Authors’ Responses to the Comments on the Manuscript

“A simulation of the large-scale drifting snow storm in a turbulent boundary layer”

General Response to the Comments:

According to your comments, we have modified the original manuscript carefully (see the point-by-point reply to the comments, and the marked-up manuscript below). We have also checked the manuscript carefully for typos, authors and corresponding affiliations, terminology, variables in equations, acknowledgements and references.

Responses to Comments of Editor:

[Comment] Your revised version of manuscript will be accepted for publication in TC after some minor revisions are made. Please see the comments from the reviewer below. At this point I ask you to carefully proofread the manuscript and make any necessary correction, such as missing units etc.

[Response1] Thank you for your recommendation.

We have carefully proofread the manuscript according to your and reviewer comments. The missing units have been added, and the typos, acknowledgements, variables in equations and references have been updated in the revised manuscript.

Responses to Comments of reviewer:

[Comment] The authors have improved the manuscript and mostly taken into account the previous remarks. I find that this work gives a good basis for further research in the area. Therefore, the manuscript now deserves publication. However, there are few mistakes in the manuscript, such as there is not unit after ‘ ’.

[Response1] Thanks for your careful reviewing.

According to your comment, the missing units have been added in the revised manuscript. At
the same time, we have also checked the manuscript carefully, the acknowledgements, typos, variables in equations and references have been updated in the revised manuscript.

Finally, once again we appreciate you for your good and comprehensive comments. Those revisions according to your comments really make this manuscript improve a lot.

Thank you!

Yours sincerely,

Zhengshi Wang, and Shuming Jia.
A list of changes

1. The word ‘sources’ has been modified into ‘source’ in line 27.
2. The symbol ‘$R$’ has been modified into ‘$R_d$’ in line 84.
3. The expression ‘$\nu = 1.5e - 5$’ has been modified into ‘$\nu = 1.5 \times 10^{-5}$ m$^2$s$^{-1}$’, in line 109.
4. The word ‘dynamic’ has been modified into ‘kinematic’ in line 109.
5. The symbol ‘$d$’ has been modified into ‘$d_p$’, in equation (10).
6. The sentence ‘$g$ is the gravity acceleration’ in line 139 has been deleted.
7. The expression ‘$1000 \times 500 \times 1000$ m’ has been modified into ‘$1000 \times 500 \times 1000$ m’ in line 175.
8. The expression ‘$d$ is the particle diameter, and’ in line 210 has been deleted.
9. The symbols ‘$d$, $\alpha$ and $\beta$’ has been modified into ‘$d_p$, $\alpha_p$ and $\beta_p$’, respectively, in equation (17).
10. The symbols ‘$\alpha$’ and ‘$\beta$’ has been modified into ‘$\alpha_p$’ and ‘$\beta_p$’ in line 208 and 210.
11. The sentences ‘the State Key Program of National Natural Science Foundation of China (91325203), the National Natural Science Foundation of China (11172118, 41371034), and the Innovative Research Groups of the National Natural Science Foundation of China (11121202), National Key Technologies R & D Program of China (2013BAC07B01)’ have been modified into ‘the National Natural Science Foundation of China (11772143, 41371034), and National Key Research and Development Program of China (2016YFC0500900)’ in line 393-395.
12. The reference ‘Budd, W. F.: The Byrd snow drift project : outline and basic results, 71-134, American Geophysical Union, Washington, DC, 1966.’ has been modified into ‘Budd, W. F.: The Byrd snow drift project : outline and basic results, American Geophysical Union, Washington, DC, 71-134, 1966.’.


Marked-up manuscript:

A simulation of the large-scale drifting snow storm in a turbulent boundary layer

Zhengshi Wang\textsuperscript{1,2}, Shuming Jia \textsuperscript{1,2}*

\textsuperscript{1} State Key Laboratory of Aerodynamics, China Aerodynamic Research and Development Center, Mianyang Sichuan 621000, China

\textsuperscript{2} Computational Aerodynamics Institute, China Aerodynamics Research and Development Center, Mianyang, Sichuan 621000, China

* Corresponding: Shuming Jia (jiashm17@cardc.cn)
Abstract. Drifting snow storm is an important aeolian process that reshapes alpine glaciers and polar ice shelves, and it may also affect the climate system and hydrological cycle since flying snow particles exchange considerable mass and energy with air flow. Prior studies have rarely considered the full-scale drifting snow storm in the turbulent boundary layer, thus, the transportation feature of snow flow higher in the air and its contribution are largely unknown. In this study, a large eddy simulation is combined with a subgrid scale velocity model to simulate the atmospheric turbulent boundary layer, and a Lagrangian particle tracking method is adopted to track the trajectories of snow particles. A drifting snow storm that is hundreds of meters in depth and exhibits obvious spatial structures is produced. The snow transport flux profile at high altitude, previously not observed, is quite different from that near the surface, thus, the extrapolated transport flux profile may largely underestimate the total transport flux. At the same time, the development of a drifting snow storm involves three typical stages, the rapid growth, the gentle growth and the equilibrium stages, in which the large-scale updrafts and subgrid scale fluctuating velocities basically dominate the first and second stage, respectively. This research provides an effective way to get an insight into natural drifting snow storms.
1 Introduction

Snow, one type of solid precipitation, is an important source of material to mountain glaciers and polar ice sheets, which are widespread throughout high and cold regions (Chang et al., 2016; Gordon and Taylor, 2009; Lehning et al., 2008). A common natural phenomenon over snow cover is the drifting snow storm, which occurs when the wind speed exceeds a critical value (Doorschot et al., 2004; Li and Pomeroy, 1997; Sturm and Stuefer, 2013). Drifting snow can entrain loose snow particles on the bed into the air, which may be further transported to high altitude by turbulent eddies (King, 1990; Mann et al., 2000; Nemoto and Nishimura, 2004). Drifting snow clouds typically can range in thickness from tens to thousands of meters (Mahesh et al., 2003; Palm et al., 2011), which may not only affect people’s daily life by reducing the visibility and producing local accumulation (Gordon and Taylor, 2009; Mohamed et al., 1998), but also can influence the global climate system evolution by changing the mass and energy balance of ice shelves (Cess and Yagai, 1991; Hanesiak and Wang, 2005; Hinzman et al., 2005; Lenaerts and Broeke, 2012).

Several field experiments on drifting snow storm have been performed (Bintanja, 2001; Budd, 1966; Dingle and Radok, 1961; Doorschot et al., 2004; Gallée et al., 2013; Gordon and Taylor, 2009; Guyomarch et al., 2014; Kobayashi, 1978; Mann et al., 2000; K Nishimura and Nemoto, 2005; Kouichi Nishimura et al., 2015; J. W. Pomeroy and Gray, 1990; Sbuhei, 1985; Schmidt, 1982; Sturm and Stuefer, 2013) since the middle of the last century. However, the measurements are commonly conducted near the surface, thus, the drifting snow features at high altitude are
unknown, and the impacts of these features are difficult to assess. A thorough investigation documenting the evolution process and structure of a full-scale drifting snow storm is essential to understand this natural phenomenon and assess its impacts.

Drifting snow models, on the other hand, offer a panoramic view of the evolution process of drifting snow and thus have become one of the most useful research approaches. Many continuum medium models of drifting snow (Bintanja, 2000; Déry and Yau, 1999; Schneiderbauer and Prokop, 2011; Uematsu et al., 1991; Vionnet et al., 2013) have advanced the knowledge of natural drifting snow to a great extent. However, a particle-tracking drifting snow model is still needed since the particle characteristics and its motion require further investigation. Although a series of particle tracking models (Huang et al., 2016; Huang and Shi, 2017; Huang and Wang, 2015; 2016; Nemoto and Nishimura, 2004; Zhang and Huang, 2008; Zwaaftink et al., 2014) have been established, these models have generally focused on the grain-bed interactions and particle motions near the surface. Thus, a drifting snow model aimed at producing a large-scale drifting snow storm in a turbulent boundary layer deserves further exploration.

