$^{-2}$ (Shapiro and Ritzwoller, 2004) to as little as 0.030 W m$^{-2}$ (Meierbachtol et al., 2015). The logarithmic scale used in Fig. 6c makes the differences between these heat sources and VHD appear small, but near
the margin VHD exceeds GHF by one to two orders of magnitude. At present, VHD releases more heat than GHF from ~75 km up the flowline (< 75 km inland due to a sinuous path) to the margin. In the future, when larger volumes of water flow from farther in the interior, the zone where VHD surpasses GHF may increase its reach to ~150 km upstream from the ice margin (Fig. 6c).

5 Discussion

5.1 The impact of VHD

An increase in the supply of surface runoff to the bed will lead to an increase in subglacial VHD as the climate warms in the future. We have shown that a six-fold increase in VHD is predicted by the end of the century under RCP 8.5. The impact of this increase is uncertain. This is because other results show that glaciers can either increase (Zwally et al., 2002) or decrease (Sundal et al., 2011; Tedstone et al., 2015) their mean annual velocity as additional water accesses the bed. The theory of efficient versus inefficient subglacial drainage explains the different observations, but it is not known what is the current mode of subglacial water drainage beneath all parts of Greenland, what specific thresholds may cause switches in drainage modes, nor the associated response of ice dynamics to these switches.

When discussing subglacial hydrology, a simplification can be made that increased water input should lead to increased basal lubrication and faster sliding but increased VHD leads to reduced subglacial water pressures and slower sliding. However, because VHD is generated by water flow, some condition is needed to define which behavior is dominant in a given setting. We speculate that increasing VHD will have different impacts near the ice sheet margin as compared to the interior of the GIS. Steep hydropotential gradients, found often near the margin, favor high VHD generation for a given water discharge while small gradients do the opposite. At the same time, under thinner ice near the margin, pressure available to close subglacial conduits is smaller than under thicker ice.

The marginal zone ice response to VHD has been well-studied and observed in the southwest sector, where an increase in runoff is correlated with reduced glacier velocities (Bartholomew et al., 2010; Sundal et al., 2011; Tedstone et al., 2015). The interior ice response to increased runoff is less well-studied. However, Bartholomew et al. (2011) show that that ice does not slow down later in the season as more runoff reaches the bed, and Doyle et al. (2014) shows a year-on-year increase in velocity even with increasing runoff.

Mayaud et al. (2014) has bridged the gap spatially between the margin and the interior, and temporally between present and future, using the same runoff and RCP scenarios used in this study. They show that near the margin in the Paakitsoq region, conduits are likely to form earlier, remain longer, and reduce glacier velocity under RCP 4.5 and 8.5 compared to present. They also hypothesize that under thicker ice, conduits are unlikely to form, and increased water input into a more distributed subglacial drainage system may lead to an increase, rather than a decrease, in glacier velocity.

An increase in the interior ice velocity and a decrease in marginal velocity suggests that surface slopes and driving stresses will change, a result confirmed by Shannon et al. (2013). However, the range of possible results is not well enough constrained there to know the impact of the change in driving stress.
5.2 Increasing VHD

The contrasting impact of VHD on ice velocity appears to be primarily a function of basal pressure and subglacial hydrological flux (e.g. Schoof (2010)). However, the specific conditions that cause a velocity increase or decrease have not been well defined. Andersen et al. (2011) performed a sensitivity study between glacier velocity and increased runoff, but that study was limited to 55 days and one marine terminating glacier. It is therefore hard to estimate what the impact of increasing VHD will be in the future on the GIS.

5.2.1 Increasing VHD in the marginal zone

A threshold of a 50% increase in runoff has been identified by Tedstone et al. (2015) as leading to a widespread reduction in glacier velocity in the southwest sector marginal zone. It is likely that the threshold is not a 1.5 times increase in runoff, but perhaps the absolute change in VHD. We demonstrate this by comparing both the change [units J] and relative change [units %] in VHD in our results to the relative change reported by Tedstone et al. (2015).

We show a 10-20% increase in basin-cumulative VHD over the same region and time period used by Tedstone et al. (2015) (Fig. 5, right panel). However, our results include all of the GIS and relative decreases elsewhere do not match observed velocity trends over similar time periods (e.g. Rignot and Kanagaratnam (2006); Joughin et al. (2010)). We also show that this 10-20% increase is equivalent to an absolute increase of ~2 PJ year\(^{-1}\) per basin (Fig 4a). Over this same period, much of the rest of the ice sheet has near zero or negative increases (when viewed on a petaJoule scale). If the correlation between our results and Tedstone et al. (2015) shown here is causal, then it appears that an increase of VHD on the order of a 1 PJ may be near the threshold that causes a reduction in ice marginal zone velocities.