In this study, a drifting snow model in the atmospheric boundary layer that focuses on the full-scale drifting snow storm is established. The wind field is solved using a large eddy simulation for the purpose of generating a turbulent atmospheric boundary layer. A subgrid scale (SGS) velocity is also considered to include the diffusive effect of small scale turbulence. Finally, particle motion is calculated using a Lagrangian particle tracking method. The large-scale drifting snow storm is produced under the
actions of large-scale turbulent structures combined with a steady-state snow saltation
boundary condition for particles, and its spatial structures and transport features are
analyzed.

2 Model and methods

2.1 Simulation of a turbulent atmospheric boundary layer

The mesoscale atmosphere prediction pattern ARPS (Advanced Regional Prediction
System, version 5.3.3) is adopted to simulate the turbulent atmospheric boundary
layer, in which the filtered three-dimensional compressible non-hydrostatic
Naiver-Stokes equation is solved (Xue et al., 2001):

\[
\frac{\partial \rho}{\partial t} + \frac{\partial \rho \vec{u}_i}{\partial x_i} = 0
\]  \hfill (1)

\[
\frac{\partial \rho \vec{u}_i}{\partial t} + \frac{\partial \rho \vec{u}_i \vec{u}_j}{\partial x_j} = -\frac{\partial p^*}{\partial x_i} + B\delta_{ij} - \frac{\partial \tau_{ij}}{\partial x_j}
\]  \hfill (2)

where ‘\(\sim\)’ represents variables that are filtered and the filtering scale is
\(\tilde{\Delta} = (\Delta x_1 \Delta x_2 \Delta x_3)^{1/3}\), in which \(\Delta x_i\) is the grid spacing along streamwise \((i = 1)\),
spanwise \((i = 2)\) and vertical direction \((i = 3)\), respectively.

\(p = p(1-q_v/(\varepsilon + q_v))(1+q_v)/(R_a T)\) is the air density, in which \(p\), \(q_v\), \(R_a\) and \(T\) are
the pressure, the specific humidity, the gas constant \((287.0 \text{ J kg}^{-1}\text{K}^{-1})\) and
temperature of the air, respectively, and \(\varepsilon = 0.622\) is a constant. \(u_i\) is the
instantaneous wind speed component, and \(x_i\) is the position coordinate. \(t\) is time,
\(\delta_{ij}\) is the Kronecker delta, \(B = -g \rho'/\rho\) is the buoyancy caused by the air density
perturbation \(\rho'\), and \(g\) is the acceleration due to gravity. \(p^* = p' - \alpha \vec{v}(\rho \vec{u})\) contains
the pressure perturbation term and damping term, where \(\alpha = 0.5\) is the damping
coefficient and $\nabla$ is the divergence. The subgrid stress $\tau_{ij}$ can be expressed as

\[ \tau_{ij} = -2\nu \tilde{S}_{ij} = -2 \left( C_s \tilde{\Lambda} \right)^2 \left| \tilde{S} \right| \tilde{S}_{ij} \]  

(3)

where $\tilde{S}_{ij} = 0.5 \left( \partial \tilde{u}_i / \partial x_j + \partial \tilde{u}_j / \partial x_i \right)$ is the strain rate tensor and $\left| \tilde{S} \right| = \sqrt{2 \tilde{S}_{ij} \tilde{S}_{ij}}$, $C_s$ is Smagorinsky coefficient that is determined locally by the dynamic Lagrangian model (Meneveau et al., 1996).

2.2 Governing equation of particle motion

The trajectory of each snow particle is calculated using a Lagrangian particle tracking method. Since a snow particle has is almost $10^3$ times more dense than air, airborne particles are assumed to process only gravity and fluid drag forces, and the governing equations of particle motion can be expressed as (Dupont et al., 2013; Huang and Wang, 2016; Vinkovic et al., 2006):

\[ \frac{dx_{pi}}{dt} = u_{pi} \]  

(4)

\[ \frac{du_{pi}}{dt} = m_p \frac{V_{xi}}{T_p} f(Re_p) + \delta_{ij} g \]  

(5)

where $x_{pi}$ and $u_{pi}$ are the position coordinate and velocity of the snow particle, respectively. $m_p$ is the mass of the solid particle, $V_r$ is the relative speed between the snow particle and air, and $T_p = \rho_p d_p^2 / 18 \rho v$ is the particle relaxation time, where $\rho_p$ is the particle density (900 kgm$^{-3}$), $d_p$ is the particle diameter and $v = 1.5 \times 10^{-5}$ m$^2$s$^{-1}$ is the kinematic viscosity of air. $f(Re_p)$ can be expressed as (Clift et al., 1978):
where \( Re_p = V_p d / \nu \) is the particle Reynolds number.

Considering the large grid spacing in simulating an atmospheric boundary layer (where the information about turbulent vortices smaller than the grid size is missing), the SGS velocity is also included and attached on the particle. Namely, the local relative is expressed as \( V_{ri} = \tilde{u}_i(x_p) - u_{ri} + u'_i \), in which \( \tilde{u}_i(x_p) \) is the resolved large-scale wind speed at the particle’s position and is determined by the resolved wind speeds of surrounding grid points through the linear interpolation algorithm. The SGS velocity can be calculated from the SGS stochastic model of Vinkovic et al. (2006):

\[
du'_i = \left( -\frac{1}{T_L} + \frac{1}{2\tilde{k}} \frac{d\tilde{k}}{dt} \right) u'_i dt + \sqrt{\frac{4\tilde{k}}{3T_L}} d\eta_i(t) \tag{7}
\]

where \( T_L = 4\tilde{k}/(3C_0\tilde{\varepsilon}) \) is the Lagrangian correlation time scale. Here, \( C_0 = 2.1 \) is the Lagrangian constant, \( \tilde{\varepsilon} = C_x\tilde{k}^{3/2}/\tilde{\Lambda} \) is the subgrid turbulence dissipation rate, \( C_x = 0.41 \) is a constant, and \( d\eta_i \) is the increment of a vector-valued Wiener process with zero mean and variance \( dt \). \( \tilde{k} \) is the subgrid turbulent kinetic energy and can be obtained from the transport equation (Deardorff, 1980):

\[
\frac{\partial \tilde{k}}{\partial t} + \tilde{u}_j \frac{\partial \tilde{k}}{\partial x_j} = \frac{V_j}{3} \frac{\partial}{\partial x_j} \frac{\partial \tilde{\theta}}{\partial x_j} + 2V_i \frac{\partial}{\partial x_j} \left( \nu_j \frac{\partial \tilde{k}}{\partial x_j} \right) + \tilde{\varepsilon} \tag{8}
\]

where \( \tilde{\theta} \) is the potential temperature and \( \tilde{\theta}_0 \) is the surface potential temperature.

### 2.3 Initial conditions of snow particles

To generate a large-scale drifting snow storm, a steady-state snow saltation condition is set as the bottom boundary condition for particles. During drifting snow events, the
sum of residual fluid shear stress $\tau_f$ and particle-borne shear stress $\tau_p$ should be equal to the total shear stress $\tau$, thus, the particle-borne stress can be expressed as:

$$\tau_p = \tau - \tau_f \quad (9)$$

Here, the residual fluid shear stress $\tau_f$ is set to be the threshold shear stress $\tau_{st}$ of drifting snow, which can be read as (Clifton et al., 2006):

$$\tau_{st} = A^2 g d_p \left( \rho_p - \rho \right) \quad (10)$$

in which $A = 0.2$ is a constant, and $d_p$ is the mean diameter of the snow particles.