Under the RCP 4.5 scenario, every basin will experience a 2 PJ year\(^{-1}\) increase in VHD, with many gaining >10 PJ year\(^{-1}\) (these numbers are the total change of a rate, not a rate of change). These significant increases in VHD should cause conduits, where they do form, to form more quickly and grow to larger dimensions than they do at present.

The VHD results presented here match the location and magnitude of an increase in runoff that causes a slowdown near the margin according to Tedstone et al. (2015). This supports our proposition that significant increases of VHD around all of GIS in the future may cause a slowdown in marginal zones elsewhere. At marine terminating glaciers, this effect may be less important than other processes determining glacier velocity and its variability, such as the processes related to ice-ocean interactions (e.g. Walter et al. (2012)). There may be fundamental differences in VHD between marine- and land- terminating glaciers. Relative to land-terminating glaciers, marine-terminating glaciers have a depressed PTT at the discharge location. They may also have reduced surface slopes near their margin and different basal topography (producing different hydropotential gradients), from the cumulative effect of a different flow regime due to their marine boundary.

5.2.2 Increasing VHD in the interior

Future VHD will be distributed over a longer part of a year relative to the present since climate warming prolongs the melt season in Greenland (Hanna et al., 2008). It will also be distributed spatially further inland relative to the present, and in the...
interior is less likely to form conduits (Dow et al., 2014). Additional heat and water at the bed will warm the basal ice. If it cannot be evacuated efficiently by conduits, it will also increase basal water pressures and reduce friction. Given that the primary cause of velocity decreases near the margin is assumed to be the evolution of subglacial conduits reducing basal water pressures, their absence in the interior means we expect velocities to increase, in line with existing observations (Doyle et al., 2014; Bartholomew et al., 2011).

When VHD occurs in new locations at the GIS bed it may convert a frozen bed to temperate and increase ice sliding (Parizek and Alley, 2004; Shannon et al., 2013). This is not likely to impact most of Greenland, where the frozen bed is under ice with a surface elevation > 2000 m and therefore remains isolated from surface runoff. However, the northern sector has a frozen bed in regions where, according to our model, VHD increases markedly under the RCP 4.5 and 8.5 scenarios (MacGregor et al., 2016).

5.3 Other uses of energy than VHD

Not all of the incoming energy is converted to VHD and used to melt conduits, warm the basal ice, or warm the bed. The primary use of energy other than VHD is change in heat content of the water itself which needs to compensate for the spatially changing PTT. Classic glacier theory (i.e. Röthlisberger (1972)) states that when flow is driven by a pressure gradient, 35% of the available VHD is used internally to keep the water at the phase transition temperature (here termed a "loss"), and the remaining amount is dissipated as heat.

Our results show that different sectors may experience large changes in VHD relative to each other due to changes in the PTT. In practice, losses near 35% occur often - whenever elevation change across a grid cell is close to 0, and flow is driven primarily by a pressure gradient (Fig. 2). Negligible losses, near 0%, are also relatively common, when ice thickness does not change and both surface and bed elevation have similar gradients. Gains of 35% may also occur where the surface remains near flat and the bed drops drastically. Finally, in some places an increasing PTT may consume 100% of the available VHD and basal freeze-on occurs. Although here we use the term "freeze" and display locations of freeze-on in blue (Fig. 3), these regions inject excess heat into the subglacial water and basal ice (not tracked in our model), due to the release of latent heat as water freezes (Alley et al., 1998; Bell et al., 2014).

There are some disagreements in the location of basal freeze-on between our model and Bell et al. (2014) observations. The largest area of disagreement occurs in the upper Petermann catchment (bottom right of Fig. 7). In this area, the model does not estimate freeze-on within a few km of the observed basal ice packages. Conversely, in the northwest sector, several observational transects running east-west appear just southward of similar east-west model clusters of freeze-on locations. It seems likely that these agreements may also indicate an artifact in the basal DEM. The basal DEM is built, in part, from these same Bell et al. (2014) observational transects (Morlighem et al., 2014). The regular vertical spacing and linear horizontal clustering suggests a processing artifact. Finally, our routing model treats over-deepenings and locations of basal freeze-on the same as other regions, which may be an invalid assumption. Hooke (1994) showed that on mountain glaciers, water preferentially routes englacially as it crosses an over-deepened section, rather than subglacially. Englacial routing in the interior of the GIS may not
be as likely to occur as in a mountain glacier, but alternate basal paths may be used by the water to avoid locations favorable for freeze-on.