At the same time, the particle-borne shear stress at the surface can be calculated from the particle trajectories as (Nemoto and Nishimura, 2004):

$$\tau_p = \sum_{i=1}^{n_i} m_i u_{pi \downarrow} - \sum_{i=1}^{n_i} m_i u_{pi \uparrow} \quad (11)$$

where $m_i$ is the mass of particle and $u_{pi \downarrow}$ and $u_{pi \uparrow}$ are the horizontal speeds of impact and lift-off particles, respectively. $n_i$ and $n_t$ are the particle number per unit area in unit time of impact and lift-off grains, respectively, which should be equivalent in steady-state saltation. Thus, the number of lift-off particles per unit area is:

$$n_t = n_i = \frac{\tau_p}{\langle m_i \rangle \left( 1 - \langle e_h \rangle \right) \langle u_{pi \downarrow} \rangle} \quad (12)$$

in which $\langle \rangle$ indicates the overall average, and $e_h$ is the horizontal restitution coefficient of snow particle. According to Sugiura and Maeno (2000), the mean horizontal restitution coefficient can be expressed as:

$$\langle e_h \rangle = \begin{cases} 0.48 \theta_i^{0.01} & v_i \leq 1.27 \text{ms}^{-1} \\ 0.48 \left( \frac{v_i}{1.27} \right)^{-\log_{10} \left( \frac{v_i}{1.27} \right)} \theta_i^{0.01} & v_i > 1.27 \text{ms}^{-1} \end{cases} \quad (13)$$
where $\theta_i$ and $v_i$ are the impact velocity and angle, respectively. Here, $\theta_i$ has a
mean value of approximately 10° (Sugiura and Maeno, 2000), and $\langle v_i \rangle$ is set to be
the threshold of impact velocity. Considering the steady-state saltation condition (one
impact particle generates one ejecta on average), $\langle v_i \rangle$ is determined by setting
ejection number $n_e = 0.51v_i^{0.6}\theta_i^{0.16}$ equal to 1. In this way, the mean horizontal
velocity of impact particles can be obtained through $\langle u_{pis} \rangle = \langle v_i \rangle \cos \langle \theta_i \rangle$.

Then, the velocities of lift-off particles can be obtained from the restitution
coefficient of snow. The horizontal restitution coefficient obeys the normal
distribution with a mean value given in Eq. 13, and a standard variance as follow
(Sugiura and Maeno, 2000):

$$\sigma^2 = 0.07\theta_i^{-0.06} \quad v_i \leq 0.52 \text{ m/s}^{-1}$$
$$0.07\left(\frac{v_i}{0.52}\right)^{-0.06} \theta_i^{-0.06} \quad v_i > 0.52 \text{ m/s}^{-1}$$

(14)

On the other hand, the vertical restitution coefficient can be described by a two
parameter gamma function (see Eq. 17), in which the parameter $\alpha$ and $\beta$ can be
expressed as (Sugiura and Maeno, 2000):

$$\alpha = 1.22\left(\frac{v_i}{0.84}\right)^{\log_\frac{V_i}{0.84} \theta_i^{0.47}} \quad v_i \geq 0.84 \text{ m/s}^{-1}$$
$$0.84 < v_i \leq 1.23 \text{ m/s}^{-1}$$
$$1.22\left(\frac{v_i}{0.84}\right)^{\log_\frac{V_i}{0.84} \theta_i^{0.47}} \left(\frac{v_i}{1.23}\right)^{-2\log_\frac{V_i}{1.23} \theta_i^{0.47}} \quad v_i \geq 1.23 \text{ m/s}^{-1}$$

(15)

$$\beta = 12.85\theta_i^{-1.41} \quad v_i \geq 0.84 \text{ m/s}^{-1}$$
$$0.84 < v_i \leq 1.23 \text{ m/s}^{-1}$$
$$12.85\left(\frac{v_i}{0.84}\right)^{-\log_\frac{V_i}{0.84} \theta_i^{-1.41}} \left(\frac{v_i}{1.23}\right)^{\log_\frac{V_i}{1.23} \theta_i^{-1.41}} \quad v_i \geq 1.23 \text{ m/s}^{-1}$$

(16)
In this condition, if some of the snow particles within the saltation layer are transported to higher in the air by turbulent vortexes (the saltation layer becomes undersaturated), more particles will lift-off from the surface to replenish the saltation layer until a saturated state is reached.

### 2.4 Simulation details

The computational domain is $1000 \, \text{m} \times 500 \, \text{m} \times 1000 \, \text{m}$, with a uniform horizontal grid size of $5 \, \text{m}$ adopted to solve finer vortex structure in the atmospheric boundary layer. The mean grid size in the vertical direction is $20 \, \text{m}$, with a grid refinement algorithm adopted near the surface (the finest grid size is $1 \, \text{m}$). Periodic boundaries are used along streamwise and spanwise dimensions, and the bottom is set as a grid wall. The top is set as an open radiation boundary with a Rayleigh damping layer that is $250 \, \text{m}$ in depth.

The atmosphere is neutral with an initial potential temperature of $300 \, \text{K}$, and an initial relative humidity of $90\%$. The initial wind profile is logarithmic with a surface roughness of $0.1 \, \text{m}$ (Doorschot et al., 2004). Atmospheric turbulence is induced by random initial potential temperature perturbations at the first-level grid level with a maximum magnitude of $0.5 \, \text{K}$, and is sustained by a constant heat flux at the bottom.

The constant heat flux is $50 \, W\text{m}^{-2}$ according to the observation of Pomeroy and Essery (1999). And the evolution time for a turbulent boundary layer is 5 times of the large-eddy turnover time $t_\ast \equiv H/u_\ast$, where $H$ is the boundary layer depth and $u_\ast$ is the friction velocity). Actually, this condition corresponds to a ‘intermediate’ turbulent boundary layer that dominated by wind shear force (Moeng and Sullivan,
190 1994). Thus, the structures of the drifting snow storm should not be affected by the 
191 changing surface heat flux significantly if the surface heat flux is small. Further 
192 simulations with different values of surface heat flux (<100 W m$^{-2}$) also prove this 
193 point.

194 For particles, periodic boundary conditions are also used at lateral boundaries, and 
195 a rebound boundary condition without energy loss is adopted at the model top. The 
196 bottom boundary condition for particles is given in Sect. 2.3, and is updated every 0.5 
197 s. Additionally, each particle represents one particle parcel for the purpose of reducing 
198 computational complexity. In this simulation, each particle parcel contains 10$^7$ snow 
199 particles. The large time step and small time step (acoustic wave integral) for the wind 
200 field calculation are 0.1 s and 0.02 s, respectively, and the particle time step is 
201 determined by the minimum of particle relaxation time.

202

![Particle size distribution per 20 μm](image)

203 **Figure 1.** Size distribution of lift-off snow particles in this simulation.

204 The size distribution of lift-off particles in drifting snow can be well described by 
205 the two-parameter gamma function (Budd, 1966; Gordon and Taylor, 2009; 
206 Nishimura and Nemoto, 2005; Schmidt, 1982):
\[
    f(d_p) = \frac{d_p^{\alpha_p - 1}}{\beta_p^{\alpha_p} \Gamma(\alpha_p)} \exp\left(-\frac{\beta_p}{d_p}\right)
\]  

(17)

where \(\alpha_p\) and \(\beta_p\) are the shape and scale parameter of the distribution, respectively. In this simulation, the diameters of lift-off snow particles are given randomly from a gamma function with the parameters of \(\alpha_p = 4\) and \(\beta_p = 50\), as shown in Fig. 1, which is also consistent with observed particle size distributions (Nishimura and Nemoto, 2005; Schmidt, 1982).