It seems likely that part of the cause for the disagreement between our model results and Bell et al. (2014) observations is because the basal DEM does not accurately represent the bed topography, at least at 150 m resolution. If this is the case, it impacts locations of basal freeze-on, and has some impact on the flow routes modeled here, but should not change the basin-scale results. Those results are primarily a function of the surface runoff volume and location, large-scale ice-thickness, and locations of the outlet glaciers. The path the water takes between the source and sink only impacts local VHD distributions, not basin-scale quantities.

5.3.1 Geothermal Heat Flux

GHF is spatially more uniform than VHD, at least near the margin where conduits concentrate the flow. GHF is temporally more steady than VHD, which primarily occurs when surface melt is active. Nonetheless, it is worth comparing the magnitude and distribution of the two. Historically the total VHD of 1.4 EJ year\(^{-1}\) under the runoff area was similar to the total GHF of 1.1 EJ year\(^{-1}\) over that same area. That is no longer the case in our calculations for the recent time period, and although GHF flux does not change, the integrated amount does change because the area of integration changes. By the end of this century under RCP 8.5, VHD will contribute \(\approx\)9.8 EJ year\(^{-1}\) while GHF only increases to 1.4 EJ year\(^{-1}\) due to a slight increase in the runoff area that reaches the bed (when surface runoff is routed to 2000 m elevation before moving to the bed).

VHD and GHF comparisons and relative changes between present and future are most likely to matter in the region > 75 km upstream of the margin and where VHD is active. This is because the change here a) switches which term is dominant and b) is far enough inland that conduits are less likely to form (Dow et al., 2014), meaning VHD is more likely to be spatially uniform rather than concentrated in smaller regions.

VHD dominates other basal heating terms considered in some glaciological models (for example, Brinkerhoff et al. (2011)). Models show that the GIS is sensitive to its basal temperature, with small differences in GHF producing significantly different GIS growth scenarios (Rogozhina et al., 2012). Local GHF highs also coincides with onset of fast ice flow (Fahnestock et al., 2001). The results of our analysis and these GHF studies suggest that if VHD changes from 1 to 2 orders of magnitude less than GHF, to 1 to 2 orders magnitudes more than GHF, it will likely decrease the importance of GHF in modulating spatial dynamics of the ice sheet, at least within the zone of active basal hydrology dominated by surface water penetration to the bed.

5.4 Erosion and sediment transport

Large amounts of eroded material are also flushed out from under the GIS each year (Cowton et al., 2012). The erosion rates implied by the sediment flux are already several orders of magnitude above the background (>1000 year) erosion rates (Koppes and Marchant, 2009). Larger VHD leads to larger conduits, faster water flow velocity, and higher erosion rates and sediment transport capacity. Conversely, slow subglacial water flow does not have as much impact on erosion and sediment transport (Hodson et al., 2016; Gimbert et al., 2016). If 5 times the amount of water flows along the GIS bed by the end of the century, it will likely increase sediment removal (Bogen and Bønsnes, 2003). If increased VHD and water at the bed of the GIS
simultaneously cause sediment removal rates to increase, while at the same time reducing the glacier velocity (Tedstone et al., 2015) and therefore the production of sediment (Herman et al., 2015), the state of the bed may change over the coming centuries to millenia from potentially deformable subglacial sediments to rigid bedrock (Weertman, 1964; Kamb, 1970; Tulaczyk et al., 2000; Bougamont et al., 2014).

5.5 The impact of model spatial resolution on results

The model resolution is a 5x5 km grid for most of the analysis presented here, which means results are smoothed over that area. In reality, subglacial discharges occur approximately on the order of one every 5 km along the coast (Lewis and Smith, 2009). If a single conduit on the order of 10 – 100 m wide carries all of the water (Fig. 1) and is subject to all of the heating (Fig. 3), then values reported (here spread over 5000 m) are likely be one or more orders of magnitude larger in focused regions, and one or more orders of magnitude smaller outside the conduit. This limitation of the model domain is less important in the interior, where conduits are less likely to form.

Our treatment of en- and sub- glacial hydrology is simplified because it does not represent actual conduits, but is at the same time more comprehensive than in existing global climate or ice-sheet models (e.g. Pollard and DeConto (2012)), and may offer a computationally efficient yet improved method to incorporate parameterizations of VHD at their existing grid resolution.

6 Conclusions

The high potential energy contained in large volumes of GIS surface meltwater is largely dissipated as heat at the ice sheet bed. This dissipated energy averaged 1.4 EJ year\(^{-1}\) between 1960 and 1999, but has recently increased to 2.1 EJ year\(^{-1}\) and will likely increase to 3.5 or 9.8 EJ year\(^{-1}\) by the end of the century under RCP 4.5 or 8.5 respectively. This viscous heat dissipation by subglacial water is the dominant basal heat source near the margin, and its impact will move inland due to increasing flux, even if conduits do not form in the interior. Under RCP 8.5, VHD will be about ten times larger than the \(-1\) EJ year\(^{-1}\) contributed by geothermal heat flux to the same area.