### 3 Results and discussions

#### 3.1 Model validation

![Drifting snow storm at different moments](image)

**Figure** 2. Drifting snow storm at different moments under the friction velocity of 0.29 ms⁻¹. When drifting snow occurs in the atmospheric boundary layer, updrafts and turbulence fluctuations can send snow particles to high altitude, forming a fully developed drifting snow storm. Fig. 2 shows the drifting snow storm in the atmospheric boundary layer at different moments, in which the friction velocity is
$u_* = 0.29 \text{ ms}^{-1}$ and dark spots represent snow particles. It can be seen that drifting snow storm experiences an evolution process from near the surface to high altitudes, which induces the fact that particle concentration decreases along increasing height. The high concentrations of drifting snow cloud are generally below 500 m, though snow particles may reach up to approximately 800 m under this condition. This is also consistent with observations (Mahesh et al., 2003; Palm et al., 2011).

Since a drifting snow storm exhibits a different structure from bottom to top, the evolution of particle number density profile in the drifting snow storm is shown in Fig. 3, which is also compared with measurements of Mann et al. (2000). From this figure, the thickness of the drifting snow layer obviously increases with time, and almost approaches its steady state after 1200 s. At the same time, the particle number density basically decreases with height, which is consistent with the measurements of Mann et al. (2000) at various friction velocities. The predicted particle number density at the surface is much larger than at higher altitude and observations, mainly because the saltating particles are also included.

**Figure 3.** Evolution of particle number density under various friction velocities (a) $0.29 \text{ ms}^{-1}$ and (b) $0.51 \text{ ms}^{-1}$.
Generally, smaller particles are more likely to be transported higher in the air. Fig. 4 shows the variation of modeled average particle diameter versus height, which is also compared with various field measurements (Nishimura and Nemoto, 2005; Schmidt, 1982). Similar to the field observations, the average particle size basically decreases with height at lower altitude but is almost constant above 1 m. The average particle diameter is approximately 75 µm ranging from one meter to hundreds of meters in height, which is also consistent with the measurements of K. Nishimura and Nemoto (2005).

![Graph showing the variation of average particle diameter versus height.](image)

**Figure 4.** Variation of average particle diameter versus height.

Then, the particle size distributions at various heights are also compared with experiment results. As shown in Fig. 5, the heights are 0.05 m, 0.5 m and 1 m. The modeled particle size distributions at various heights are consistent with the measurements (Nishimura and Nemoto, 2005; Schmidt, 1982). Therefore, the established model is able to produce a large-scale drifting snow storm.
Besides, it can be seen that the proportion of particles below 100 \( \mu \text{m} \) in diameter at 0.05 m is smaller than that of the experimental result. The reason could be that mid-air collisions, occurred frequently within the high concentration saltating snow cloud at the near surface, play an important role in conveying larger particles to higher altitude (Carneiro et al., 2013). However, the mid-air collision mechanism is beyond the scope of the current study.
3.2 Snow transport flux

The snow transport flux is of great importance to predict the mass and energy balances of ice sheets. The total transport flux can be obtained from vertical integration of the snow transport flux profile.

![Figure 6. Variations of snow transport flux versus height.](image)

The profiles of snow transport rate, per unit area, per unit time, under various friction velocities are shown in Fig. 6(a). It can be seen that the transport flux undergoes a sharp decrease with height at lower altitude (e.g., below 1.0 m), however, the transport flux tends to decrease rather gentle until almost the top of the drifting snow storm, as shown in Fig. 6(b), probably due to the large-scale turbulent motion and increasing wind speed with height. In other words, the suspension flux of drifting snow at higher altitudes, previously not observed, may be much larger than we previously thought. The mean horizontal wind speed profiles of the fully developed turbulent boundary layer under various friction velocities are shown in Fig. 7. The horizontal wind speed increases with height and changes into a constant above the boundary layer. The rapid decrease of the snow transport flux occurs at about the top of the turbulent boundary layer, mainly because turbulences become weaker above
this height and less particles can be transported to a higher altitude.

Besides, the transition of snow transport flux profile at about 1 m should be mainly caused by the different motion states of particles with different particle sizes, as shown in Fig. 4. Above the critical height, particles generally follow the turbulent flow in the state of suspension because their gravities and relaxation times are small enough. However, plenty of larger particles at the near surface make the particles velocity differs from the wind speed, since particle inertia plays an important role.

![Figure 7](image.png)

Figure 7. Horizontal wind speed profiles of the fully developed turbulent boundary layer under various friction velocities.

In previous studies, only the transport fluxes at the near surface are commonly measured (Mann et al., 2000; Nishimura and Nemoto, 2005; Schmidt, 1982; 1984; Tabler, 1991), thus, the features of the entire transport flux profile is largely unclear, which may result in considerable uncertainties about the total transport flux. The proportions of suspension flux above a given height $h_c$ (referred as $Q_c$) to the total
suspension flux $Q_s$ are shown in Fig. 7, in which snow particles below 0.1 m are not calculated (Mann et al., 2000).

![Figure](image)

**Figure** 8. Proportion of suspension flux above $h_c$ to the total suspension flux under (a) various friction velocities and (b) various surface heat fluxes $Q_s$.

From Fig. 8(a), the contribution of $Q_c$ to the total suspension flux is non-negligible under various $h_c$, the proportion of $Q_c$ when $h_c=100$ m to the total suspension flux has exceeded 30% when the friction velocity is 0.46 ms$^{-1}$. At the same time, the proportion of $Q_c$ to the total suspension flux increases with friction velocity but decreases with increasing $h_c$. From Fig. 8(b), it can be seen that the proportion $Q_c$ to the total suspension flux is only slightly affected by the surface heat flux, which indicates that the structures of drifting snow storm are not sensitive to the surface heat flux under this condition. The influence of surface heat flux is also weakened by the increasing friction velocity, mainly because larger friction velocity results in stronger turbulence under the actions of wind shear.

In this way, not only the snow transport flux, but also the sublimation of suspended snow particles should be reevaluated because the sublimation rate of snow particles higher in the air may be much larger than near the surface due to the lower
air humidity and greater wind speed at higher altitude (Mann et al., 2000; Nishimura and Nemoto, 2005; Schmidt, 1982; 1984; Tabler, 1991).

3.3 **Structures in a drifting snow storm**

In a drifting snow storm, particles aggregate locally and produce special spatial structures (as shown in Fig. 2). These structures should be directly related to the turbulence structures present in the atmospheric boundary layer. Drifting snow storms without atmospheric turbulence are shown in Fig. 9. This simulation is achieved by replacing the resolved wind speed at particle’s position \( \bar{u}_i(\vec{x}_p) \) with a given value obtained from the standard logarithmic profile, and the other model settings and simulation procedures stay the same with other simulations. In this way, the effect of large-scale turbulent structures on the development of the drifting snow storm vanishes. Compared with Fig. 2, drifting snow particles mainly travel at the near surface with a uniform spatial distribution when atmospheric turbulence is not included.

![Figure 9. Drifting snow storm without atmospheric turbulence under friction velocity of 0.35 ms\(^{-1}\).](image)
It is known that snow particles will become suspended if the local vertical wind speed exceeds the terminal velocity of particle. In a turbulent atmospheric boundary layer, there exists a large amount of turbulent structures with different scales and shapes. The vertical wind speed component of large-scale turbulence (namely, updraft) plays an important role in carrying snow particles to high altitude, while small scale turbulence (e.g., the SGS fluctuating velocity) tends to spread particles from high concentration zones to low concentration zones. As shown in Fig. 10(a), at the initial period of a drifting snow storm, the structures in the drifting snow storm are consistent with large-scale updrafts, and snow particles are mainly located in the updraft. With the further development of the drifting snow storm, as shown in Fig. 10(b), more snow particles are scattered around the updraft bubbles although high concentration particle clouds are still in the wind bubbles. When drifting snow storm approaches its saturated state, snow particle clouds are almost connected together with numerous high concentration zones inside.

**Figure 10.** Evolution of drifting snow storm and vertical wind speed bubbles under friction velocity of 0.35 ms$^{-1}$, and wind bubbles are iso-surface of vertical wind speed with a value of 1.0 ms$^{-1}$ (corresponding to the critical wind speed at which the particle of mean particle size becomes suspended particle, since the maximum diameter of
suspended particles is found to be approximately equal to the mean particle size of the lift-off particles).

The evolution of the depth of drifting snow storm can be divided into three typical stages. In sequence, these phases are the rapid growth phase, the gentle growth stage, and an equilibrium state, as shown in Fig. 11. Here, the depth of drifting snow storm refers to the average height of the topmost particle during this period (100 s). The rapid growth stage is mainly driven by large-scale turbulent motion, while the turbulent diffusion by the SGS fluctuating velocity is the main contributor to the gentle growth stage. The duration of second stage decreases with increasing friction velocity, which mainly comes from the stronger turbulent diffusion under larger friction velocities.

**Figure 11.** Time evolutions of the thickness of drifting snow storm under various friction velocities.
friction velocities.

At the same time, the time required for the drifting snow storm to reach its maximum thickness decreases with friction velocity, ranging from about 1200 s to approximate 600 s when the friction velocity increases from 0.29 ms\(^{-1}\) to 0.46 ms\(^{-1}\).

The thicknesses of saturated drifting snow storms are almost constant with a value approximately 900 m under different friction velocities, probably because the boundary layer depth as well as the surface heat flux are unchanged. Higher domain heights are also tested with the same model settings, and the thickness of the drifting snow seems basically unchanged. Drifting snow storm with difference thicknesses may be achieved by changing the initial state of the air and surface heat flux. Thus, the final thickness of a drifting snow storm should be largely dependent on the maximum height of atmospheric turbulences.

4 Conclusion

In this work, large-scale drifting snow storms are simulated in a large eddy simulation combined with a particle tracking model that includes subgrid scale velocity fluctuations. A typical drifting snow storm of several hundred meters in depth is generated, and the structure of the particle cloud with different concentrations is also produced. The transport flux profile has obviously different slopes near the surface compared to higher altitudes, that is, transport flux at near surface decreases with height sharply, but decreases more gentle at higher altitude. Previous studies may largely underestimate the total transport during drifting snow storms.

At the same time, the evolution of the thickness of drifting snow storm generally
contains three stages. Drifting snow storm development generally begins with a rapid
growth stage driven by the large scale atmospheric turbulent motions, followed by a
gentle growth stage driven by the SGS fluctuating wind speed, before reaching an
equilibrium stage when the drifting snow approaches a saturated state. The second
stage becomes shorter with increasing friction velocity, mainly because stronger
turbulence under higher friction velocity enhances the turbulent diffusion of particles.

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A simulation of the large-scale drifting snow storm in a turbulent boundary layer

Zhengshi Wang\textsuperscript{1,2}, Shuming Jia \textsuperscript{1,2}*

\textsuperscript{1} State Key Laboratory of Aerodynamics, China Aerodynamic Research and Development Center, Mianyang Sichuan 621000, China

\textsuperscript{2} Computational Aerodynamics Institute, China Aerodynamics Research and Development Center, Mianyang, Sichuan 621000, China

*Corresponding: Shuming Jia (jiashm17@cardc.cn)
Abstract. Drifting snow storm is an important aeolian process that reshapes alpine glaciers and polar ice shelves, and it may also affect the climate system and hydrological cycle since flying snow particles exchange considerable mass and energy with air flow. Prior studies have rarely considered the full-scale drifting snow storm in the turbulent boundary layer, thus, the transportation feature of snow flow higher in the air and its contribution are largely unknown. In this study, a large eddy simulation is combined with a subgrid scale velocity model to simulate the atmospheric turbulent boundary layer, and a Lagrangian particle tracking method is adopted to track the trajectories of snow particles. A drifting snow storm that is hundreds of meters in depth and exhibits obvious spatial structures is produced. The snow transport flux profile at high altitude, previously not observed, is quite different from that near the surface, thus, the extrapolated transport flux profile may largely underestimate the total transport flux. At the same time, the development of a drifting snow storm involves three typical stages, the rapid growth, the gentle growth and the equilibrium stages, in which the large-scale updrafts and subgrid scale fluctuating velocities basically dominate the first and second stage, respectively. This research provides an effective way to get an insight into natural drifting snow storms.
1 Introduction

Snow, one type of solid precipitation, is an important source of material to mountain glaciers and polar ice sheets, which are widespread throughout high and cold regions (Chang et al., 2016; Gordon and Taylor, 2009; Lehning et al., 2008). A common natural phenomenon over snow cover is the drifting snow storm, which occurs when the wind speed exceeds a critical value (Doorschot et al., 2004; Li and Pomeroy, 1997; Sturm and Stuefer, 2013). Drifting snow can entrain loose snow particles on the bed into the air, which may be further transported to high altitude by turbulent eddies (King, 1990; Mann et al., 2000; Nemoto and Nishimura, 2004). Drifting snow clouds typically can range in thickness from tens to thousands of meters (Mahesh et al., 2003; Palm et al., 2011), which may not only affect people’s daily life by reducing the visibility and producing local accumulation (Gordon and Taylor, 2009; Mohamed et al., 1998), but also can influence the global climate system evolution by changing the mass and energy balance of ice shelves (Cess and Yagai, 1991; Hanesiak and Wang, 2005; Hinzman et al., 2005; Lenaerts and Broeke, 2012).

Several field experiments on drifting snow storm have been performed (Bintanja, 2001; Budd, 1966; Dingle and Radok, 1961; Doorschot et al., 2004; Gallée et al., 2013; Gordon and Taylor, 2009; Guyomarch et al., 2014; Kobayashi, 1978; Mann et al., 2000; K Nishimura and Nemoto, 2005; Kouichi Nishimura et al., 2015; J. W. Pomeroy and Gray, 1990; Sbuhei, 1985; Schmidt, 1982; Sturm and Stuefer, 2013) since the middle of the last century. However, the measurements are commonly conducted near the surface, thus, the drifting snow features at high altitude are
unknown, and the impacts of these features are difficult to assess. A thorough investigation documenting the evolution process and structure of a full-scale drifting snow storm is essential to understand this natural phenomenon and assess its impacts.

Drifting snow models, on the other hand, offer a panoramic view of the evolution process of drifting snow and thus have become one of the most useful research approaches. Many continuum medium models of drifting snow (Bintanja, 2000; Déry and Yau, 1999; Schneiderbauer and Prokop, 2011; Uematsu et al., 1991; Vionnet et al., 2013) have advanced the knowledge of natural drifting snow to a great extent. However, a particle-tracking drifting snow model is still needed since the particle characteristics and its motion require further investigation. Although a series of particle tracking models (Huang et al., 2016; Huang and Shi, 2017; Huang and Wang, 2015; 2016; Nemoto and Nishimura, 2004; Zhang and Huang, 2008; Zwaaitink et al., 2014) have been established, these models have generally focused on the grain-bed interactions and particle motions near the surface. Thus, a drifting snow model aimed at producing a large-scale drifting snow storm in a turbulent boundary layer deserves further exploration.

In this study, a drifting snow model in the atmospheric boundary layer that focuses on the full-scale drifting snow storm is established. The wind field is solved using a large eddy simulation for the purpose of generating a turbulent atmospheric boundary layer. A subgrid scale (SGS) velocity is also considered to include the diffusive effect of small scale turbulence. Finally, particle motion is calculated using a Lagrangian particle tracking method. The large-scale drifting snow storm is produced under the
actions of large-scale turbulent structures combined with a steady-state snow saltation boundary condition for particles, and its spatial structures and transport features are analyzed.