Up to 6 times additional future VHD at the ice sheet bed (relative to the historical amount) should result in a similar 6 fold increase in basal ice melt volume and is expected to contribute to more numerous, larger, longer-lasting, and more widespread subglacial conduits in the margin zone. Based on recent measurements by others and glaciological theory of ice sliding, increased VHD may decrease glacier velocity at the margin, and accelerate it in the interior where conduits either do not form or have insufficient impact on subglacial water pressures to influence ice sliding rates. This decrease may be offset by other processes and there may still be a net acceleration, especially at marine terminating glaciers.

Appendix A: About This Document

This manuscript is prepared with the intent to create a "fully reproducible" scientific publication. We may not have completely succeeded, but have made progress in this direction. In order to be fully reproducible at the binary-level, a clone of our operating
system with the full analysis software should be provided. This could be done with a virtual machine (VM) but we have not
taken this step because VMs require ~20 GB of space, and journals do not yet support this size of supplemental materials.

Instead, we used only free and open source software above the operating system level, document in detail the version(s) of
all software packages used, and provide every line of code required to reproduce the document, beginning with the commands
to download the MAR (Fettweis et al., 2013) and IceBridge BedMachine Greenland, Version 2 (Morlighem et al., 2015, 2014)
data sets, followed by the GRASS GIS (Neteler et al., 2012) and Python commands to produce intermediary data products and
graphics.

The supplementary data is a plain-text file that contains the manuscript text and all of the code. As plain text, it can be viewed
in any editor or document viewer. However, its internal structure is that of an Emacs Org Mode (Schulte and Davison, 2011;
Schulte et al., 2012) file and is best viewed in Emacs, which supports execution of the embedded code blocks. A reader should
be able to reproduce the contents of this document, although it will require 3rd-party applications (GRASS, Python, etc.), and,
optionally, a similar system-level Emacs configuration as the authors.

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References


Figure 1. Accumulation of subglacial water flowing through each grid cell. Results are presented on a 5x5 km grid. Labels represent (H)istorical mean from 1960 – 1999, (P)resent mean from 2010 – 2019, (4.5) years 2090 – 2099 under IPCC AR5 RCP4.5, and (8.5) same as (4.5) but under scenario RCP8.5. Gray contours mark 0 and 2000 m elevation.
Figure 2. Net hydropotential gradient for each cell (\(\nabla \phi\)), and the decomposition of net hydropotential gradient to elevation-driven hydropotential gradient (\(\nabla \phi_z\)) and pressure-driven hydropotential gradient (\(\nabla \phi_p\)). Red implies flow downhill and under thinning ice. Blue implies flow uphill and under thickening ice.
Figure 3. Heat released at the bed due to VHD. Labels same as Fig. 1. Colorbars represent heating (red) and cooling (blue), and numbers are valid for both colorbars (i.e. 1 W m\(^{-2}\) equals 3x10\(^7\) J m\(^2\) year\(^{-1}\), and each of those values are positive on the red colorbar and negative on the blue colorbar). Gray contours mark 0 and 2000 m elevation.
**Figure 4.** Change in VHD per basin. Label TB-TR represents increase from reference to baseline periods (1985–1994 and 2007–2014) from Tedstone et al. (2015), P-H increase from historical to present, 4.5-P increase from present to 2090s under RCP 4.5, and similarly for 8.5-P. Gray contours are 0 and 2000 m elevation.
**Figure 5.** Relative change in VHD per basin highlighting the impact of different averaging periods. P/H is 100 x present divided by historical, and TR/TB is 100 x the reference (1985–1994) divided by baseline (2007–2014) years from Tedstone et al. (2015). Gray contours are 0 and 2000 m elevation.
Figure 6. Detail along a flow line in Southwest Greenland. a) surface and bed elevation (left axis) and gradient of $\phi$ (right axis), b) flow rate of subglacial water, and c) power or heat flux, frictional heating, and geothermal heat flux (GHF). Legend labels H, P, 4.5, and 8.5 same as Fig. 1. Frictional heating from Brinkerhoff et al. (2011), and GHF from Shapiro and Ritzwoller (2004). Lines in panel (c) are smoothed to reduce visual noise and are actually as variable as panel (a).
Figure 7. Close-up of Petermann glacier region at 150 m resolution. Gray basemap is shaded relief of hydropotential gradient. Blue dots and black lines are locations of basal freeze-on predicted by the model and from Bell et al. (2014), respectively. Each blue dot is a 150 m x 150 m square pixel.

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