2 Model and methods

2.1 Simulation of a turbulent atmospheric boundary layer

The mesoscale atmosphere prediction pattern ARPS (Advanced Regional Prediction System, version 5.3.3) is adopted to simulate the turbulent atmospheric boundary layer, in which the filtered three-dimensional compressible non-hydrostatic Naiver-Stokes equation is solved (Xue et al., 2001):

\[
\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i}(\rho \tilde{u}_i) = 0
\]  

(1)

\[
\frac{\partial \rho \tilde{u}_i}{\partial t} + \frac{\partial}{\partial x_j}(\rho \tilde{u}_i \tilde{u}_j) = - \frac{\partial \rho^*}{\partial x_i} + B \delta_{ij} - \frac{\partial \tau_{ij}}{\partial x_j}
\]  

(2)

where \( \tilde{\Delta} = (\Delta x_1 \Delta x_2 \Delta x_3)^{1/3} \), in which \( \Delta x_i \) is the grid spacing along streamwise \( (i=1) \), spanwise \( (i=2) \) and vertical direction \( (i=3) \), respectively.

\[ \rho = p(1-q_r/(\varepsilon+q_r))(1+q_r)/(R_g T) \] is the air density, in which \( p \), \( q_r \), \( R_g \) and \( T \) are the pressure, the specific humidity, the gas constant (287.0 \( J kg^{-1} K^{-1} \)) and temperature of the air, respectively, and \( \varepsilon=0.622 \) is a constant. \( u_i \) is the instantaneous wind speed component, and \( x_i \) is the position coordinate. \( t \) is time, \( \delta_{ij} \) is the Kronecker delta, \( B = -g \rho' / \rho \) is the buoyancy caused by the air density perturbation \( \rho' \), and \( g \) is the acceleration due to gravity. \( \rho' = \rho - \rho \tilde{\epsilon} (\rho u) \) contains the pressure perturbation term and damping term, where \( \alpha = 0.5 \).
coefficient and $\nabla$ is the divergence. The subgrid stress $\tau_{ij}$ can be expressed as (Smagorinsky, 1963):

$$\tau_{ij} = -2\nu_s \tilde{S}_{ij} = -2 \left( C_s \tilde{A} \right)^2 \left| \tilde{S} \right| \tilde{S}_{ij}$$  \hspace{1cm} (3)

where $\tilde{S}_{ij} = 0.5 \left( \partial u_i / \partial x_j + \partial u_j / \partial x_i \right)$ is the strain rate tensor and $\left| \tilde{S} \right| = \sqrt{2 \tilde{S}_{ij} \tilde{S}_{ij}}$, $C_s$ is Smagorinsky coefficient that is determined locally by the dynamic Lagrangian model (Meneveau et al., 1996).

2.2 Governing equation of particle motion

The trajectory of each snow particle is calculated using a Lagrangian particle tracking method. Since a snow particle has is almost $10^3$ times more dense than air, airborne particles are assumed to process only gravity and fluid drag forces, and the governing equations of particle motion can be expressed as (Dupont et al., 2013; Huang and Wang, 2016; Vinkovic et al., 2006):

$$\frac{dx_{pi}}{dt} = u_{pi}$$  \hspace{1cm} (4)

$$\frac{du_{pi}}{dt} = \frac{m_p V_{ri}}{T_p} f(Re_p) + \delta_{ij} g$$  \hspace{1cm} (5)

where $x_{pi}$ and $u_{pi}$ are the position coordinate and velocity of the snow particle, respectively. $m_p$ is the mass of the solid particle, $V_r$ is the relative speed between the snow particle and air, and $T_p = \rho_p d_p^2 / 18 \rho_v$ is the particle relaxation time, where $\rho_p$ is the particle density ($900 \text{ kgm}^{-3}$), $d_p$ is the particle diameter and $\nu = 1.5 \times 10^{-5}$ is the kinematic dynamic viscosity of air. $f(Re_p)$ can be expressed as (Clift et al., 1978):
where \( Re_p = V_p d / \nu \) is the particle Reynolds number.

Considering the large grid spacing in simulating an atmospheric boundary layer (where the information about turbulent vortices smaller than the grid size is missing), the SGS velocity is also included and attached on the particle. Namely, the local relative is expressed as \( V_{ri} = \bar{u} - u + u' \), in which \( \bar{u} \) is the resolved large-scale wind speed at the particle’s position and is determined by the resolved wind speeds of surrounding grid points through the linear interpolation algorithm. The SGS velocity can be calculated from the SGS stochastic model of Vinkovic et al. (2006):

\[
\frac{d\bar{u}'}{dt} = \left( -\frac{1}{T_L} + \frac{1}{2} \frac{d\tilde{k}}{dt} \right) u' + \sqrt{\frac{4\tilde{k}}{3T_L}} \bar{\eta} (t) \tag{7}
\]

where \( T_L = 4\tilde{k}/(3C_0\tilde{\varepsilon}) \) is the Lagrangian correlation time scale. Here, \( C_0 = 2.1 \) is the Lagrangian constant, \( \tilde{\varepsilon} = C_\varepsilon \tilde{k}^{3/2} / \tilde{\Gamma} \) is the subgrid turbulence dissipation rate, \( C_\varepsilon = 0.41 \) is a constant, and \( d\bar{\eta} \) is the increment of a vector-valued Wiener process with zero mean and variance \( dt \). \( \tilde{k} \) is the subgrid turbulent kinetic energy and can be obtained from the transport equation (Deardorff, 1980):

\[
\frac{\partial \tilde{k}}{\partial t} + \bar{u}_i \frac{\partial \tilde{k}}{\partial x_j} = \frac{\nu}{\theta_0} \frac{\partial^2 \tilde{k}}{\partial x_i \partial x_j} + 2\nu_s \tilde{S}_{ij} + 2 \frac{\partial}{\partial x_j} \left( \nu_i \frac{\partial \tilde{k}}{\partial x_j} \right) + \tilde{\varepsilon} \tag{8}
\]

where \( \theta \) is the potential temperature and \( \theta_0 \) is the surface potential temperature.

2.3 Initial conditions of snow particles

To generate a large-scale drifting snow storm, a steady-state snow saltation condition...
is set as the bottom boundary condition for particles. During drifting snow events, the sum of residual fluid shear stress $\tau_f$ and particle-borne shear stress $\tau_p$ should be equal to the total shear stress $\tau$, thus, the particle-borne stress can be expressed as:

$$\tau_p = \tau - \tau_f \quad (9)$$

Here, the residual fluid shear stress $\tau_f$ is set to be the threshold shear stress $\tau_{sf}$ of drifting snow, which can be read as (Clifton et al., 2006):

$$\tau_f = A^2 g \bar{d}_p \left( \rho_p - \rho \right) \quad (10)$$

in which $A = 0.2$ is a constant, $g$ is the gravity acceleration, and $\bar{d}_p$ is the mean diameter of the snow particles.

At the same time, the particle-borne shear stress at the surface can be calculated from the particle trajectories as (Nemoto and Nishimura, 2004):

$$\tau_p = \sum_{i=1}^{n_\downarrow} m_i u_{pi\downarrow} - \sum_{i=1}^{n_\uparrow} m_i u_{pi\uparrow} \quad (11)$$

where $m_i$ is the mass of particle and $u_{pi\downarrow}$ and $u_{pi\uparrow}$ are the horizontal speeds of impact and lift-off particles, respectively. $n_\downarrow$ and $n_\uparrow$ are the particle number per unit area in unit time of impact and lift-off grains, respectively, which should be equivalent in steady-state saltation. Thus, the number of lift-off particles per unit area is:

$$n_\uparrow = n_\downarrow = \left\langle \frac{\tau_p}{m_i(1-\langle e_h\rangle)\langle u_{pi\downarrow}\rangle} \right\rangle \quad (12)$$

in which $\langle \cdot \rangle$ indicates the overall average, and $e_h$ is the horizontal restitution coefficient of snow particle. According to Sugiura and Maeno (2000), the mean horizontal restitution coefficient can be expressed as:
where \( \theta_i \) and \( v_i \) are the impact velocity and angle, respectively. Here, \( \theta_i \) has a mean value of approximately \( 10^\circ \) (Sugiura and Maeno, 2000), and \( \langle v_i \rangle \) is set to be the threshold of impact velocity. Considering the steady-state saltation condition (one impact particle generates one ejecta on average), \( \langle v_i \rangle \) is determined by setting ejection number \( n_e = 0.51v_i^{0.6}\theta_i^{0.16} \) equal to 1. In this way, the mean horizontal velocity of impact particles can be obtained through \( \langle u_{pi(i)} \rangle = \langle v_i \rangle \cos(\theta_i) \).

Then, the velocities of lift-off particles can be obtained from the restitution coefficient of snow. The horizontal restitution coefficient obeys the normal distribution with a mean value given in Eq. 13, and a standard variance as follow (Sugiura and Maeno, 2000):

\[
\sigma^2 = \begin{cases} 0.07\theta_i^{-0.06} & \text{if } v_i \leq 0.52 \text{ ms}^{-1} \\ 0.07\left(\frac{v_i}{0.52}\right)^{-0.06}\theta_i^{-0.06} & \text{if } v_i > 0.52 \text{ ms}^{-1} \end{cases} \tag{14}
\]

On the other hand, the vertical restitution coefficient can be described by a two parameter gamma function (see Eq. 17), in which the parameter \( \alpha \) and \( \beta \) can be expressed as (Sugiura and Maeno, 2000):

\[
\alpha = \begin{cases} 1.22\theta_i^{0.47} & \text{if } v_i \geq 0.84 \text{ ms}^{-1} \\ 1.22\left(\frac{v_i}{0.84}\right)^{\log_{1.23}\theta_i^{0.47}}\theta_i^{0.47} & \text{if } 0.84 < v_i \leq 1.23 \text{ ms}^{-1} \\ 1.22\left(\frac{v_i}{0.84}\right)^{\log_{1.23}\theta_i^{0.47}}\left(\frac{v_i}{1.23}\right)^{-2\log_{1.23}\theta_i^{0.47}}\theta_i^{0.47} & \text{if } v_i \geq 1.23 \text{ ms}^{-1} \end{cases} \tag{15}
\]
In this condition, if some of the snow particles within the saltation layer are transported to higher in the air by turbulent vortexes (the saltation layer becomes undersaturated), more particles will lift-off from the surface to replenish the saltation layer until a saturated state is reached.

2.4 Simulation details

The computational domain is 1000 m $\times$ 500 m $\times$ 1000 m, with a uniform horizontal grid size of 5 m adopted to solve finer vortex structure in the atmospheric boundary layer. The mean grid size in the vertical direction is 20 m, with a grid refinement algorithm adopted near the surface (the finest grid size is 1 m). Periodic boundaries are used along streamwise and spanwise dimensions, and the bottom is set as a grid wall. The top is set as an open radiation boundary with a Rayleigh damping layer that is 250 m in depth.

The atmosphere is neutral with an initial potential temperature of 300 K, and an initial relative humidity of 90%. The initial wind profile is logarithmic with a surface roughness of 0.1 m (Doorschot et al., 2004). Atmospheric turbulence is induced by random initial potential temperature perturbations at the first-level grid level with a maximum magnitude of 0.5 K, and is sustained by a constant heat flux at the bottom. The constant heat flux is 50 W m$^{-2}$ according to the observation of Pomeroy and Essery (1999). And the evolution time for a turbulent boundary layer is 5 times of the...
large-eddy turnover time $t_*$ ($\equiv H/u_*$, where $H$ is the boundary layer depth and $u_*$ is the friction velocity). Actually, this condition corresponds to a ‘intermediate’ turbulent boundary layer that dominated by wind shear force (Moeng and Sullivan, 1994). Thus, the structures of the drifting snow storm should not be affected by the changing surface heat flux significantly if the surface heat flux is small. Further simulations with different values of surface heat flux ($<100 \text{ } Wm^{-2}$) also prove this point.

For particles, periodic boundary conditions are also used at lateral boundaries, and a rebound boundary condition without energy loss is adopted at the model top. The bottom boundary condition for particles is given in Sect. 2.3, and is updated every 0.5 s. Additionally, each particle represents one particle parcel for the purpose of reducing computational complexity. In this simulation, each particle parcel contains $10^7$ snow particles. The large time step and small time step (acoustic wave integral) for the wind field calculation are 0.1 s and 0.02 s, respectively, and the particle time step is determined by the minimum of particle relaxation time.

**Figure 1.** Size distribution of lift-off snow particles in this simulation.
The size distribution of lift-off particles in drifting snow can be well described by the two-parameter gamma function (Budd, 1966; Gordon and Taylor, 2009; Nishimura and Nemoto, 2005; Schmidt, 1982):

\[
f(d) = \frac{d_{\alpha p}^{\alpha p - 1}}{\beta_p^{\alpha p} \Gamma(\alpha_p)} \exp\left(-\frac{\beta_p}{d_{\alpha p}}\right)
\]

(17)

where \(d\) is the particle diameter, and \(\alpha_p\) and \(\beta_p\) are the shape and scale parameter of the distribution, respectively. In this simulation, the diameters of lift-off snow particles are given randomly from a gamma function with the parameters of \(\alpha_p = 4\) and \(\beta_p = 50\), as shown in Fig. 1, which is also consistent with observed particle size distributions (Nishimura and Nemoto, 2005; Schmidt, 1982).

3 Results and discussions

3.1 Model validation

Figure 2. Drifting snow storm at different moments under the friction velocity of 0.29 ms\(^{-1}\).

When drifting snow occurs in the atmospheric boundary layer, updrafts and
turbulence fluctuations can send snow particles to high altitude, forming a fully
developed drifting snow storm. Fig. 2 shows the drifting snow storm in the
atmospheric boundary layer at different moments, in which the friction velocity is
$u_* = 0.29 \text{ ms}^{-1}$ and dark spots represent snow particles. It can be seen that drifting
snow storm experiences an evolution process from near the surface to high altitudes,
which induces the fact that particle concentration decreases along increasing height.
The high concentrations of drifting snow cloud are generally below 500 m, though
snow particles may reach up to approximately 800 m under this condition. This is also
consistent with observations (Mahesh et al., 2003; Palm et al., 2011).

Since a drifting snow storm exhibits a different structure from bottom to top, the
evolution of particle number density profile in the drifting snow storm is shown in Fig.
3, which is also compared with measurements of Mann et al. (2000). From this figure,
the thickness of the drifting snow layer obviously increases with time, and almost
approaches its steady state after 1200 s. At the same time, the particle number density
basically decreases with height, which is consistent with the measurements of Mann
et al. (2000) at various friction velocities. The predicted particle number density at the
surface is much larger than at higher altitude and observations, mainly because the
saltating particles are also included.
Generally, smaller particles are more likely to be transported higher in the air. Fig. 4 shows the variation of modeled average particle diameter versus height, which is also compared with various field measurements (Nishimura and Nemoto, 2005; Schmidt, 1982). Similar to the field observations, the average particle size basically decreases with height at lower altitude but is almost constant above 1 m. The average particle diameter is approximately 75 µm ranging from one meter to hundreds of meters in height, which is also consistent with the measurements of K Nishimura and Nemoto (2005).
Then, the particle size distributions at various heights are also compared with experiment results. As shown in Fig. 5, the heights are 0.05 m, 0.5 m and 1 m. The modeled particle size distributions at various heights are consistent with the measurements (Nishimura and Nemoto, 2005; Schmidt, 1982). Therefore, the established model is able to produce a large-scale drifting snow storm.
Figure 5. Particle size distribution at various heights.

Besides, it can be seen that the proportion of particles below 100 µm in diameter at 0.05 m is smaller than that of the experimental result. The reason could be that mid-air collisions, occurred frequently within the high concentration saltating snow cloud at the near surface, play an important role in conveying larger particles to higher altitude (Carneiro et al., 2013). However, the mid-air collision mechanism is beyond the scope of the current study.
3.2 Snow transport flux

The snow transport flux is of great importance to predict the mass and energy balances of ice sheets. The total transport flux can be obtained from vertical integration of the snow transport flux profile.

Figure 6. Variations of snow transport flux versus height.

The profiles of snow transport rate, per unit area, per unit time, under various friction velocities are shown in Fig. 6(a). It can be seen that the transport flux undergoes a sharp decrease with height at lower altitude (e.g., below 1.0 m), however, the transport flux tends to decrease rather gentle until almost the top of the drifting snow storm, as shown in Fig. 6(b), probably due to the large-scale turbulent motion and increasing wind speed with height. In other words, the suspension flux of drifting snow at higher altitudes, previously not observed, may be much larger than we previously thought. The mean horizontal wind speed profiles of the fully developed turbulent boundary layer under various friction velocities are shown in Fig. 7. The horizontal wind speed increases with height and changes into a constant above the boundary layer. The rapid decrease of the snow transport flux occurs at about the top of the turbulent boundary layer, mainly because turbulences become weaker above
this height and less particles can be transported to a higher altitude.

Besides, the transition of snow transport flux profile at about 1 m should be mainly caused by the different motion states of particles with different particle sizes, as shown in Fig. 4. Above the critical height, particles generally follow the turbulent flow in the state of suspension because their gravities and relaxation times are small enough. However, plenty of larger particles at the near surface make the particles velocity differs from the wind speed, since particle inertia plays an important role.

![Figure 7. Horizontal wind speed profiles of the fully developed turbulent boundary layer under various friction velocities.](image)

In previous studies, only the transport fluxes at the near surface are commonly measured (Mann et al., 2000; Nishimura and Nemoto, 2005; Schmidt, 1982; 1984; Tabler, 1990), thus, the features of the entire transport flux profile is largely unclear, which may result in considerable uncertainties about the total transport flux. The proportions of suspension flux above a given height \( h_c \) (referred as \( Q_c \)) to the total
suspension flux $Q_s$ are shown in Fig. 7, in which snow particles below 0.1 m are not calculated (Mann et al., 2000).

![Figure 8](attachment:image.png)

**Figure 8.** Proportion of suspension flux above $h_c$ to the total suspension flux under (a) various friction velocities and (b) various surface heat fluxes $Q_s$.

From Fig. 8-(a), the contribution of $Q_c$ to the total suspension flux is non-negligible under various $h_c$, the proportion of $Q_c$ when $h_c=100$ m to the total suspension flux has exceeded 30% when the friction velocity is 0.46 m s$^{-1}$. At the same time, the proportion of $Q_c$ to the total suspension flux increases with friction velocity but decreases with increasing $h_c$. From Fig. 8-(b), it can be seen that the proportion $Q_c$ to the total suspension flux is only slightly affected by the surface heat flux, which indicates that the structures of drifting snow storm are not sensitive to the surface heat flux under this condition. The influence of surface heat flux is also weakened by the increasing friction velocity, mainly because larger friction velocity results in stronger turbulence under the actions of wind shear.

In this way, not only the snow transport flux, but also the sublimation of suspended snow particles should be reevaluated because the sublimation rate of snow particles higher in the air may be much larger than near the surface due to the lower
air humidity and greater wind speed at higher altitude (Mann et al., 2000; Nishimura and Nemoto, 2005; Schmidt, 1982; 1984; Tabler, 1990).

3.3 Structures in a drifting snow storm

In a drifting snow storm, particles aggregate locally and produce special spatial structures (as shown in Fig. 2). These structures should be directly related to the turbulence structures present in the atmospheric boundary layer. Drifting snow storms without atmospheric turbulence are shown in Fig. 9. This simulation is achieved by replacing the resolved wind speed at particle’s position ($\bar{u}_i(\tilde{x}_p)$) with a given value obtained from the standard logarithmic profile, and the other model settings and simulation procedures stay the same with other simulations. In this way, the effect of large-scale turbulent structures on the development of the drifting snow storm vanishes. Compared with Fig. 2, drifting snow particles mainly travel at the near surface with a uniform spatial distribution when atmospheric turbulence is not included.

**Figure 9.** Drifting snow storm without atmospheric turbulence under friction velocity of 0.35 ms$^{-1}$. 

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It is known that snow particles will become suspended if the local vertical wind speed exceeds the terminal velocity of particle. In a turbulent atmospheric boundary layer, there exists a large amount of turbulent structures with different scales and shapes. The vertical wind speed component of large-scale turbulence (namely, updraft) plays an important role in carrying snow particles to high altitude, while small scale turbulence (e.g., the SGS fluctuating velocity) tends to spread particles from high concentration zones to low concentration zones. As shown in Fig. 10(a), at the initial period of a drifting snow storm, the structures in the drifting snow storm are consistent with large-scale updrafts, and snow particles are mainly located in the updraft. With the further development of the drifting snow storm, as shown in Fig. 10(b), more snow particles are scattered around the updraft bubbles although high concentration particle clouds are still in the wind bubbles. When drifting snow storm approaches its saturated state, snow particle clouds are almost connected together with numerous high concentration zones inside.

Figure 10. Evolution of drifting snow storm and vertical wind speed bubbles under friction velocity of 0.35 ms\(^{-1}\), and wind bubbles are iso-surface of vertical wind speed with a value of 1.0 ms\(^{-1}\) (corresponding to the critical wind speed at which the particle of mean particle size becomes suspended particle, since the maximum diameter of
suspended particles is found to be approximately equal to the mean particle size of the lift-off particles).

The evolution of the depth of drifting snow storm can be divided into three typical stages. In sequence, these phases are the rapid growth phase, the gentle growth stage, and an equilibrium state, as shown in Fig. 11. Here, the depth of drifting snow storm refers to the average height of the topmost particle during this period (100 s). The rapid growth stage is mainly driven by large-scale turbulent motion, while the turbulent diffusion by the SGS fluctuating velocity is the main contributor to the gentle growth stage. The duration of second stage decreases with increasing friction velocity, which mainly comes from the stronger turbulent diffusion under larger friction velocities.

**Figure** 11. Time evolutions of the thickness of drifting snow storm under various
friction velocities.

At the same time, the time required for the drifting snow storm to reach its maximum thickness decreases with friction velocity, ranging from about 1200 s to approximate 600 s when the friction velocity increases from 0.29 ms\(^{-1}\) to 0.46 ms\(^{-1}\).

The thicknesses of saturated drifting snow storms are almost constant with a value approximately 900 m under different friction velocities, probably because the boundary layer depth as well as the surface heat flux are unchanged. Higher domain heights are also tested with the same model settings, and the thickness of the drifting snow seems basically unchanged. Drifting snow storm with difference thicknesses may be achieved by changing the initial state of the air and surface heat flux. Thus, the final thickness of a drifting snow storm should be largely dependent on the maximum height of atmospheric turbulentences.

4 Conclusion

In this work, large-scale drifting snow storms are simulated in a large eddy simulation combined with a particle tracking model that includes subgrid scale velocity fluctuations. A typical drifting snow storm of several hundred meters in depth is generated, and the structure of the particle cloud with different concentrations is also produced. The transport flux profile has obviously different slopes near the surface compared to higher altitudes, that is, transport flux at near surface decreases with height sharply, but decreases more gentle at higher altitude. Previous studies may largely underestimate the total transport during drifting snow storms.

At the same time, the evolution of the thickness of drifting snow storm generally
contains three stages. Drifting snow storm development generally begins with a rapid
growth stage driven by the large scale atmospheric turbulent motions, followed by a
gentle growth stage driven by the SGS fluctuating wind speed, before reaching an
equilibrium stage when the drifting snow approaches a saturated state. The second
stage becomes shorter with increasing friction velocity, mainly because stronger
turbulence under higher friction velocity enhances the turbulent diffusion of particles.

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